# Best Practices in Math: Math Language and Fluency

(Grades K-2)





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Say hello.

Describe your role as an educator and the mathematics you support.



## Schedule for This Year

December 2022

Best Practices in Math:
Math Language and Fluency

Best Practices in Math:
Modeling and Practice
Word-Problem Solving

TBD

Best Practices in Math:
Use of Multiple Representations



### Instructional Platform

### INSTRUCTIONAL DELIVERY

Explicit instruction

Precise language

Multiple representations

### INSTRUCTIONAL STRATEGIES

Fluency building

Problem solving instruction



## Mathematical Language



## Instructional Platform

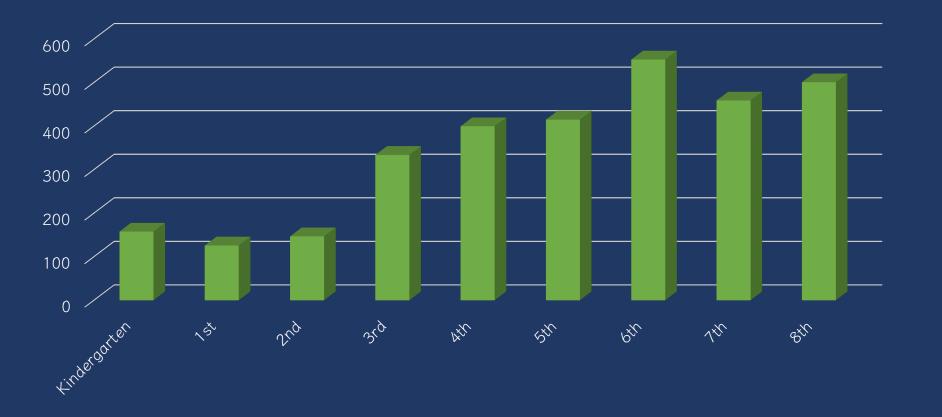
INSTRUCTIONAL DELIVERY

Explicit instruction

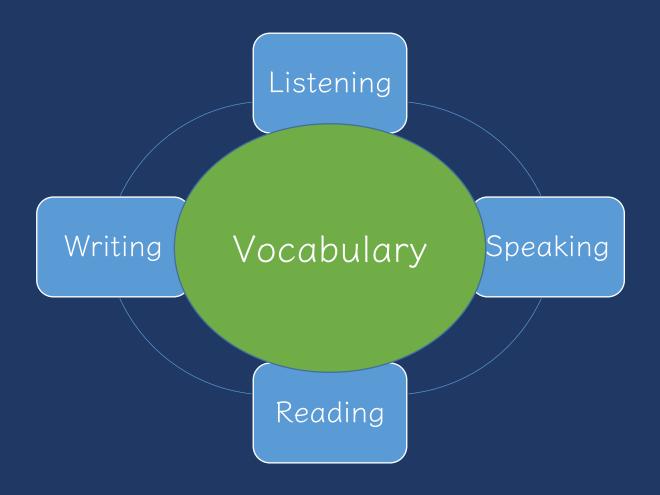
Precise language

INSTRUCTIONAL STRATEGIES

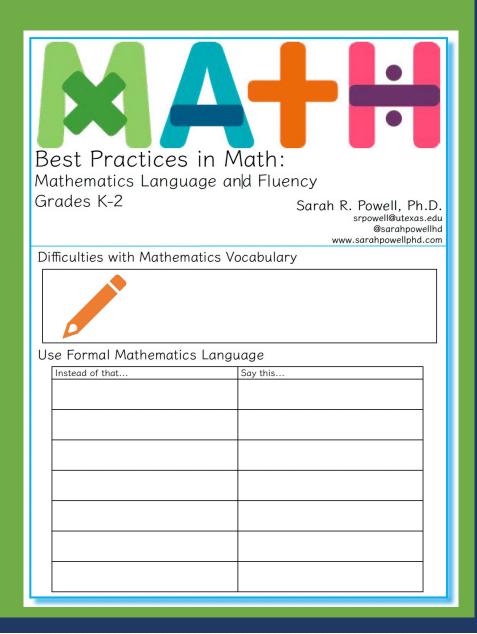














1. Some math terms are shared with English but have different meanings

right

degree



- 1. Some math terms are shared with English but have different meanings
- 2. Some math words are shared with English with similar meanings (but a more precise math meaning)

difference even



- 1. Some math terms are shared with English but have different meanings
- 2. Some math words are shared with English with similar meanings (but a more precise math meaning)
- 3. Some math terms are only used in math

trapezoid

numerator

parallelogram



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round
square
second
base



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- 4. Some math terms have more than one meaning
- 5. Some math terms are similar to other content-area terms with different meanings

divide vs. Continental Divide variable vs. variably cloudy



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- 6. Some math terms are homographs

