

The Quantum Mechanics of Two Interacting Realities

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Abstract.

We consider how two physical realities can be represented over a common set of spacetime coordinates. As an example we will utilize quantum electrodynamics since this is a familiar and well-understood theory. We will designate one world the 'red' one and the other the 'green' one. We will try to show how they can interact in a physically plausible way. We will also examine whether such an interacting theory is renormalizable. It will be shown that we can extend these ideas to the Standard Model. There are implications for this theory if we consider General Relativity and these will be discussed briefly. If there are, in fact, such other realities these could provide a plausible explanation for dark matter.

Introduction.

The possibility of multiple universes and other realities has often been discussed (1). Everett's Many-Worlds Interpretation is, perhaps, to be regarded as the starting point. In most cases and respects, these other universes are precluded from interacting with ours and there is, of course, a good reason for this – we have no compelling evidence for the existence of such interactions. All the same, it might be interesting to theorize about how another reality might interact with our own. But this can only be done subject to the constraint that nothing implausible is proposed – anything that would plainly violate our everyday observations must not result from such speculation. It should be mentioned that another reality, one that shared our spacetime and influenced it gravitationally, could be considered a candidate for dark matter provided it interacted with us so weakly and infrequently as to be seldom observed.

I will try to show that a theory of multiple realities can, in fact, be constructed using quantum electrodynamics (QED) as a simple and familiar example. We can imagine one reality – call it the 'red' one populated with 'red' electrons and 'red' photons. We will suppose that there is another, 'green,' reality populated with 'green' electrons and photons. There will exist a *common coordinate system* between them. We will take this idea in a very literal way and just imagine that the various fields are all functions of a common coordinate system defined over a shared Minkowski spacetime. If we are observers living in the 'red' reality we will imagine that the 'green' reality exists all around us and is defined over whatever spacetime coordinate system we decide to use. Ordinarily, we just cannot see this 'green' reality because its particles do not interact with our 'red' ones. We will introduce a new function, $c(\mathbf{x}, t)$, which reflects the degree to which the 'red' and 'green' realities interact with one another. The reader will want a more mathematically rigorous description of this common coordinate system and such will be forthcoming. We will always assume that the laws of physics are the same in both realities and that the two kinds of electrons have the same mass and charge in their respective realities.

QED in Two Realities.

We start out by writing the Lagrangian as it would look if these realities were always completely independent:

$$1) \quad L_{em} = \overline{\psi}_R [\gamma^\mu [i \partial_\mu - e A_{R\mu}] - m] \psi_R - \frac{1}{4} F_R^{\mu\nu} F_{R\mu\nu} \\ + \overline{\psi}_G [\gamma^\mu [i \partial_\mu - e A_{G\mu}] - m] \psi_G - \frac{1}{4} F_G^{\mu\nu} F_{G\mu\nu}.$$

The objects ψ_R , A_R , are understood to pertain to the 'red' reality. The 'G' subscript means they belong to the 'green' reality. A common spacetime coordinate system is shared by both the 'red' and 'green' particles. $F_R^{\mu\nu}$ is the electromagnetic field strength tensor appropriate to the 'red' world. $F_G^{\mu\nu}$ pertains to the 'green' reality. Now an interaction between these realities could occur if there were to take place a *mixing* of A_R and A_G in their interaction with the electron fields according to:

$$2) \quad \begin{aligned} A_{R\mu} &\longrightarrow (1 + c(\mathbf{x}, t)^2)^{-1/2} [A_{R\mu} + c(\mathbf{x}, t) A_{G\mu}] \quad \text{and} \\ A_{G\mu} &\longrightarrow (1 + c(\mathbf{x}, t)^2)^{-1/2} [A_{G\mu} + c(\mathbf{x}, t) A_{R\mu}] \quad \text{where } c(\mathbf{x}, t) \text{ is taken to be a real scalar field.} \end{aligned}$$

Note that this mixing of quantum fields is confined to the photon fields. It is not applied to the electron fields. Nor is it applied within the electromagnetic field strength tensors. When $c(\mathbf{x}, t) = 0$ there is no interaction. As $c(\mathbf{x}, t)$ becomes larger 'red' observers begin to experience some of the 'green' reality and vice-versa. $(1 + c(\mathbf{x}, t)^2)^{-1/2}$ functions as a kind of normalization factor. Under the influence of this transformation the Lagrangian becomes:

$$3) \quad \begin{aligned} L_{\text{em}} = & \overline{\psi}_R [\gamma^\mu [i \partial_\mu - e (1 + c(\mathbf{x}, t)^2)^{-1/2} [A_{R\mu} + c(\mathbf{x}, t) A_{G\mu}]] - m] \psi_R - \frac{1}{4} F_R^{\mu\nu} F_{R\mu\nu} \\ & + \overline{\psi}_G [\gamma^\mu [i \partial_\mu - e (1 + c(\mathbf{x}, t)^2)^{-1/2} [A_{G\mu} + c(\mathbf{x}, t) A_{R\mu}]] - m] \psi_G - \frac{1}{4} F_G^{\mu\nu} F_{G\mu\nu}. \end{aligned}$$

We will assume, for the moment, that $c(\mathbf{x}, t)$ is roughly constant over the spacetime volume of interest. Also note that $c(\mathbf{x}, t)$ is, right now, not a dynamical variable of this theory. It is like a physical "constant" that changes with time and space. While this new Lagrangian maintains local gauge invariance only under circumstances where $c(\mathbf{x}, t)$ is constant it has the advantage of resulting, under these circumstances, in simple Feynman rules and a physics which, in many respects, corresponds with that we would like to see for a theory that doesn't grossly violate observed reality. In situations where $c(\mathbf{x}, t)$ varies things become more complicated. And we must address this problem since our theory would be either not interesting or not believable, physically, if $c(\mathbf{x}, t)$ could never change.

