

Essential Components of Math Interventions and SDI



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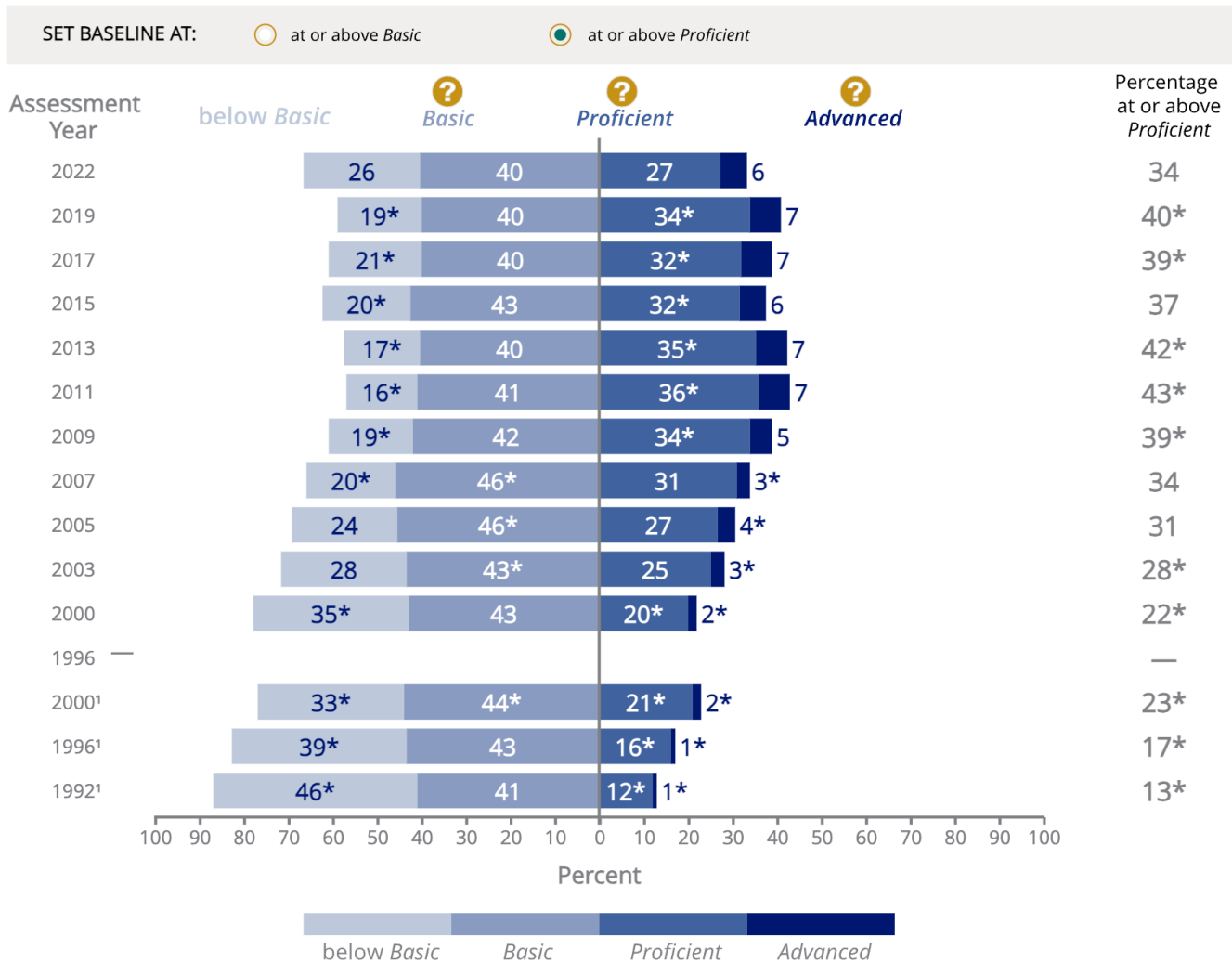
Describe your strengths in supporting mathematics.

Describe an opportunity for growth.



GRADE 4 | MATHEMATICS

Average scale scores, percentage, percentage, percentage, percentage and percentage for grade 4 mathematics, by All students jurisdiction: 1990, 1992, 1996, 2000, 2003, 2005, 2007, 2009, 2011, 2013, 2015, 2017, 2019, and 2022



Instructional Platform

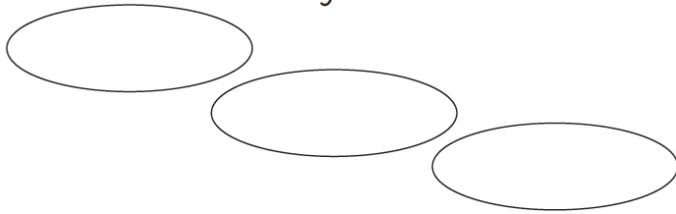


Essential Components of Math Interventions and SDI

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Instructional Platform

Instructional Delivery



Instructional Strategies



evidence-based practice

A practice that
has shown
consistent and
positive results



evidence-based practice



evidence-based intervention

An intervention
(i.e., packaged
program) that
has shown
consistent and
positive results