eight vs. ate

sum vs. some

rows vs. rose

base vs. bass



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- 7. Some math terms are related but have distinct meanings

factor vs. multiple

hundreds vs. hundredths

numerators vs. denominator



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- 7. Some math terms are related but have distinct meanings
- 8. An English math term may translate into another language with different meanings

mesa vs. tabla



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- 8. An English math term may translate into another language with different meanings
- 9. English spelling and usage may have irregularities

four vs. forty



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- 8. An English math term may translate into another language with different meanings
- 9. English spelling and usage may have irregularities
- 10. Some math concepts are verbalized in more than one way

skip count vs. multiples

one-fourth vs. one quarter



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- 8. An English math term may translate into another language with different meanings
- 9. English spelling and usage may have irregularities
- 10. Some math concepts are verbalized in more than one way
- 11. Informal terms may be used for formal math terms

rhombus vs. diamond

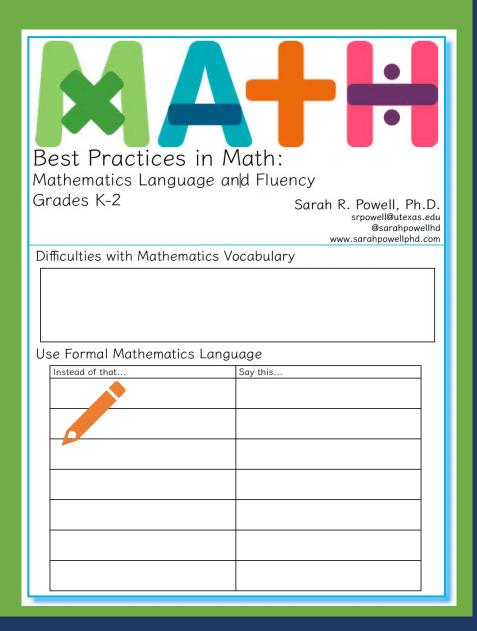
vertex vs.





What are the ways you see your students experience difficulty with the vocabulary of math?







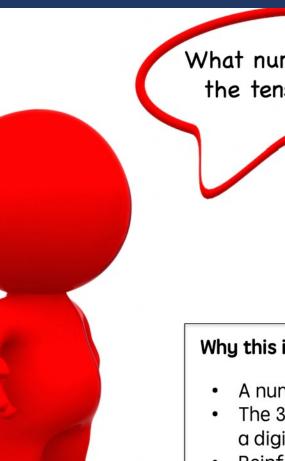
Use formal math language

Use terms precisely









What number is in the tens place?

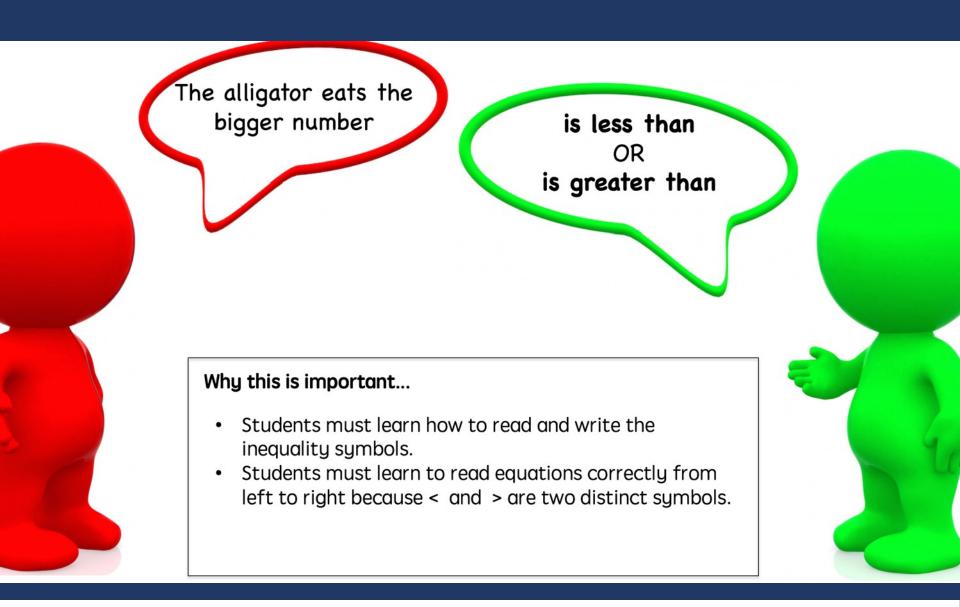
What digit is in the tens place?
What is the value of the digit in the tens place?