These new Feynman rules are similar to the familiar ones but with two important differences: Firstly, the vertices connecting an incoming and outgoing 'red' electron (or positron) line with a 'red' photon contribute with a coupling constant $e (1 + c(\mathbf{x}, t)^2)^{-1/2}$. It is likewise for the 'green' particles. Secondly, new vertices appear which connect incoming and outgoing 'red' electron (or positron) lines with a 'green' photon and incoming and outgoing 'green' electron (or positron) lines with a 'red' photon (*fig.1*). (In the first two cases we omit drawing the graphs with the outgoing electrons exchanged. But we know they are there.) These contribute with a coupling constant which is $e c(\mathbf{x}, t) (1 + c(\mathbf{x}, t)^2)^{-1/2}$. Consider the scattering of one 'red' electron off another in the presence of an interaction. To find the probability amplitude for this process (to second order in the coupling constant) we will sum the amplitudes corresponding to the usual Feynman diagrams and new diagrams in which it is a 'green' virtual photon that is being exchanged. Straightforward arithmetic shows that the overall coupling constant is still e . Thus the resulting amplitude is unchanged by the presence of the interaction. The contribution from the 'green' virtual photon compensates exactly for the reduction in the coupling strength of the normal interaction. This is encouraging – as long as we are dealing with interactions between

'red' particles and other 'red' particles, electromagnetism should continue to work normally in the 'red' world even if $c(\mathbf{x}, t)$ became different from zero. The same situation would obtain in the 'green' world. Suppose, instead, that we try to scatter 'red' electrons off of 'green' electrons. Now things are a little different. In each of the two relevant Feynman diagrams would be a vertex connecting either 'green' fermions with a virtual 'red' photon or 'red' fermions with a 'green' virtual photon. Arithmetic again yields a simple result. If we are 'red' observers looking at the behavior of 'red' electrons, we would have to conclude that the 'green' electrons had a charge that was only $2 c(\mathbf{x}, t) (1 + c(\mathbf{x}, t)^2)^{-1} e$. We would always assume that our 'red' electrons have charge e . If the 'green' electrons scatter abnormally, it must be because they have a reduced charge. Also, since there are no vertices connecting an incoming 'red' electron with an outgoing 'green' electron, the scattering would be the same as that produced by two non-identical particles; this makes sense as we would not want to say that 'green' and 'red' particles are indistinguishable.

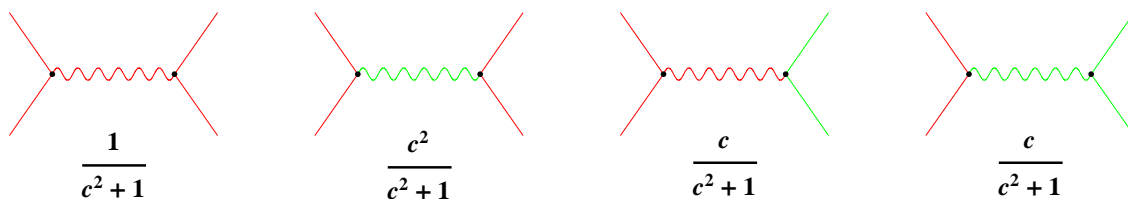


fig.1

The Classical Limit.

We want to know what the physics resulting from this would look like to an ordinary, macroscopic, observer. And it is not clear how much more we can do in a quantum mechanical way. There, if we do not regard $c(\mathbf{x}, t)$ as a constant, we have no easy way of doing the math. Let us look at Equation 3) from a semi-classical point of view. We must recall that, according to Dirac theory, the 4-current density in the 'red' world is given by $e \overline{\psi}_R \gamma^\mu \psi_R$, and by $e \overline{\psi}_G \gamma^\mu \psi_G$, in the 'green' one. Varying Equation 3) by $A_{R\mu}$ we find:

$$4) \quad F_R^{\mu\nu},_{\nu} = J^\mu / (1 + c(\mathbf{x}, t)^2)^{1/2} + \tilde{J}^\mu c(\mathbf{x}, t) / (1 + c(\mathbf{x}, t)^2)^{1/2}$$

where J^μ denotes the 4-current density in the 'red' world, and \tilde{J}^μ that in the 'green' world. Varying by $A_{G\mu}$, we find a corresponding equation for things the 'green' world. Let us now vary Equation 3) by $\overline{\psi}_R$ so as to get the Dirac equation for the behavior of 'red' electrons. We find:

$$5) \quad [\gamma^\mu [i \partial_\mu - e (1 + c(\mathbf{x}, t)^2)^{-1/2} [A_{R\mu} + c(\mathbf{x}, t) A_{G\mu}]] - m] \psi_R = 0.$$

This tells us what effective "4-potential" the 'red' electron is responding to. We can perform the same exercise for the 'green' Dirac equation. We obtain, as a practical matter, a Lorentz force law for 'red' electron which reads:

$$6) \quad m \ddot{x}_R^\mu = e \left(F_R^{\mu\nu} / (1 + c(\mathbf{x}, t)^2)^{1/2} + F_G^{\mu\nu} c(\mathbf{x}, t) / (1 + c(\mathbf{x}, t)^2)^{1/2} - \right. \\ \left. (1 + c(\mathbf{x}, t)^2)^{-3/2} [c(\mathbf{x}, t) (c(\mathbf{x}, t)^{\cdot\mu} A_{R\nu} - c(\mathbf{x}, t)_{,\nu} A_R^\mu) - \right. \\ \left. (c(\mathbf{x}, t)^{\cdot\mu} A_{G\nu} - c(\mathbf{x}, t)_{,\nu} A_G^\mu) \right] \dot{x}_R^\nu.$$

And we will obtain a reversed version for the 'green' electron, having the 'R's and 'G's interchanged.