evidence-based practice



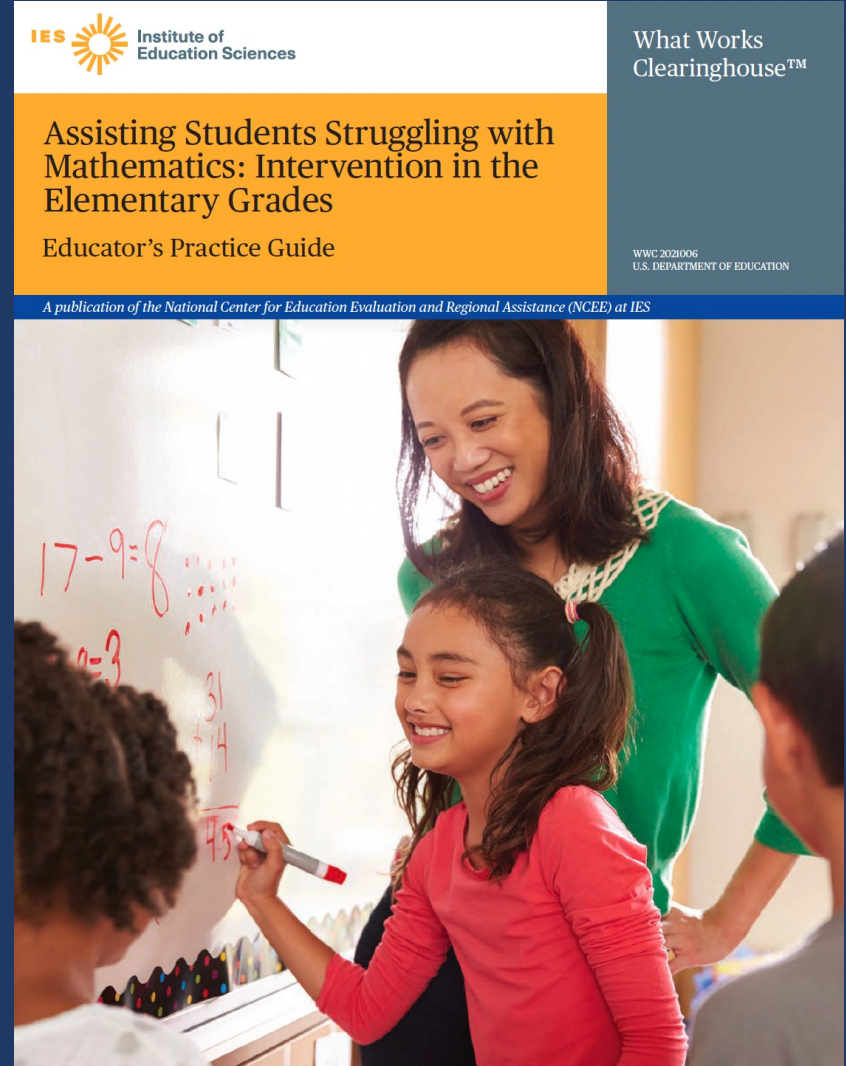
evidence-based intervention

evidence-based strategy

A method or strategy
that has shown
consistent and
positive results



What's the continuum of mathematics support?



Students require modeling and practice on how to use the language of mathematics.

Students should use hands-on tools, virtual manipulatives, drawings, and other visuals to understand mathematics concepts and procedures.

Teachers should use systematic and explicit instruction to help students develop a strong foundation for specific mathematics skills.

Teachers should use fluency building activities to build counting fluency and fluency with the operations.

Students should learn how to set up and solve word problems by combining an attack strategy with a focus on word-problem schemas.



Instructional Platform

INSTRUCTIONAL DELIVERY

Vocabulary

Representations

Model and
Practice

INSTRUCTIONAL STRATEGIES

Fluency

Word Problems



Vocabulary



Instructional Platform

INSTRUCTIONAL DELIVERY

Vocabulary

INSTRUCTIONAL STRATEGIES



VOCABULARY

Research and Information

Use Formal Mathematics Language

Instead of that...	Say this...





Significant correlation ($r = .49$) between mathematics vocabulary and mathematics performance. Mathematics vocabulary appears most important for word-problem performance ($r = .58$).

(Lin et al., 2021)

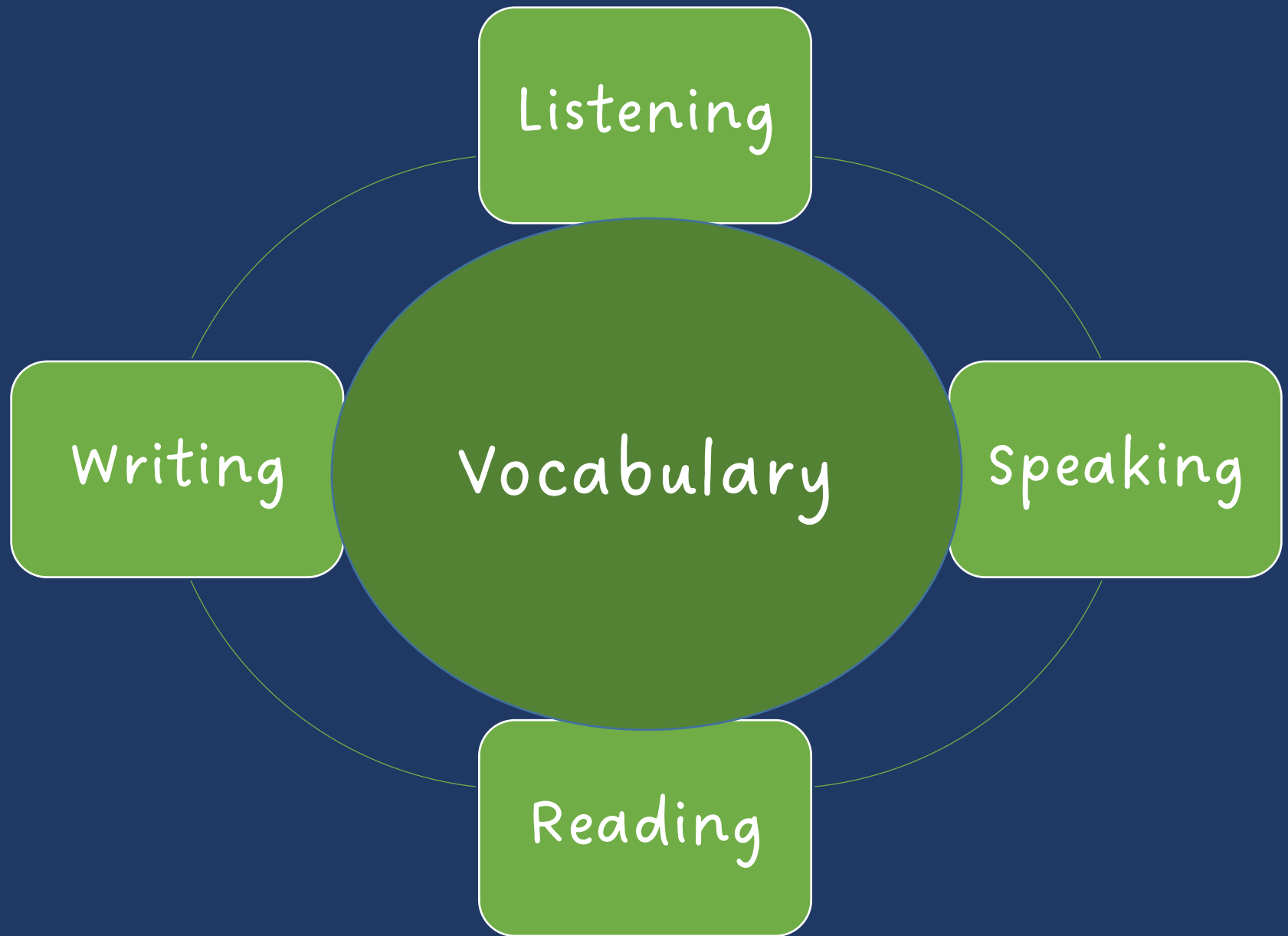
Early mathematics vocabulary related to mathematics and literacy.

(Hornburg et al., 2018; Purpura et al., 2017)

Students who experience difficulty with mathematics demonstrate lower mathematics vocabulary performance.

(Hughes et al., 2020; Powell & Nelson, 2017; Powell et al., 2017; Unal et al., 2021)







Use formal math language

Use terms precisely





What number is in the tens place?




What digit is in the tens place?
What is the value of the digit in the tens place?