135

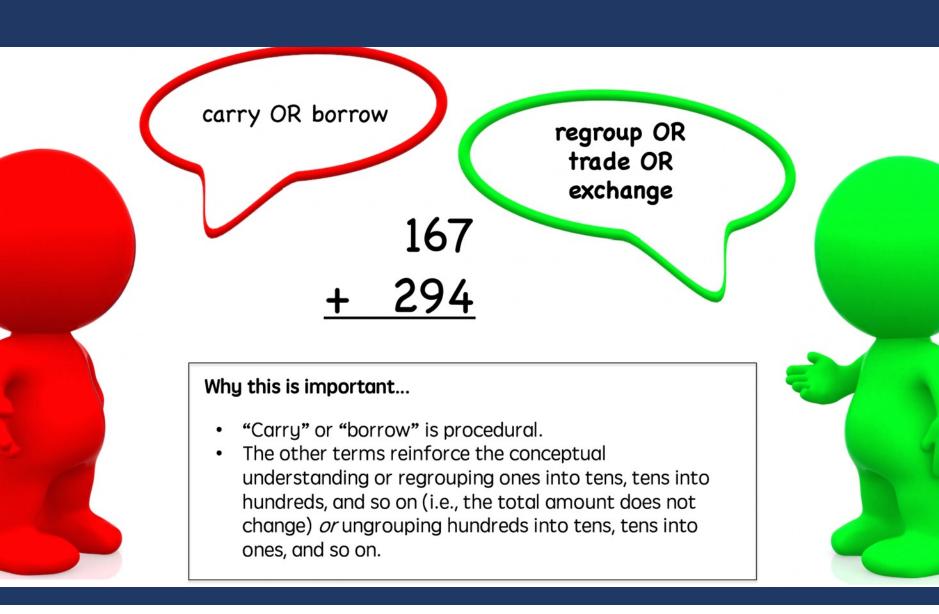
#### Why this is important...

- A number refers to the entire amount.
- The 3 in the tens place value is not a number, but rather a digit in the number 135.
- Reinforces conceptual understanding of place value.
- Emphasizes that 3 is part of the number 135 with a value of 30.