Equation 6) is actually rather remarkable as it shows that we can deduce useful things by *not* trying to use the quantized theory. Equation 6) follows from 5) in the most simple way. We *know* that Dirac's Equation – the one with A_μ as we are used to seeing it – gives us the familiar Lorentz force law when translated into the classical world. (It is actually rather hard to deduce this mathematically. But it is certainly true.) Thus by treating the strange term that appears in Equation 5) *exactly as if* it were A_μ (i.e. constructing an $F_{\mu\nu}$ from it) we arrive at Equation 6). And it must be true.

It will be observed that this equation of motion does not respect local gauge invariance, nor should it. As has been mentioned, gauge invariance requires the constancy of $c(\mathbf{x}, t)$. And simply specifying a gauge will not help us here. We could require, for example, $\partial_\mu A_{R,G}^\mu = 0$. But this, alone, is insufficient. We could imagine adding a 4-vector, Λ^μ , to either A^μ and this would not disturb the gauge condition so long as $\Lambda^\mu_{,\mu} = 0$. It would, however, change Equation 6). The $A_{R,G}^\mu$ in this theory must be definite, unambiguous, and not subject to the addition of any factors. We would be better off endowing both of our photons with a vanishingly small mass. In effect we add terms $\epsilon^2 A_{R,G}^\mu A_{R,G\mu}$ to the Lagrangians for our two photons (understanding that ϵ is so small that it can be taken to zero at the end of any practical calculation). The dynamical equations for the two A fields become Proca equations. This is invaluable both because it automatically ensures $\partial_\mu A_{R,G}^\mu = 0$ *and* also rules out the addition of any intrusive gradients to our A fields.

No assumptions regarding the constancy of $c(\mathbf{x}, t)$ have been made in deriving Equations 4) and 6) (and their two 'green' counterparts). These will be true under any circumstances. It seems likely that, under many circumstances, $c(\mathbf{x}, t)$ can be treated as, more-or-less, a constant. This allows us to make some simplifications to the mathematics. Since all we are interested in is the effective field that 'red' or 'green' electrons respond to, let us simplify matters by writing:

$$7) \quad F^{\mu\nu} = F_R^{\mu\nu} / (1 + c(\mathbf{x}, t)^2)^{1/2} + F_G^{\mu\nu} c(\mathbf{x}, t) / (1 + c(\mathbf{x}, t)^2)^{1/2} \text{ and}$$

$$8) \quad \tilde{F}^{\mu\nu} = F_G^{\mu\nu} / (1 + c(\mathbf{x}, t)^2)^{1/2} + F_R^{\mu\nu} c(\mathbf{x}, t) / (1 + c(\mathbf{x}, t)^2)^{1/2}.$$

It now becomes possible to write Maxwell's equations and the Lorentz force law, in the presence of an interaction, in a more compact form:

$$9) \quad F^{\mu\nu}_{,\nu} = J^\mu + 2 \tilde{J}^\mu c(\mathbf{x}, t) / (1 + c(\mathbf{x}, t)^2)$$

$$10) \quad F_{\alpha\beta,\gamma} + F_{\beta\gamma,\alpha} + F_{\gamma\alpha,\beta} = 0$$

$$11) \quad \tilde{F}^{\mu\nu}{}_{,\nu} = \tilde{J}^\mu + 2 J^\mu c(\mathbf{x}, t) / (1 + c(\mathbf{x}, t)^2)$$

$$12) \quad \tilde{F}_{\alpha\beta,\gamma} + \tilde{F}_{\beta\gamma,\alpha} + \tilde{F}_{\gamma\alpha,\beta} = 0$$

$$13) \quad m \ddot{x}_R^\mu = e F^\mu{}_\nu \dot{x}_R^\nu$$

$$14) \quad m \ddot{x}_G^\mu = e \tilde{F}^\mu{}_\nu \dot{x}_G^\nu$$

where $F^{\mu\nu}$ denotes the classical electromagnetic field strength tensor, measured by the 'red' physicist, and $\tilde{F}^{\mu\nu}$ that measured similarly by the 'green' one.

Now the 4-divergences of the left-hand sides of Equation 4), and the 'green' version thereof, both vanish identically owing to the antisymmetry of $F_R^{\mu\nu}$ and $F_G^{\mu\nu}$. The current densities should also have vanishing 4-divergences. This implies that:

$$15) \quad c(\mathbf{x}, t)_{,\mu} J^\mu = 0 \text{ and}$$

$$c(\mathbf{x}, t)_{,\mu} \tilde{J}^\mu = 0.$$

Equations 15) put some definite constraints on what $c(\mathbf{x}, t)$ can do. In most reasonable and electrically neutral worlds we can assume the electromagnetic currents to be zero in most places. At worst they will, in the classical limit, be non-zero only at the specific locations of 'red' and 'green' point electrons or positrons. Elsewhere $c(\mathbf{x}, t)$ is free to change subject to whatever other physics guides it.