135


Why this is important...

- A number refers to the entire amount.
- The 3 in the tens place value is not a number, but rather a digit in the number 135.
- Reinforces conceptual understanding of place value.
- Emphasizes that 3 is part of the number 135 with a value of 30.





The alligator eats the
bigger number



is less than
OR
is greater than

Why this is important...

- Students must learn how to read and write the inequality symbols.
- Students must learn to read equations correctly from left to right because $<$ and $>$ are two distinct symbols.





carry OR borrow

regroup OR
trade OR
exchange





$$\begin{array}{r} 167 \\ + 294 \\ \hline \end{array}$$

Why this is important...

- “Carry” or “borrow” is procedural.
- The other terms reinforce the conceptual understanding or regrouping ones into tens, tens into hundreds, and so on (i.e., the total amount does not change) *or* ungrouping hundreds into tens, tens into ones, and so on.





top number and
bottom number



numerator and
denominator


Why this is important...

- Identifying that there are two separate (whole) numbers suggests that whole number properties can be applied to fractions.
- Emphasizing that a fraction is ONE number with ONE magnitude on a number line that is communicated with a numerator and denominator is important.





reduce the fraction




rename OR
find equivalent OR
simplify


Why this is important...

- Reducing suggests that the quantity or magnitude of the new number will be less than the original number.





Four point seven
Four point oh seven



Four and seven tenths
Four and seven hundredths

4.7
4.07

Why this is important...

- Accurately shares the magnitude of the decimal.
- Emphasizes place value.

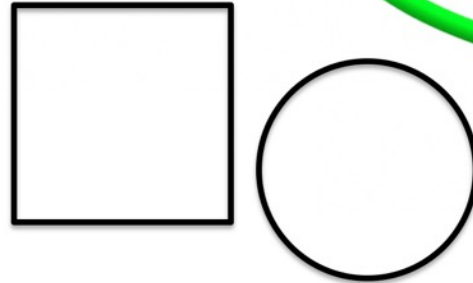




box OR ball



square OR
circle



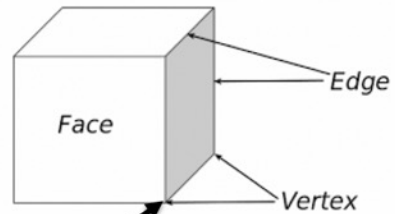
Why this is important...

- Use the formal language of shapes to confirm informal language.



point

vertex



Why this is important...

- This is the endpoint where two or more line segments or rays meet.

VOCABULARY

Research and Information

Use Formal Mathematics Language

Instead of that...	Say this...



Identify examples of
"Instead of _____, say _____."



Use formal math language

Use terms precisely



VOCABULARY

Use Terms With Precision

Strategies for Teaching Mathematics Language



What are your strengths?



What are your opportunities for growth?



What are your plans for next Monday?

Next month?

Next year?



Factor

$$1 \times 8 = 8$$

$$2 \times 4 = 8$$

factor

factor

Multiple

$$8 \times 1 = 8$$

$$8 \times 2 = 16$$

multiples of 8

E



Improper fraction

$$\frac{8}{5}$$

Mixed number

$$1\frac{3}{5}$$

Proper fraction

$$\frac{2}{9}$$

Proportion

$$\frac{2}{5} = \frac{8}{20}$$

Ratio

$$4:3$$

Unit fraction

$$\frac{1}{6}$$

D



Equation $9x - 4 = 7x$

Expression $9x - 4$

Formula $a^2 + b^2 = c^2$

Function $f(x)$

Inequality $9x - 4 > 6x$

c



Quadrilaterals

Kite



Rhombus



Parallelogram



Square



Rectangle

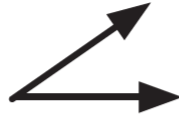


Trapezoid

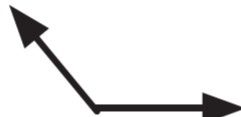


A

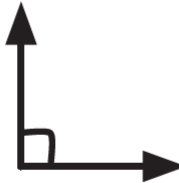
Acute angle



Obtuse angle



Right angle



Straight angle



B

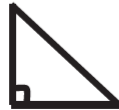
Acute triangle



Obtuse triangle



Right triangle



Equilateral triangle



Isosceles triangle

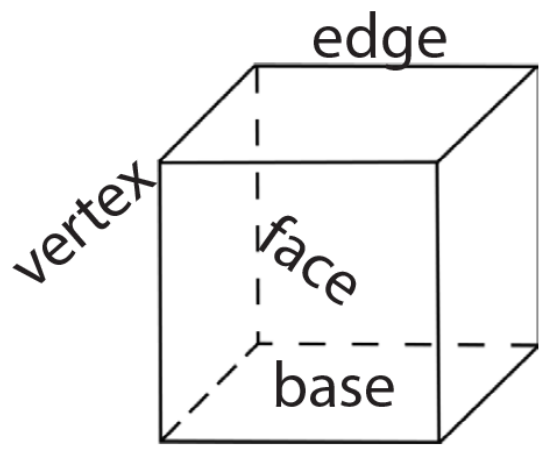
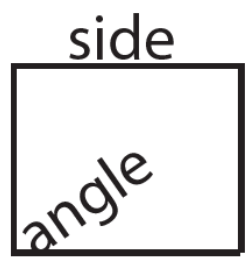


Scalene triangle



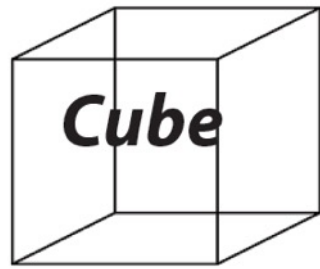
C

Angle
Base
Edge
Face
Side
Vertex



#





I

VOCABULARY

Use Terms With Precision

Strategies for Teaching Mathematics Language



What are your strengths?



What are your opportunities for growth?



What are your plans for next Monday?
Next month?
Next year?

MATH



Discuss terms you want students to use with precision.

MATH

Use formal math language

Use terms precisely



VOCABULARY

Use Terms With Precision

Strategies for Teaching Mathematics Language



What are your strengths?



What are your opportunities for growth?



What are your plans for next Monday?



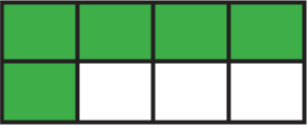

Next month?

Next year?