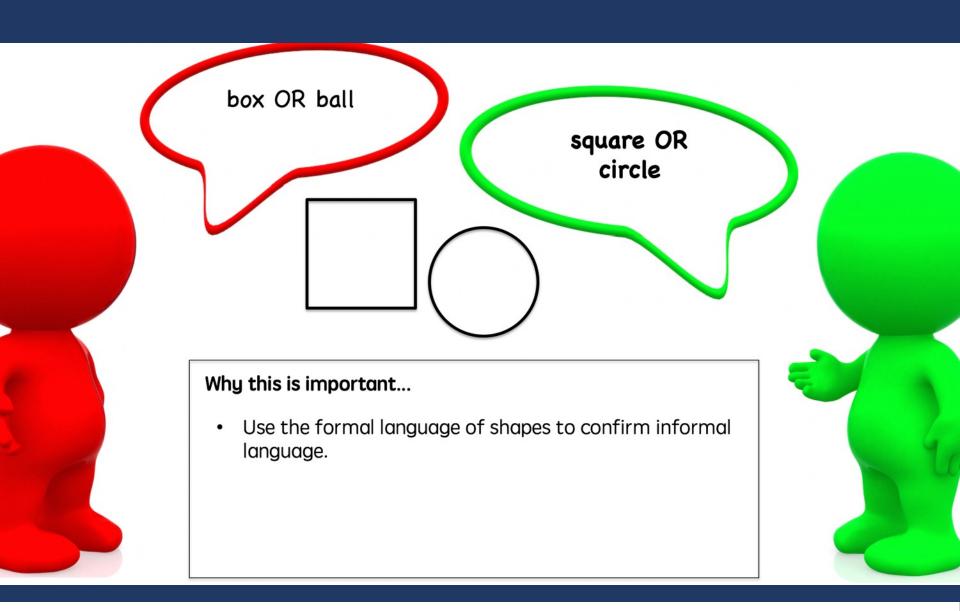




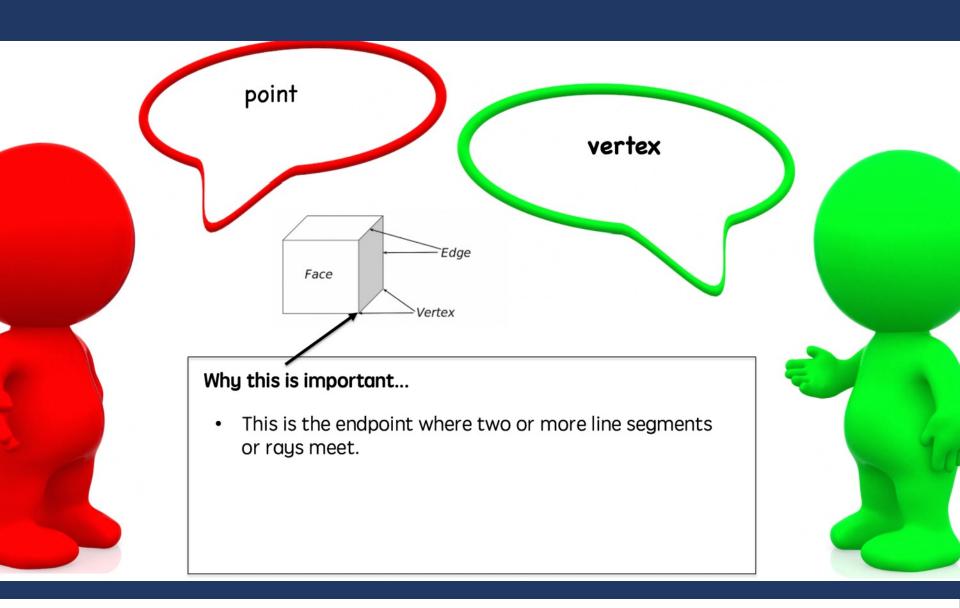




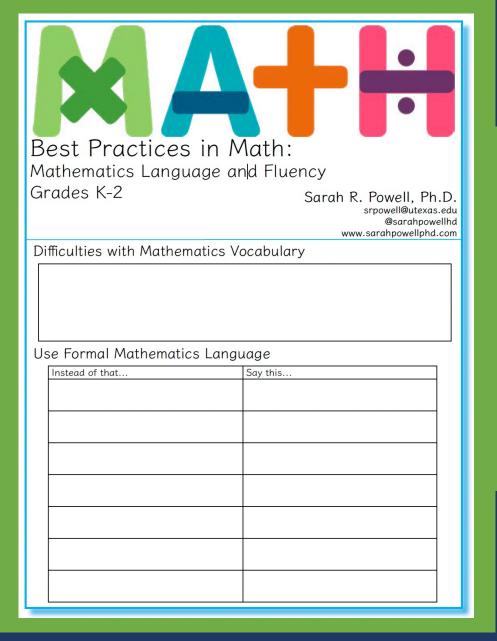














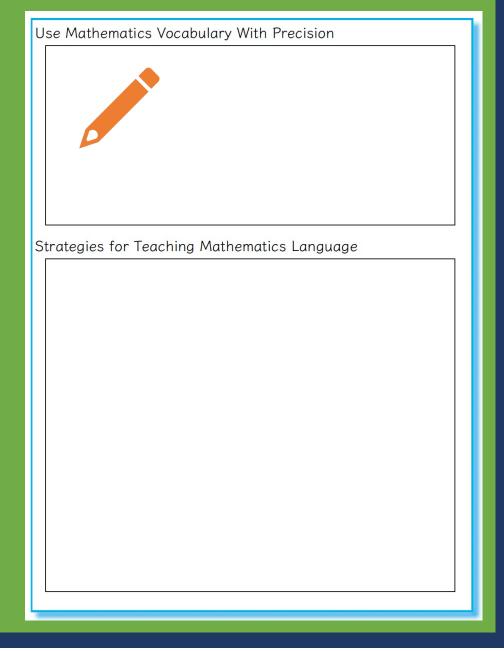
Identify examples of "Instead of \_\_\_\_, say \_\_\_."