By J^μ we mean $e \overline{\psi}_R \gamma^\mu \psi_R$ and likewise for the 'green' current. This may cause some confusion because it would seem that $J^0 = e \psi_R^\dagger \psi_R$ which would have to be negative everywhere. Of course, J^0 is, properly, to be understood as a field theoretic operator. (We have presented some arguments in terms of one-particle Dirac theory just to establish a few simple facts.) Considered as an operator J^0 would, in most places, have a positive expectation value in a world full of 'red' positrons and a negative one if the world were dominated by 'red' electrons. Thus J^μ assumes a role identical to that of a classical electromagnetic current. Really, by J^μ we mean $\langle \Psi | J^\mu | \Psi \rangle$ where $|\Psi\rangle$ designates the state of this twofold World in a kind of extended Fock space populated with both 'red' and 'green' particles. We assume this Fock space to have a vacuum state and that its basis states are constructed from this by the sequential action of the multiple creation operators that correspond to the 'green' and 'red' particles in our theory. We assume, also, that 'green' and 'red' operators always commute – they simply do not see one another and act on their respective Fock "subspaces" independently. We work in the Dirac Interaction Picture.

Now we can imagine mixing A_R and A_G in a very different, but also physically reasonable way. We can write:

$$3') \quad L_{em} = \overline{\psi}_R [\gamma^\mu [i \partial_\mu - e (1 + c(\mathbf{x}, t)^2)^{-1/2} [A_{R\mu} + c(\mathbf{x}, t) A_{G\mu}]] - m] \psi_R - \frac{1}{4} F_R^{\mu\nu} F_{R\mu\nu} \\ + \overline{\psi}_G [\gamma^\mu [i \partial_\mu - e (1 + c(\mathbf{x}, t)^2)^{-1/2} [A_{G\mu} - c(\mathbf{x}, t) A_{R\mu}]] - m] \psi_G - \frac{1}{4} F_G^{\mu\nu} F_{G\mu\nu}.$$

Again, no change occurs in the electromagnetic interactions between particles of the same color, regardless of

what $c(\mathbf{x}, t)$ does. Also, there are *no* electromagnetic interactions between 'red' and 'green' particles whatsoever in areas where $c(\mathbf{x}, t)$ is constant. In this case equations 9) and 11) become even simpler:

$$9') \quad F^{\mu\nu}{}_{, \nu} = J^{\mu}$$

$$11') \quad \tilde{F}^{\mu\nu}{}_{, \nu} = \tilde{J}^{\mu} \text{ where } \tilde{F}^{\mu\nu} = F_G^{\mu\nu} / (1 + c(\mathbf{x}, t)^2)^{1/2} - F_R^{\mu\nu} c(\mathbf{x}, t) / (1 + c(\mathbf{x}, t)^2)^{1/2}.$$

Equation 6) changes as well. It remains the same for 'red' electrons. But for the 'green' ones we must not only exchange R and G but also change $c(\mathbf{x}, t)$ to $-c(\mathbf{x}, t)$. We will refer to this as the Type-II model. It will have observable consequences; if, for instance, we consider the Compton scattering of a 'red' photon off a 'red' electron in a high- $c(\mathbf{x}, t)$ region there will be some chance of seeing a 'green' photon emerge. We will usually discuss the (more symmetrical) Type-I model but will also consider this alternative.

The Role of $c(\mathbf{x}, t)$.

There are many things this theory cannot tell us about $c(\mathbf{x}, t)$. The most important of these is whether it should be treated as a dynamical variable of the theory – one with its own place in the Lagrangian of our twofold reality – or as a completely external variable. First, let's suppose it's the latter way. Then $c(\mathbf{x}, t)$ is rather like a physical "constant" that happens to vary with space and time.

Suppose that $c(\mathbf{x}, t)$ is, initially, zero everywhere but that it becomes a bit bigger than zero in a small area where both a 'red' and a 'green' physicist have an electron of their own type under observation. As the 'red' electron starts to move under the influence of its 'green' counterpart, and vice-versa, both physicists will be amazed that 4-momentum is not being conserved. But there is no reason why it should be. Conservation of 4-momentum follows from Noether's Theorem and relies on the independence of the Lagrangian from space and time. By allowing $c(\mathbf{x}, t)$ to change with space and time we have destroyed this invariance. Conservation of 4-momentum will only hold if $c(\mathbf{x}, t)$ is constant everywhere. In a small area where $c(\mathbf{x}, t)$ is constant there will be a conserved 4-momentum but it will be the sum of the 4-momenta present in both worlds plus any interaction energy between the variously colored particles involved. Charge conservation also becomes an ambiguous concept when $c(\mathbf{x}, t)$ changes.

Maybe $c(\mathbf{x}, t)$ ought to be regarded as a dynamical variable of this theory rather than as something that has to be introduced in an arbitrary way. It would then be possible to define a rigorously conserved 4-momentum. One could incorporate $c(\mathbf{x}, t)$ into the Lagrangian 3) by any number of means. Suppose we try the simplest one:

$$16) \quad L_{\text{real}} = L_{\text{em}} + \kappa c(\mathbf{x}, t)_{, \mu} c(\mathbf{x}, t)^{\mu} \text{ (where } \kappa \text{ is a real constant).}$$

If we assume $c(\mathbf{x}, t)$ is always quite small we end up with a wave equation for $c(\mathbf{x}, t)$ having a source term proportional to:

$$17) \quad J^{\mu} A_{G\mu} + \tilde{J}^{\mu} A_{R\mu}.$$

It is not obvious that such an equation leads us to any productive physics. We would need simultaneous knowl-

edge of both the 'red' and 'green' realities to evaluate it in any particular case. And we can, of course, propose other 'kinetic' terms for $c(\mathbf{x}, t)$, if we prefer those, and end up with a different theory. In any case, such a theory would lead to a conserved 4-momentum derivable from L_{real} . But this would no longer resemble that which we conventionally recognize as 4-momentum. It would contain terms involving $c(\mathbf{x}, t)$.