MATH

MATH

Use semantic maps

Term	Definition	Example	Nonexample
integer	(... -3, -2, -1, 0, 1, 2, 3...)	15	$\frac{1}{3}$
denominator	The equal parts of a whole or set.	$\frac{5}{8}$ <p>8 is the denominator</p> 	$\frac{5}{8}$ 
numerator	The equal parts of a given fraction.	$\frac{5}{8}$ <p>5 is the numerator</p> 	$\frac{5}{8}$ 

(Stevens et al., 2022)



Use word walls

difference

The result of subtracting or the result when comparing two numbers.

$$5 - 4 = 1$$

1 is the **difference**

horizontal line

A straight line that goes from left to right or right to left.



equivalent

Two numbers that have the same value.

$$\frac{2}{4} \text{ is equivalent to } \frac{1}{2}$$

total

The result or sum when adding numbers.

$$5 + 7 = 12$$

(mathspiral.com)



Use flash cards

addend

quotient

divisor

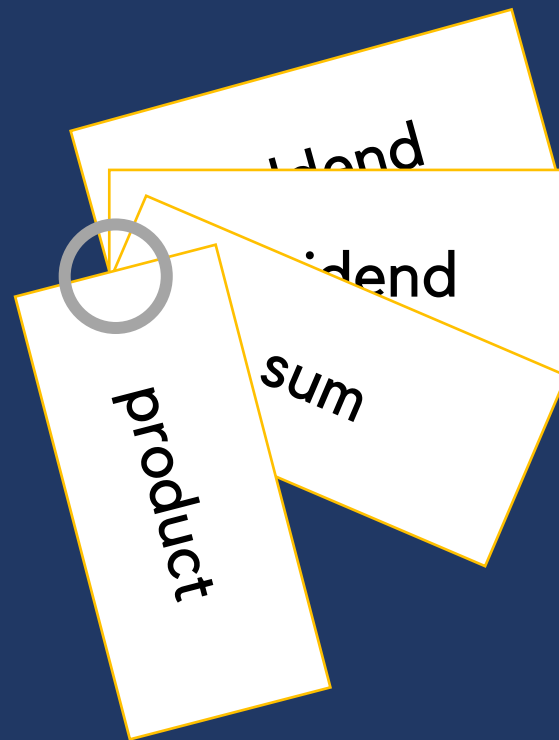
dividend

factor

sum

product

difference

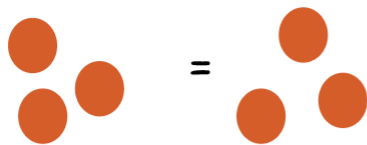


(Petersen-Brown et al., 2019)



Use glossaries

equal - with the same value

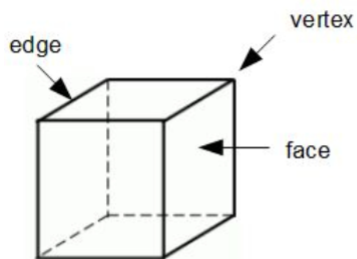


E

equation - expressions with an equal sign

$$5 = 2 + 3$$

edge - line segment between faces



Glosario de Matemáticas

Término	Definición
adición (<i>add</i>)	Juntar o agregar.
algoritmo (<i>algorithm</i>)	Es una serie de pasos organizados que describe el proceso que se debe seguir, para dar solución a un problema específico.
alinear (<i>array</i>)	Un conjunto de objetos, imágenes o números alineados en columnas y filas.
ancho (<i>width</i>)	La medida de un lado de un objeto, generalmente el lado más corto.
ángulo (<i>angle</i>)	Dos semirrectas o segmentos de línea recta que comparten un punto final.
ángulo agudo (<i>acute angle</i>)	Un ángulo que mide menos de 90°.
ángulo obtuso (<i>obtuse angle</i>)	Un ángulo que mide entre 90° y 180°.
ángulo recto (<i>right angle</i>)	Un ángulo que mide exactamente 90°.
área (<i>area</i>)	La cantidad de unidades cuadradas que cubre una figura geométrica cerrada.
balance presupuestario (<i>balance the budget</i>)	Un presupuesto es cuando la cantidad total de dinero gastado, ahorrado y compartido es igual al ingreso total.
báscula (<i>balance scale</i>)	Instrumento de medición que se utiliza para medir el peso o la carga.
base (computación) (<i>base (computation)</i>)	Un número que se multiplica por un exponente.
base (geometría) (<i>base (geometry)</i>)	La forma inferior de una figura tridimensional.

 **SPIRAL**
Specialized Math Intervention to Reach All Learners

(mathspiral.com)