Use formal math language

Use terms precisely

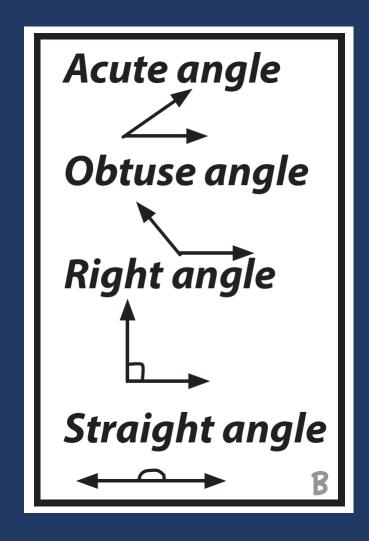






**Quadrilaterals** Rhombus Kite Parallelogram Square Rectangle **Trapezoid** 





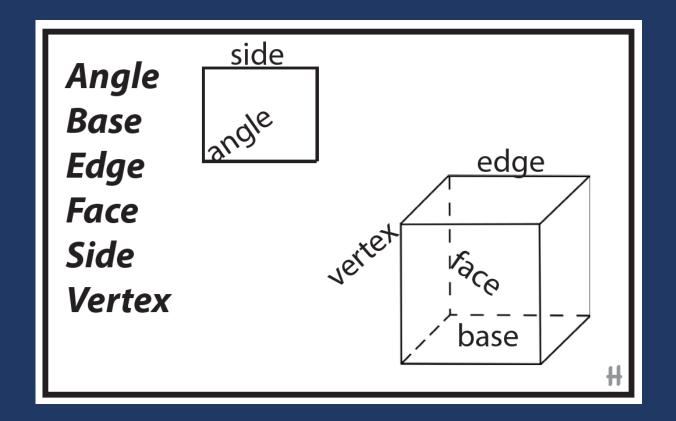


Acute triangle Equilateral triangle

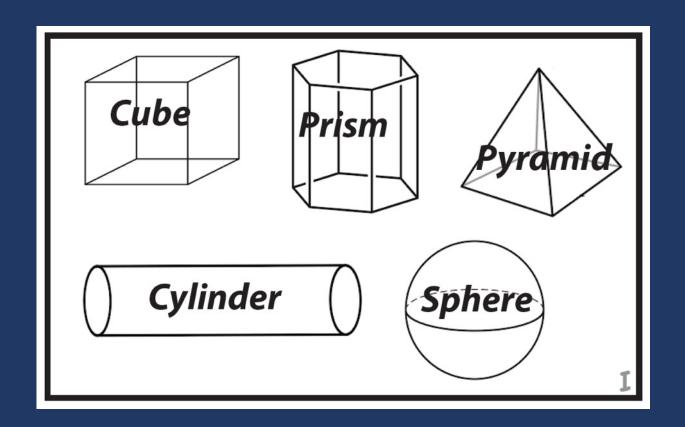
Obtuse triangle Isosceles triangle

Right triangle Scalene triangle











Use Mathematics Vocabulary With Precision							
Strategies for Teaching Mathematics Language							
Strategies for reaching Mathematics Language							



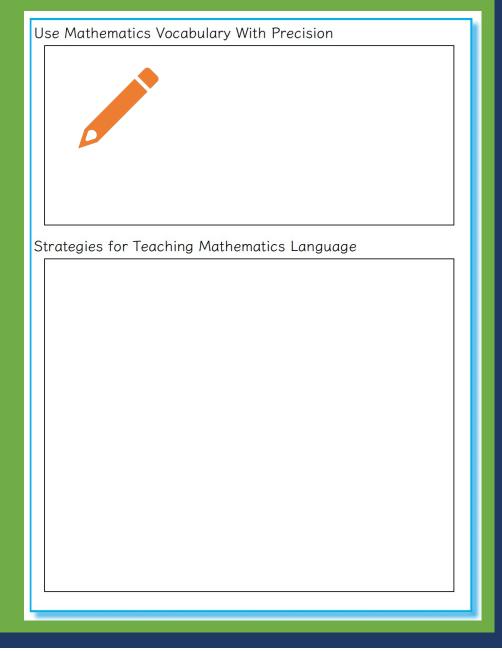
Discuss terms you want your students to use with precision.



Use formal math language

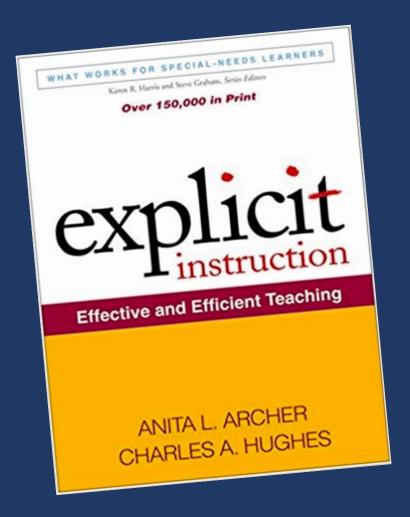
Use terms precisely

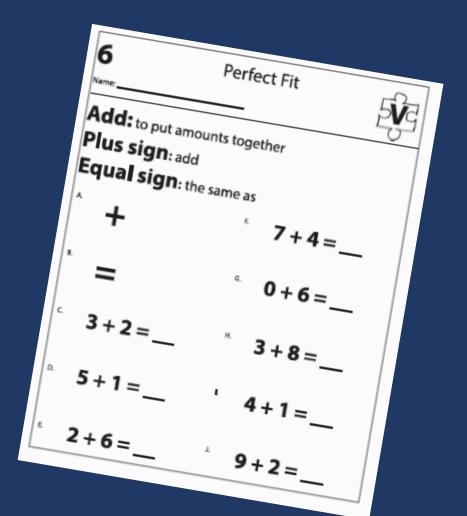






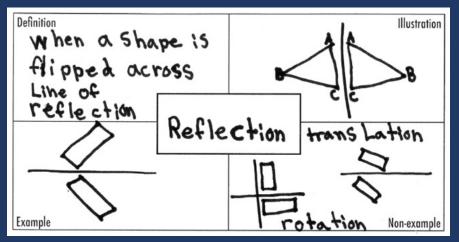
# 1. Use explicit instruction

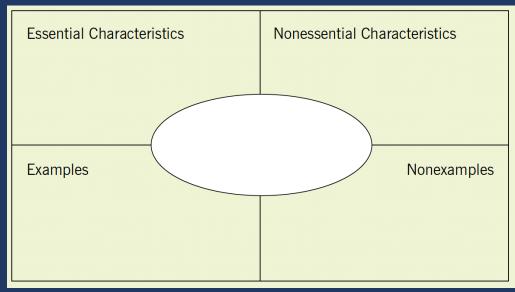






# 2. Use graphic organizers





Dunston & Tyminski (2013)