We do not want a theory that blatantly contradicts observed reality. Adopting something like Equation 16) might lead to consequences that would have been noticed long ago unless we arrange things (e.g. κ) in such a way that those consequences would always be so small as to be imperceptible. And that would not lead to an interesting theory. Also, Equations 15) already put severe constraints on what $c(\mathbf{x}, t)$ can do. Imposing any further dynamical constraints on it might confine us to a very uninteresting theory. We are, perhaps, better off regarding $c(\mathbf{x}, t)$ as something like a physical "constant" that varies according to its own unknown physics. If $c(\mathbf{x}, t)$ does not become very large in very many places, we might well not have noticed it. Also it seems to seldom fluctuate much over atomic time and distance scales. If it did, this could result in easily noticed disturbances to our atoms' behavior.

The Importance of Congruence Between the Realities.

Referring back to Equations 15) we notice some interesting things. The 4-gradient of $c(\mathbf{x}, t)$ is constrained only where J^μ or \tilde{J}^μ differs from zero. Where they do not, $c(\mathbf{x}, t)$ is free to change as it wishes. Suppose that both J^μ and \tilde{J}^μ differ from zero in some area. This places two constraints on the 4-gradient of $c(\mathbf{x}, t)$ and would restrict more stringently the forms an interaction could take. Of course, if $J^\mu = \tilde{J}^\mu$ the number of constraint equations drops back to one. It should then be easier for an interaction to take place. The less different the two realities are the more freedom $c(\mathbf{x}, t)$ has to change. And, if we want to consider a kinetic term (as in Equation 16)) we see that the source term, Equation 17), would usually average out to zero if the 'red' and 'green' worlds were completely different and unrelated. If the two realities are rather similar the source term may have a better chance of becoming large in certain locations.

Is Such a Theory Renormalizable?

I consider this in the simple case where $c(\mathbf{x}, t)$ may be treated as a constant over the volume of spacetime where the interactions of interest are taking place. The 'red' and 'green' photon loops that figure in calculating the vertex correction and electron self-mass terms sum to results that differ in no essential way from those encountered in normal QED. Of course, there are twice as many particles to keep in mind. But, otherwise, nothing important is changed and we can renormalize these in the usual way.

The fermion loops that renormalize the photon propagators – the vacuum polarization terms – require a more careful treatment. These loops can and do link incoming 'red' photon lines to outgoing 'green' photon lines and vice-versa. There is, accordingly, some amplitude for a 'red' photon to be created at one vertex only to be absorbed as a 'green' photon somewhere else. We were very happy when the second-order diagrams in *fig. 1* showed that 'red' electrons would see each other's charges as e no matter what $c(\mathbf{x}, t)$ did. We are less happy when we inspect *fig. 2* and find the intrusion of an additional factor $4 \left(c(\mathbf{x}, t)^2 / (1 + c(\mathbf{x}, t)^2) \right)$ coming from the one-loop diagrams. This problem shows up at the e^4 order. The closed loops diverge and must be regularized.

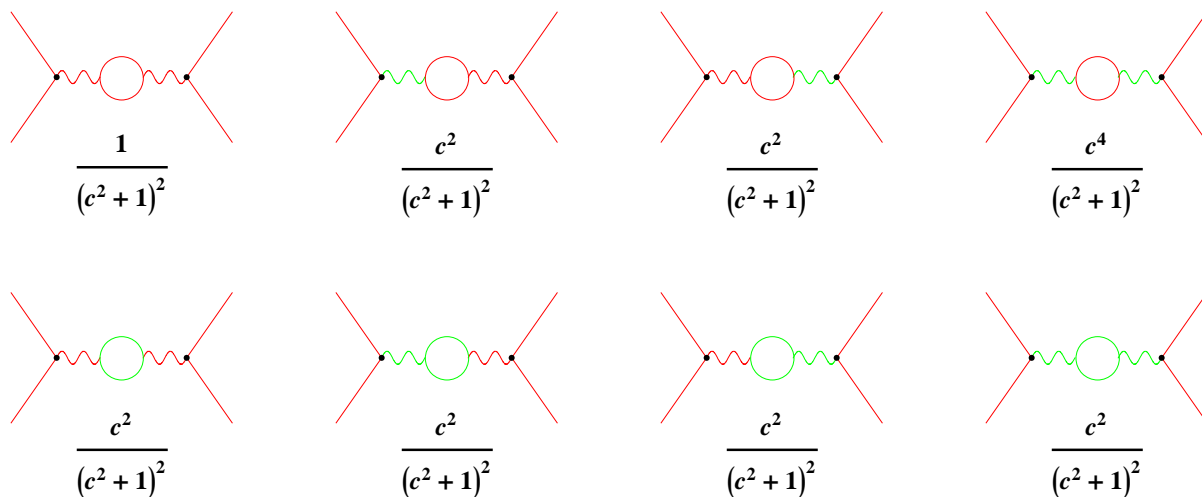


fig.2

A propagator represents the amplitude for a particle to be created at one spacetime point and absorbed at another. It is meant to be evaluated in its free-field theory and no interactions should be allowed for it once it has been renormalized. A 'red' photon must therefore always be absorbed as 'red.' But there are many ways in which this can happen. Let us look at *fig. 3*. At the one-loop level everything seems fine. But we see now just what the problem is at the two-loop level. Again we find the factor $4 (c(x, t)^2/(1 + c(x, t)^2))$. By renormalizing this situation (there are a variety of methods we can imagine using) we absorb it into the new physical charge, e_{phys} , which is what we actually measure in the laboratory. This accommodates the problem that seemed to stem from *fig. 2*. Electron scattering will then proceed through finite diagrams just like the (loop-less) two left-most diagrams in *fig. 1*. but with e replaced by e_{phys} . 'Red' virtual photon lines will stay 'red' and 'green' ones 'green.' It should be pointed out that a real ($k^\mu k_\mu = 0$) photon will always retain its color. Moving at c these states are frozen, so to speak, in time.