Use anchor charts

Addition Computation

1

17 ← addend

+ 59 ← addend

76 ← sum

Quadrilaterals

Kite



Rhombus



Parallelogram



Square



Rectangle



Trapezoid

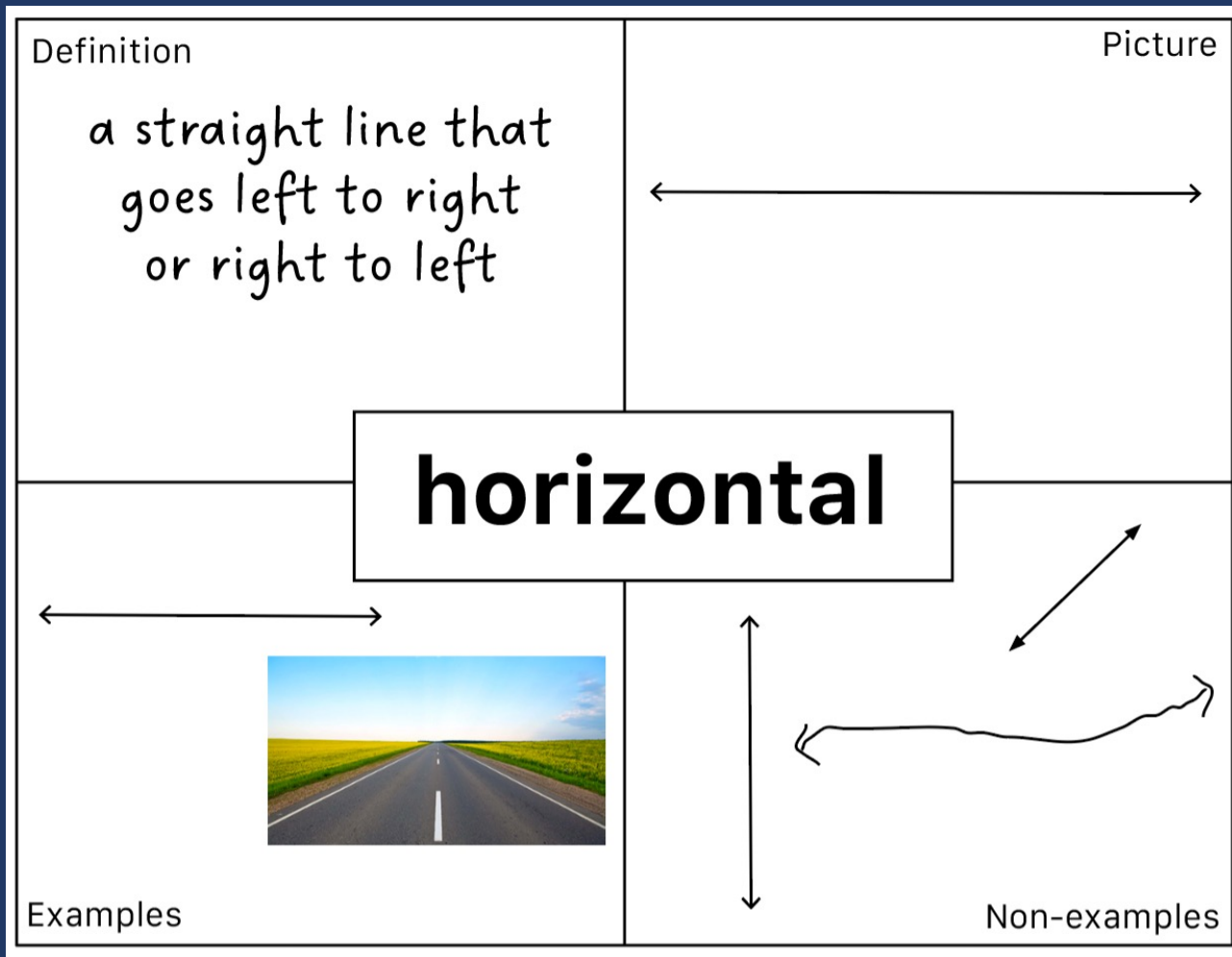


Use discussion



add
change
compare
decrease
difference
increase
part
put together
subtract
total

Use graphic organizers



Use technology

The screenshot shows the Flocabulary website interface. At the top left is the Flocabulary logo with the tagline "BY NEARPOD". To the right of the logo are navigation links: "Lessons", "Mixes", and "About", each with a dropdown arrow, followed by a search icon. On the far right of the navigation bar are three buttons: "Join a Class", "Log In", and "Free Trial". Below the navigation bar is a teal header with the word "Math" in white. The main content area features a grid of seven math topics, each with a representative image and a title:

- Addition & Subtraction**: Image showing a purple plus sign and an orange minus sign.
- Multiplication & Division**: Image showing a pink multiplication sign and a green division sign.
- Numbers & Operations**: Image showing a collage of various numbers in different colors and sizes.
- Expressions & Equations**: Image showing a yellow pencil resting on a notebook with mathematical equations.
- Geometry & Measurement**: Image showing various colorful geometric shapes like pyramids, prisms, and cylinders.
- Statistics & Probability**: Image showing three dice with numbers 1, 2, and 3.
- Ratios & Proportional Relationships**: Image showing a pie chart with a green section labeled "75%" and an orange section labeled "25%".



Use games

Name: _____ Date: _____

3RD GRADE MATH

T W D H P T R I Y T S F T O Y T S P X G U C I C
M S G C E N T I M E T E R S Y S C Y Z D R G D J
I M I E U J R L H F O A W Z X U A L F J O Q F T
U P F N Z L R V C N N P Z D D H L P H F A V J Z
Y R U P M I A C O R D P I V J T E I H Y M F M S
E K X H R T T Y U J E S V X S V A T Z W M S E T
W Z Z W G E Q G M P C V C Z E H E L W L T T A A
N U V V B R J F H Y N E O Z H T K U K F A Z S W
Q Y J P S H A C D X A M Y G C U K M Z L J E U P
T Z W B P N R Z Y F L I Y D N A J J Z M W D R S
O W W U W T G I T I A T F F I S Q G X K K I E Z
E W R Q C S U U C U B J L E Z P B H G B C V M Q
F R A C T I O N S K Z O W M D X B M M C O I E C
N Z C A T L I J B J M U F O X X A D O Y L D N K
D E V P T U C M Y S A H K Z S U O W R S C V T G
M X N L N S O L V E R R I Y I B Z N Q O X C P W
M V W Z C D Q Z Z U G X L U K P Y O B S W I M N
K F L J U R J G J R O Q E M X C U O H N M S F D
S U B T R A C T G U L Y Y A K W U N U S O L H H
E G F D D A I O I A I Y R R J I C A P A C I T Y
I L W B A T R D O X K C J G H T D X E G C S M Z
X J Q Y A H L T B J R A I W J B C K I U S S I U
N U O D N R L V T I T L C U P C L W C B F S Z Q
J F N P R R K P Y M R E L U R Q H M A E Y Y Z H

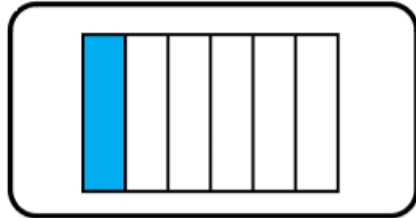
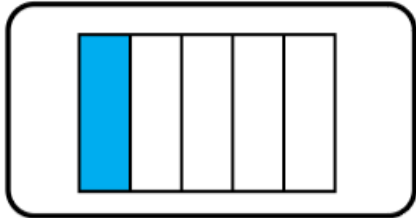
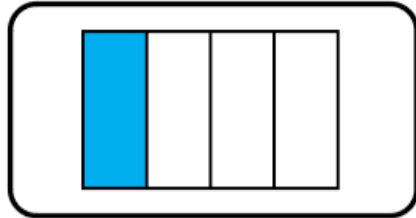
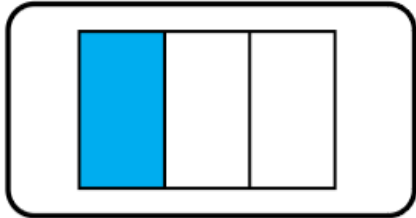
ADD	BALANCED	CAPACITY	CENTIMETERS
CLOCK	DIVIDE	FRACTIONS	GRAM
INCHES	KILO GRAM	LITER	MEASUREMENT
MULTIPLY	NOON	RULER	SCALE
SOLVE	SUBTRACT	TIME	

square	circle	decagon	triangular prism	cone
cylinder	cube	sphere	line	pyramid
parallelogram	octagon	FREE	trapezoid	oval
kite	pentagon	cylinder	rectangle	line segment
hexagon	rhombus	triangle	quadrilateral	rectangular prism

