

## Math 1496 - Sample Test 2

1. Find the derivative of the following

(i)  $y = x \sin^{-1} x$

(ii)  $y = \ln(x^2 + e^x)$

(iii)  $x^2 - xy + y^4 = x - y$

2. If  $f(x) = x^3 + x + 1$  find  $(f^{-1})'(3)$ .

3. Find the absolute minimum and maximum of the following on the given interval

(i)  $f(x) = 1 - x^2$  on  $[-2, 3]$

(ii)  $f(x) = 2x^3 - 15x^2 + 24x$  on  $[0, 3]$

4. State the Mean Value Theorem. Verify the Mean Value Theorem for the following

(i)  $f(x) = x^3 - x$  on  $[0, 2]$

(ii)  $f(x) = \frac{x}{x+2}$  on  $[1, 10]$

5. If  $y = x(x - 4)^3$  calculate the following

(i) The critical numbers

(ii) When  $y$  is increasing and decreasing.

(iii) Determine whether any of the critical numbers are minimum or maximum.

(iv) When  $y$  is concave up and down and determine the points of inflection.

(v) Then sketch the curve.

6. A ladder 13 feet long is resting against the wall of a house. The base of the ladder is pulled away from the wall at a rate of 2 ft/sec. At what rate is the tip of the ladder moving down the wall when the base of the ladder is 5 ft away from the wall?

7. A paper cup in the shape of an inverted cone with height 10 cm and a base of radius 3 cm, is being filled at a rate of  $2 \text{ cm}^3/\text{min}$ . Find the rate of change in the height of the water when the height of the water is 5 cm.