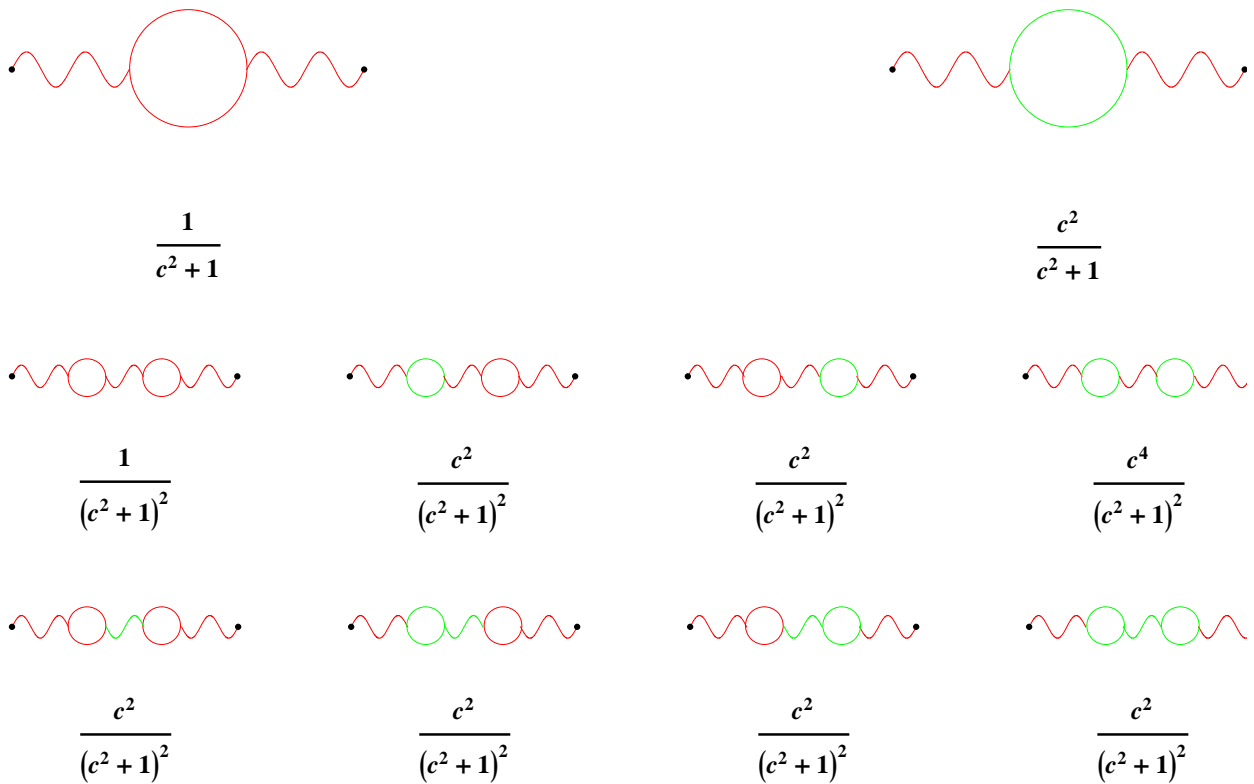


fig.3

Actually, there is an easier way of arriving at the same result. We can simply rotate A_R and A_G into $(A_1 + A_2)/\sqrt{2}$ and $(A_1 - A_2)/\sqrt{2}$, respectively. (We are not mixing anything or doing any strange physics here. We are just giving new names to old things.) Re-expressed in terms of these fields we get a new Equation 3). The kinetic terms for the $A_{R,G}$ fields stay, formally, unchanged. The newly written fermionic terms give rise to vertices such that A_1 photon lines, although they may be interspersed with 'red' and 'green' electron loops (whose net contributions always sum to one), never turn into A_2 lines, and likewise for the A_2 . So both the A_1 and A_2 photon lines may be renormalized *exactly* as they are in normal QED. After this the result is simply rewritten in terms of A_R and A_G . The renormalization of the Type-II theory is particularly simple since, here, 'red' and 'green' photon lines can never interconvert. We can renormalize this theory in the ordinary way.

$c(\mathbf{x}, t)$ under Various Circumstances.

Suppose that both worlds are always identical – $\psi_R = \psi_G$, $A_R = A_G$, always. Equation 3) now describes a situation void of any distinction between 'red' and 'green' particles. It describes a single reality with an electromagnetic coupling constant that depends on $c(\mathbf{x}, t)$. If this is constant everywhere we can just reset e and recover perfectly normal physics. If $c(\mathbf{x}, t)$ varies we end up with a strange world in which the electromagnetic interaction changes from place to place. We do not seem to live in such a world and this simple possibility is ruled out unless $c(\mathbf{x}, t)$ never varies by more than an unnoticeable amount. Dropping the requirement that $\psi_R = \psi_G$ leads to the same situation but with 'red' and 'green' electrons that do not behave as identical particles but still interact through a common photon. We are better off assuming that our two worlds are not constrained to be identical.

If $c(\mathbf{x}, t)$ were to become just slightly different from zero over a defined area and time, 'red' observers

within this area would be able to "see" the 'green' and 'red' photons emitted by vibrating 'green' electrons in the 'green' world. These would become more apparent as $c(\mathbf{x}, t)$ increased. Now it might be possible for $c(\mathbf{x}, t)$ to become less than zero. If this happened the 'green' electrons would appear to be positively charged – a strange, but not unimaginable, circumstance.