https://wordmint.com/public_puzzles/13055



Use games



one

one-half

one-third

one-fourth

one-fifth

one-sixth



Use math writing

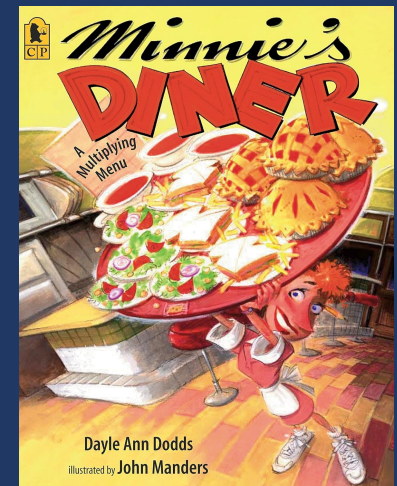
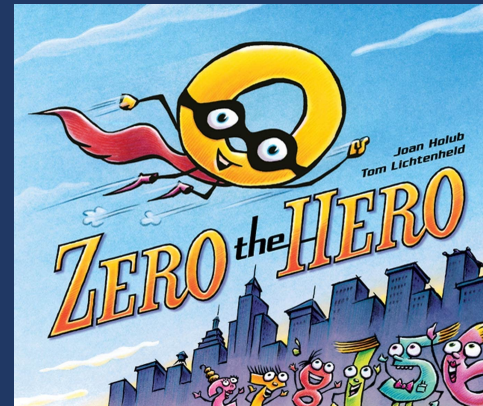
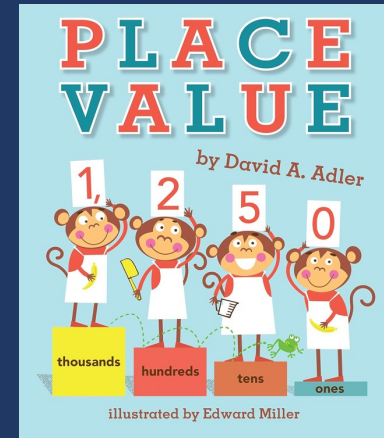
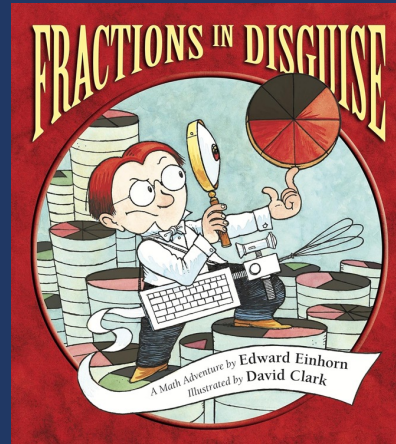
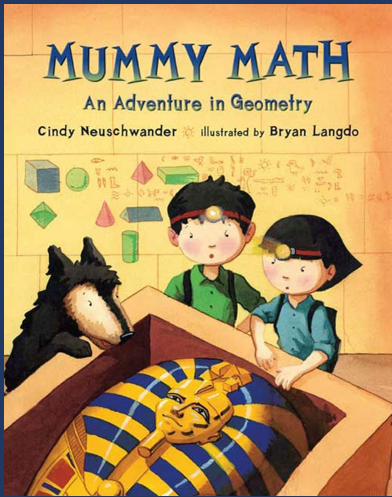
I would help Cole out by not putting them into thirds because he put 1 and $\frac{2}{3}$ but the answer should be $\frac{3}{5}$. So next I would draw the lines the make them into 5 pieces but put next to each other. Then you shade in 3 of the squares and keep the others alone. then that would be the correct way to do $\frac{3}{5}$.

What Alex did wrong was that it was that he has five rectangles but they are different sizes so first what I would do is draw 5 rectangles side by side then what you would do is shade 3 of them and that would equal $\frac{3}{5}$ so that would be the correct way to solve it.

I would help Bo out by he shaded three rectangles which is correct but he left 5 shaded and there should only be 2 dark rectangles so if you erase 3 rectangles then then answer would be $\frac{2}{5}$ and that is the correct way to solve it.



Use read-alouds



(Purpura et al., 2017)



Model and practice

- Teacher** Let's work on addition. Today, let's think about addition as combining. What does it mean to combine?
- Students** Put together.
- Teacher** When we combine, we put things together. When you cook, you put ingredients together. For example, to make macaroni and cheese, you combine what?
- Students** Macaroni noodles and cheese!
- Teacher** That's right. You combine macaroni and cheese! Now, let's think about combining numbers. Look at this problem.
(Show problem.)

(Powell & Driver, 2015; Stevens et al., 2022)



Make sure students use
mathematics vocabulary
as much as adults do!



VOCABULARY

Use Terms With Precision

Strategies for Teaching Mathematics Language



What are your strengths?



What are your opportunities for growth?

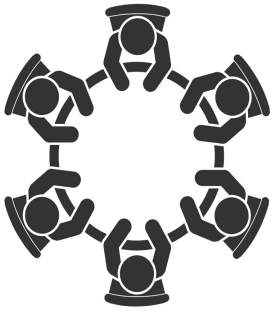


What are your plans for next Monday?

Next month?

Next year?





What are your strengths with vocabulary?

What are your opportunities for growth?

What are your plans for next Monday?

Next month?

Next year?



Representations



Instructional Platform

INSTRUCTIONAL DELIVERY

Vocabulary

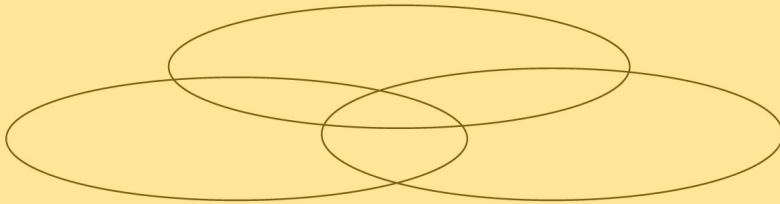
Representations

INSTRUCTIONAL STRATEGIES



REPRESENTATIONS

Research and Information



What are your strengths?



What are your opportunities for growth?



What are your plans for next Monday?
Next month?
Next year?

MATH

MATH



Hands-on manipulatives contribute to increases in mathematics performance.

(Bouck & Park, 2018; Carbonneau et al., 2013; Namkung & Bricko, 2021; Sherman & Bisanz, 2009; Strickland & Maccini, 2012)

Virtual manipulatives contribute to increases in mathematics performance.

(Bouck et al., 2020; Satsangi et al., 2016)

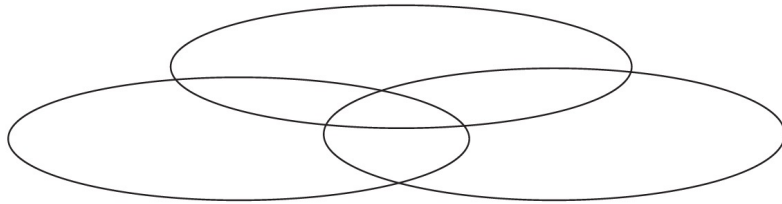
Other visuals (e.g., graphic organizers) contribute to increases in mathematics performance.

(Jitendra et al., 2009; Sharp & Dennis, 2017; van Garderen, 2007; Xin, 2008)



REPRESENTATIONS

Research and Information



What are your strengths?