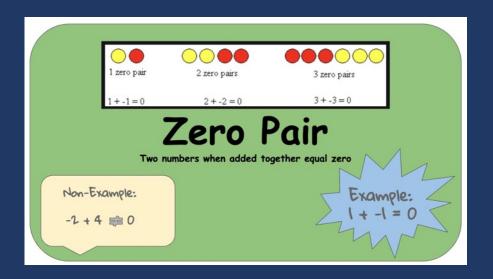
# 2. Use graphic organizers

Word	Lightbulb Word				
Definition	Picture				

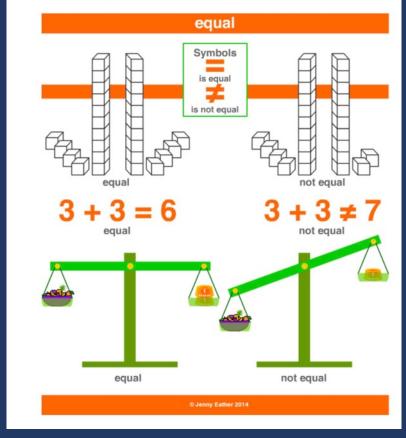
Dunston & Tyminski (2013)



# 3. Have students create vocabulary cards

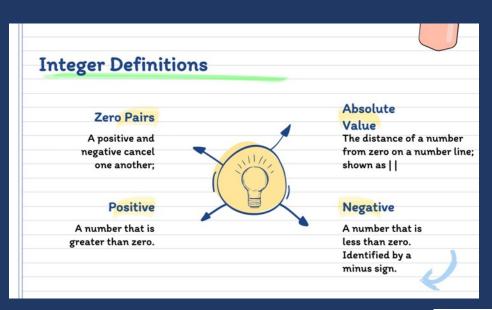


6. **Equal**: having the same amount or value.





# 4. Have students create glossaries



Numerator: how many parts of the whole



- Ex. <sup>10</sup>

Odd number: a number not divided evenly by 2

- Ex. 1, 3, 5, 7, 9....

Percent: a specific number in comparison to 100

- 74%

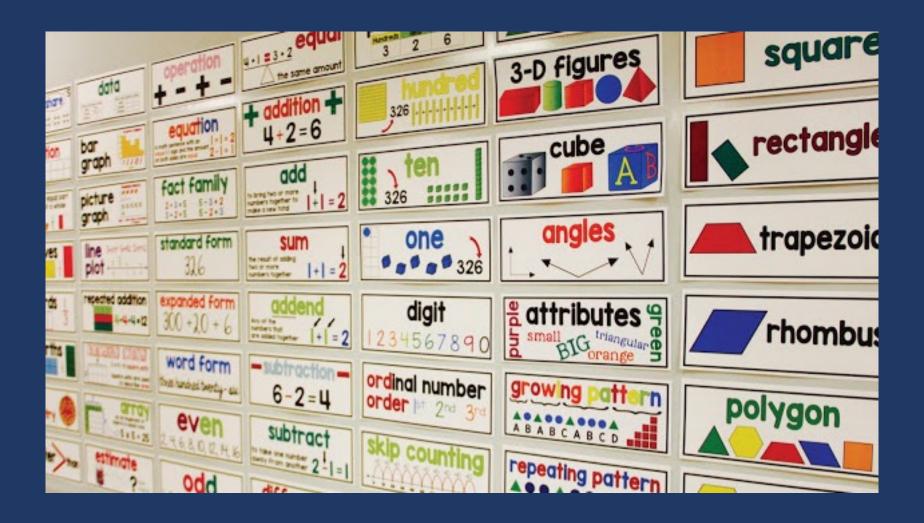
Polygon: any enclosed shape that is made up of 3 or more straight lines