Even if $c(\mathbf{x}, t)$ became different from zero in some spacetime volume, this would not affect the local electromagnetic interactions between 'red' particles and other 'red' particles, and 'green' ones with 'green' in that volume. If we lived in the 'red' reality, we would not see our 'red' atoms fall apart if $c(\mathbf{x}, t)$ changed. This is, of course, very encouraging if we want this idea to be considered plausible. But this is not to say that $c(\mathbf{x}, t)$ would be devoid of observable consequences, even in our 'red' world. Consider the decay of 'red' positronium. We can easily write down the necessary Feynman diagrams. We find that the overall rate of its decay, in an area where $c(\mathbf{x}, t)$ is non-zero, is reduced by a factor of $1 - c(\mathbf{x}, t)^2 / (1 + c(\mathbf{x}, t)^2)^2$. In particular, the rate at which it will decay into two 'red' photons is reduced by a factor of $1 / (1 + c(\mathbf{x}, t)^2)^2$. If we are 'red' observers looking at all this from outside the high $c(\mathbf{x}, t)$ area we will not be able to see the green photons resulting from this process. We will only see our 'red' positronium decaying, somewhat slowly, into normal 'red' photons sometimes, into only one 'red' photon other times, and, occasionally, into nothing at all! A rather disconcerting, but potentially observable, situation. In this situation neither 4-momentum nor spin will always be conserved, according to the 'red' observer.

Suppose that a 'red' observer ventured into a spacetime volume where $c(\mathbf{x}, t) = 1$. Within that volume his atoms would function normally. If their electrons vibrated they would they would give off 'red' and 'green' photons in equal measure. He could also see 'green' objects, within that area, just as if they were his familiar 'red' objects. Suppose that, outside this area, far away, where $c(\mathbf{x}, t) = 0$, there are vibrating 'red' and 'green' electrons which, of course, are giving off only 'red' and 'green' photons, respectively. The observer inside the $c(\mathbf{x}, t) = 1$ region would be able to see the light from both of these. But its intensity would be reduced by a factor of 1/2 in both cases.

Let us examine a still more radical case. Imagine that $c(\mathbf{x}, t) \rightarrow \infty$ in a small spatiotemporal region with it being zero everywhere without. There a 'red' observer could respond only to 'green' photons. If he ventured into such a region he would see himself surround by the 'green' reality – he would respond to the 'green' photons hitting his retina. He could no longer respond to 'red' photons from "his" world. An observer in the 'green' reality could see him since, as the electrons in his body vibrated, they would give off 'green' photons. If he left this region, or if $c(\mathbf{x}, t)$ returned to zero, neither could see the other again. We might wonder if he could breathe in this region – maybe there is no oxygen in the other reality. Surely he could, as 'red' oxygen molecules would diffuse into his region where they would interact with him as 'green' molecules which his now-'green' lungs could process. Perhaps he sees a friendly 'green' observer in the other reality. Could he shake hands with him? No. If he tried to reach his hand out of the interaction region it would simply find itself back in 'red' reality and be able to interact only with 'red' things. But suppose this strange region of spacetime were surrounded by a small area of milder interaction where $c(\mathbf{x}, t)$ was only, say, about 1. There both 'red' and 'green' atoms could interact and a handshake might be possible. It would probably be a strange affair. The forces that repel my hand as I try to pass it through yours are a complicated combination of electrostatic, dispersion, and Pauli exchange forces. These latter would be absent since 'red' and 'green' fermions are not identical. I am unsure what form an interaction between 'red' and 'green' matter would take under macroscopic circumstances such as these. But it would be peculiar.

Recalling the Type-II theory we might think it was without any observable consequences. But such is

not the case. If a 'red' observer is in an area where $c(\mathbf{x}, t) = 0$ and, far away in an area where $c(\mathbf{x}, t)$ is rather large, a green electron is vibrating that observer will be able to see the 'red' photons it is emitting. If he wandered into the $c(\mathbf{x}, t) \rightarrow \infty$ region described above he would also see himself surrounded by the 'green' reality. But he could never, possibly, shake hands with the friendly 'green' observer – $c(\mathbf{x}, t)$ would always be the same in the area where their hands tried to interact therefore no interaction could be possible.

The Standard Model.

It is of interest to see whether this idea can be generalized to a more realistic physical model. We will examine, briefly, the Standard Model. We will employ the notation familiar from (2).

Since we are considering two realities we just double the Lagrangian to include both the 'red' and 'green' fermion fields. More interesting is L_{scalar} - the one that contains the Higgs boson. There will now be two of these - a 'red' one and a 'green' one. They will share the same properties and symmetry-breaking $V[\varphi]$ potential and couple in the usual way to the gauge fields of their own color. We will assume that, when $c(\mathbf{x}, t)$ differs from zero, all the gauge fields transform according to $f_R \rightarrow (f_R + c(\mathbf{x}, t) f_G) / (1 + c(\mathbf{x}, t)^2)^{1/2}$ and vice-versa for the f_G s both in respect of L_{scalar} and the Lagrangians that describe the 'red' and 'green' fermionic fields. The kinetic terms for the gauge fields are, as before, left unchanged.