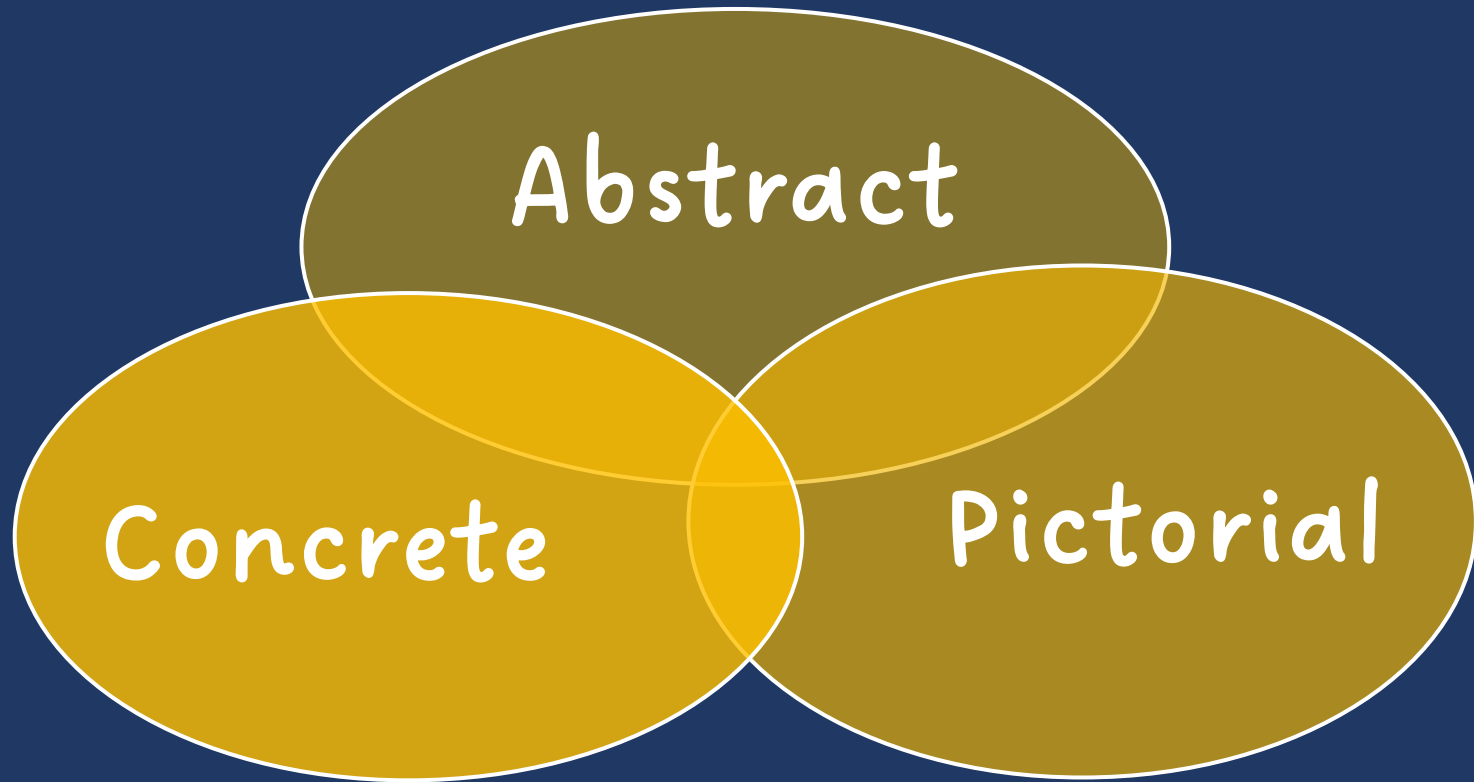
What are your opportunities for growth?

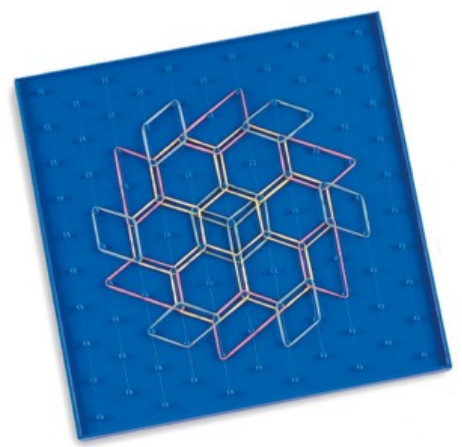
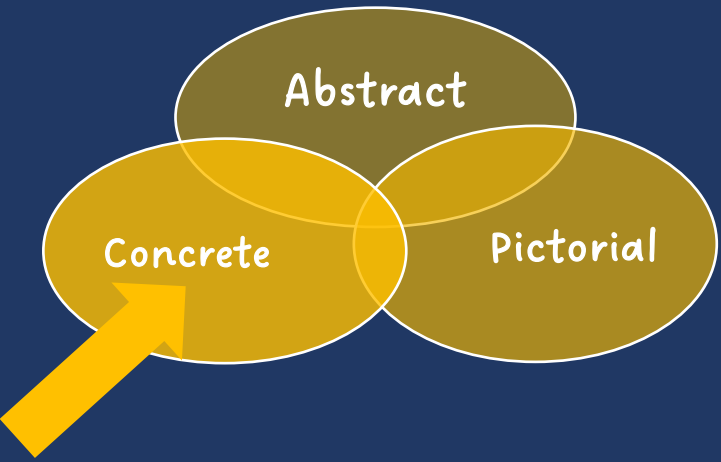


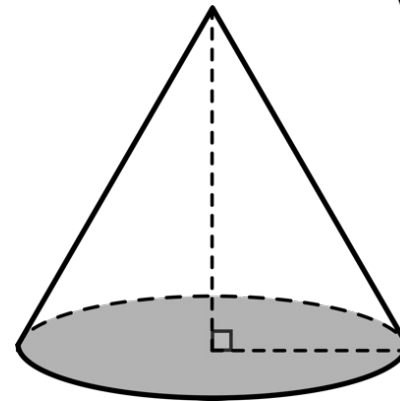
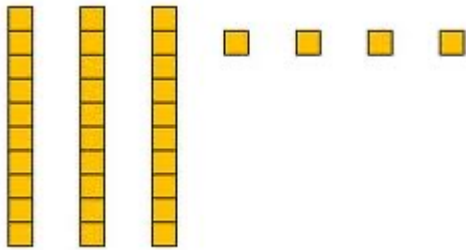
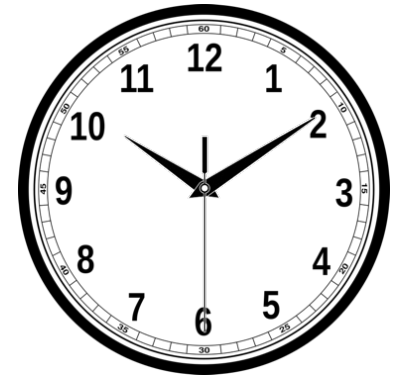
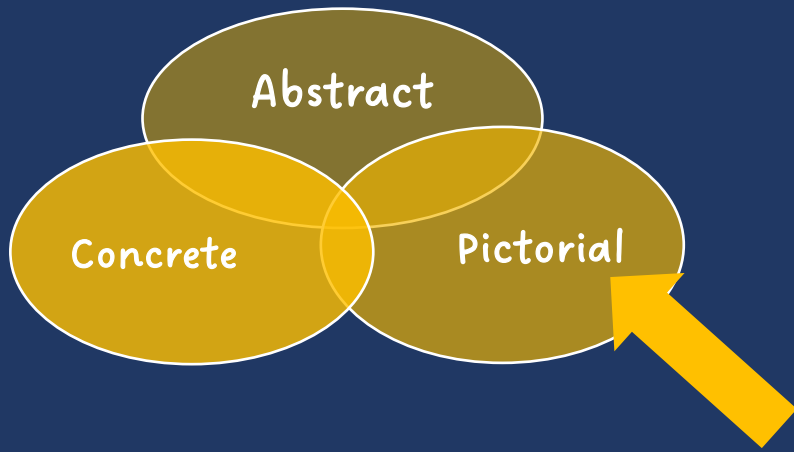
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Next month?
Next year?