- E>

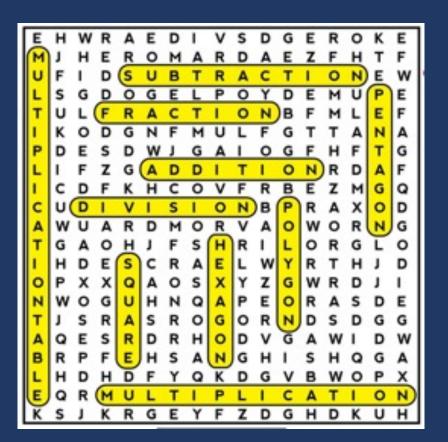


#### 5. Create a word wall

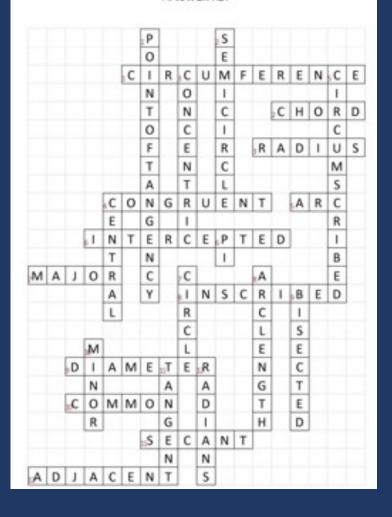




# 6. Do word games

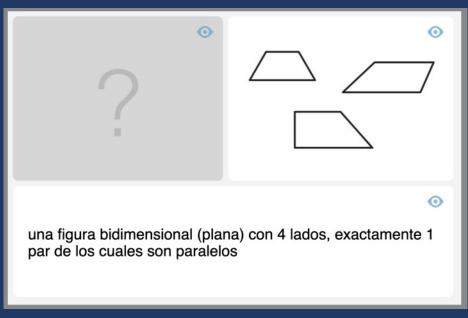


#### CIRCLES VOCABULARY CROSSWORD





# 7. Use technology



Math Learning Center



Math Lingo



Use Mathematics Vocabulary With Precision								
Strategies for Teaching Mathematics Language								

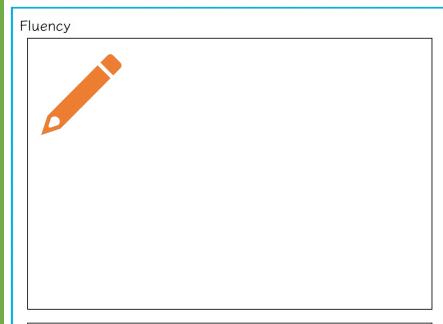


Discuss your strategy for focusing on mathematical language in your teaching.



# Fluency







What is your mathematical language goal for January?

What is your fluency goal for January?



# Instructional Platform

#### INSTRUCTIONAL DELIVERY

Explicit instruction

Precise language

Multiple representations

INSTRUCTIONAL STRATEGIES

Fluency building



# Building Fluency

Fluency is doing mathematics easily and accurately.

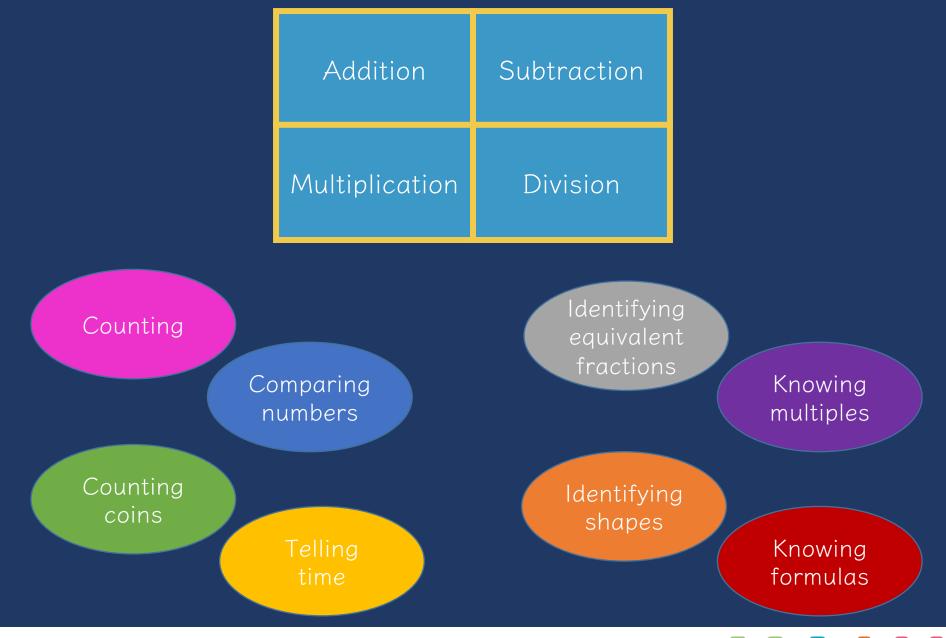
Fluency in mathematics makes mathematics easier.

Fluency provides less stress on working memory.

Fluency
helps
students
build
confidence
with
mathematics.

With fluency, it is important to emphasize both conceptual learning and procedural learning.







### 100 addition facts

Single-digit addends sum to a single- or double-digit number



Subtraction

### 100 subtraction facts

Subtrahend and difference are single-digit numbers and minuend is single- or double-digit number





# 100 multiplication facts

Multiplication of single-digit factors results in a single- or double-digit product

2 (factor)

 $\times 3$  (factor)

ó (<u>product</u>)



Division

## 90 division facts

Divisor and quotient are single-digit numbers and dividend is single- or double-digit number

$$8 \quad \div \quad 4 \quad = \quad 2$$

(dividend) (divisor) (quotient)



Addition	Subtraction				
Multiplication	Division				

Build fluency with math facts.