What results is a theory that differs from the conventional Standard Model in only two ways (besides the obvious fact that there are now two colors of each particle to keep track of). We end up with interaction terms from L_{fermion} that give rise to vertices where, for instance, a 'red' neutrino goes in emerging as a 'red' electron and a 'green' W^+ . A similar analysis pertains as in *fig. 1*. From L_{scalar} (both 'red' and 'green' together) comes the new term:

$$18) \quad 4 c(\mathbf{x}, t)/(1 + c(\mathbf{x}, t)^2) [(g'^2 + g^2) Z_{R\mu} Z_G^\mu + g^2 (W_{R-\mu}^- W_G^{+\mu} + W_{G-\mu}^- W_R^{+\mu})]$$

which we are not sure how to interpret physically. It is encouraging to see that the 'red' and 'green' physical photons resulting from this variation of the Standard Model do not acquire any mass or couple in abnormal ways. And the masses of the other particles are not affected by $c(\mathbf{x}, t)$.

An observer scattering 'red' neutrinos off of 'red' electrons would see no change regardless of what $c(\mathbf{x}, t)$ did. But there would still be consequences if $c(\mathbf{x}, t)$ changed. Consider the β -decay of a 'red' neutron. It is mediated by the release of a W^- boson from a 'red' d quark which then becomes a 'red' u quark. This boson then becomes an electron and an antineutrino. If $c(\mathbf{x}, t)$ were different from zero the decay into a 'red' electron and antineutrino would proceed unchanged. But decay could also proceed through different channels into a 'green' electron and antineutrino pair. So the rate of β -decay would be increased by a factor of $1 + 4 c(\mathbf{x}, t)^2/(1 + c(\mathbf{x}, t)^2)^2$. If the resulting 'green' electron and antineutrino moved out into a $c(\mathbf{x}, t) = 0$ area the 'red' physicist, looking at all of this, would conclude that a neutron just turned into a proton without producing anything.

The Common Coordinate System and General Relativity.

Things would only become complicated if the 'red' and 'green' spacetimes were to have different geometries so we need look at this problem in a different manner. We should suppose, instead, that there is only one metric

and one spacetime in which both our realities live. This common metric would have to be derived equally from both the 'red' and 'green' worlds according to $G_{\mu\nu} = 8 \pi (T_{R\mu\nu} + T_{G\mu\nu})$. In looking at it this way we remain close to the original interpretation of a common coordinate system. The 4-divergence of the right-hand side of the foregoing equation must vanish. So the sum of the 'red' and 'green' stress-energy tensors would be, in this sense conserved. Although the divergence of each, considered individually, might not be zero. Of course, we can easily extend this theory to encompass as many additional realities as we might like. If there were two extra realities we would need three $c(\mathbf{x}, t)$ s, and more if there were others. (This is true, also, for the Type-II theory.)

But this begs the obvious question why we do not see gravity from seemingly non-existent planets or light being bent by invisible stars. We would have to suppose that we are fortunate and there just aren't such stars and planets nearby us in the other reality. On the other hand, if $c(\mathbf{x}, t) = 0$ in almost all places and times, we might regard the gravitational contribution from this invisible other reality as a plausible candidate for dark matter. Now the amount of dark matter that seems to be present exceeds the obvious matter by about an order of magnitude. We could explain this by saying that the 'green' universe contained quite a bit of matter. We could, equally-well, suppose that there are something like five other universes, each similar to our own. The differently colored particles would share many of the attributes of WIMPS. The distribution of these types of matter would, presumably, depend on conditions existing at the initial singularity. Were the two or more types homogeneously mixed we could expect to find more of these other worlds around us. If the initial conditions were not homogeneous most of the other kind(s) of matter might be concentrated very far away (3).

Conclusions.

This theory is by no means unique in proposing the existence of other realities. It is, however, rather unusual in that it provides a mechanism whereby two realities could actually interact in such a manner that neither would see any fatal disruption to its own physics but might, on occasion, encounter intrusions from the other. (This might go some considerable way towards addressing the epistemological arguments that are often made against parallel realities.) The form such intrusions might take has been explored in the β -decay and positronium examples. Certainly, others could be imagined. An interesting feature that many such examples have in common is that, if observed, they could easily be written off as detector malfunctions; they would likely not be regarded otherwise unless they were being looked for. Now $c(\mathbf{x}, t)$ does not seem to get very large in very many places very often. But it could do so, here and there, occasionally, and go pretty-much unnoticed. And it has never been looked for at all.

References and Footnotes.

- 1) See, for instance, <https://en.wikipedia.org/wiki/Multiverse>.
- 2) Quigg, C. Gauge Theories of the Strong, Weak, and Electromagnetic Interactions, Benjamin/Cummings, 1983.
- 3) I might be asked whether we should regard this extra reality, and our own, as Everett branches derived from a common past. This might not seem an unreasonable possibility (assuming that Everett is right); both realities would share the same laws of physics and, automatically, a common coordinate system. And both realities would be quite similar – something we have suggested may be conducive to $c(\mathbf{x}, t)$ becoming large. But this is not plausible for a simple reason: Suppose we place the quantum mechanical measurement that

bifurcates these branches at some point in the common Minkowski coordinate system and draw a future-pointing light cone from it. The distinction between 'red' and 'green' worlds only occurs within this light cone. Outside, it would be a single 'monochrome' world. Suppose that a 'monochrome' particle were to move into the aforementioned light cone. What would happen? Would it turn 'red' or 'green'? If so, into which and why? If it stayed 'monochrome' how would it interact with the colored particles? There is nothing in our Lagrangian that tells us this. We could, instead, suppose that there were always two 'red' and 'green' realities with things outside the light cone being the same. But then we end up with the unacceptable situation where the charge of our electrons changes with $c(\mathbf{x}, t)$. It is also worth mentioning, in relation to the dark matter argument, that gravitational influences from Everett 'other worlds' have been looked for unsuccessfully (Page, D. N., Geilker, C. D. *Phys. Rev. Lett.* **47**, 979 (1981)).