- Addition: single-digit addends
- Subtraction: single-digit subtrahend
- Multiplication: single-digit factors
- Division: single-digit divisor



					hlams
Cover, Copy	, Compare			Taped Pro	
9 × 6	8 × 6		6 × 5	8 × 6	7 × 9
54 7	48 6 × 5		9 × 8	8 × 5	7 × 8
× 8 56	3 6+3= 1+7=	File Folder	7 × 7	6 × 9	5 × 9
9 × 9 81	X 6+4= 7+3= 2+7=		1 9	6 × 9	9 × 5
6 × 7	5+6= 4+7=		× 4 9 11 6	8	4
8	7+8= 6+7=		× 7	<u>× 8</u>	× 8
× 8 64	7+9= 7+6= 8+7=	16	5		
	7 + 0 =	15 7			
	9+6= $6+0=$	15			
	6+8=	6 14			



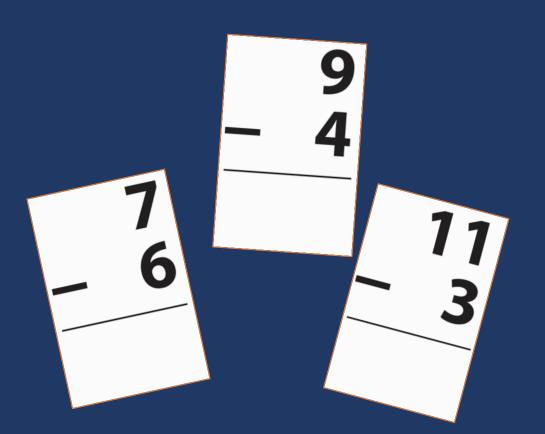
× 8

× 6

× 7

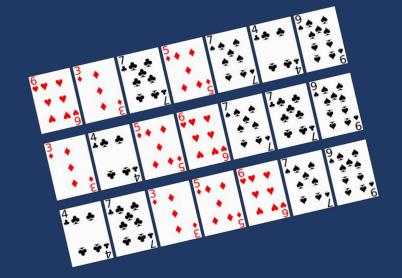
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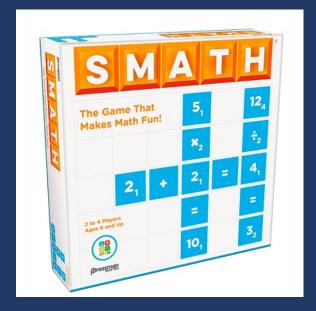
× 4



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Reflex

Get your free 30-day trial

Help your students attain math fact fluency success whether in-person, remote, or through hybrid learning

Game-based system to improve math fact fluency for grades 2-6 in less than 30 days!



DAILY and BRIEF



Addition Subtraction

Multiplication Division

Build fluency with whole-number computation



Addition Subtraction

Multiplication Division

Build fluency with rational-number computation

$$\frac{9}{4} - \frac{3}{8}$$

$$\frac{2}{3} \times \frac{3}{4}$$

$$7.892$$

$$\div 0.14$$



Addition Subtraction

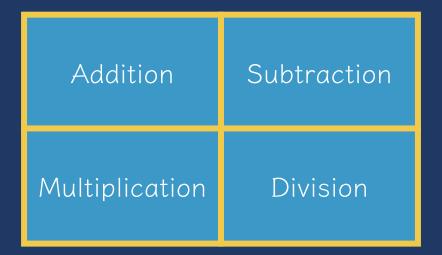
Multiplication Division

Build fluency with integer computation

$$-14 - (-7) =$$

$$-135 \div 2 =$$







What fluency practice do your students need?



# Instructional Platform

#### INSTRUCTIONAL DELIVERY

Explicit instruction

Precise language

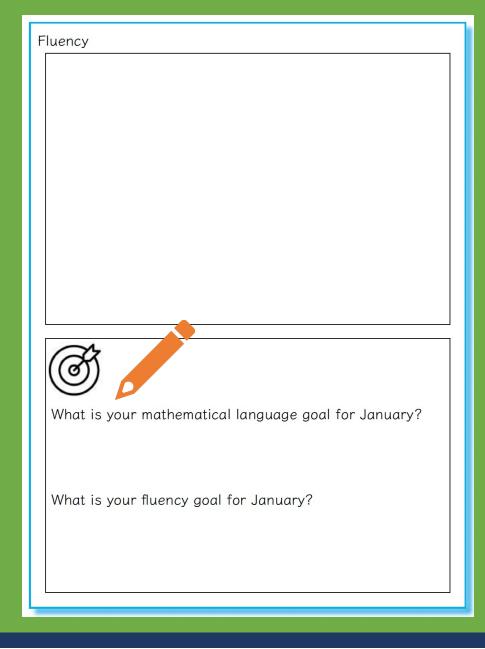
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