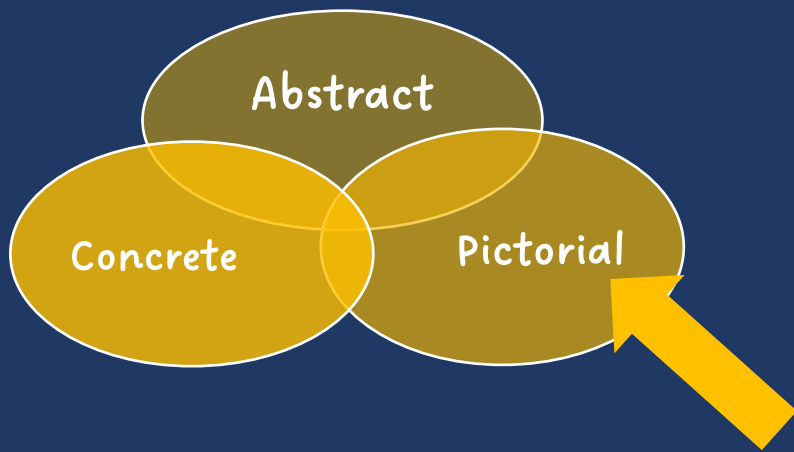
MATH

MATH







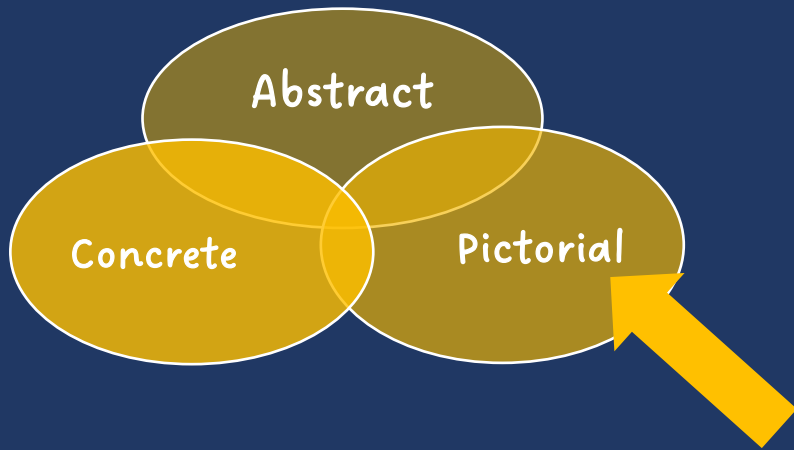


Modeling Fractions with Cuisenaire Rods

The interface for modeling fractions with Cuisenaire rods. On the left is a palette of rods: a white cube, a red rod (1 unit), a light green rod (2 units), a purple rod (3 units), a yellow rod (4 units), a dark green rod (5 units), a black rod (6 units), a brown rod (7 units), a blue rod (8 units), and an orange rod (9 units). In the center is a grid with a model of a brown rod (7 units) composed of seven red rods (1 unit each). On the right is a control panel with icons for 'View Hint' (lightbulb), 'Clear' (refresh), 'View Help' (question mark), and 'Trash Can' (trash bin).

A screenshot of a geometry software interface. The main workspace is a black dot grid. A triangle is drawn with vertices on the grid. The left vertical side is a yellow rod, the bottom horizontal side is a red rod, and the hypotenuse is a yellow rod. Below the grid is a toolbar with various geometric shapes and tools, including a trash can icon.



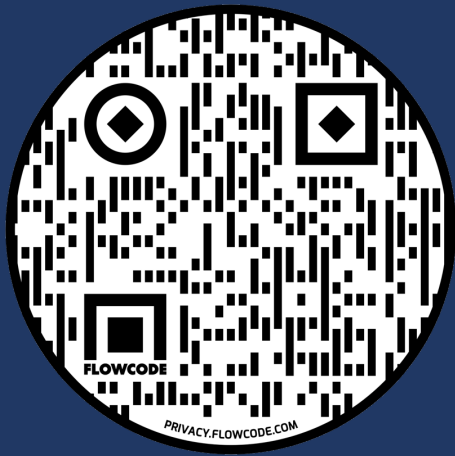


Virtual Manipulatives

Help students see and learn math using different tools!

Number & Operations	Place Value
Fractions & Decimals	Integers & Algebra
Geometry	Time & Money
Data & Probability	Extras

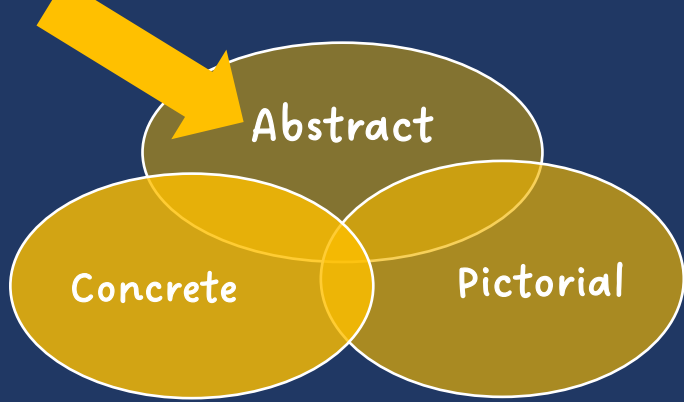
Sarah R. Powell, Ph.D.
srpowell@utexas.edu
www.sarahpowellphd.com
@sarahpowellphd



bit.ly/srpowell

Fractions & Decimals	fraction strips	fraction strips	fraction strips	Cuisenaire rods
	fraction circles	geoboard	geoboard	geoboard
	two-color counters	decimal strips	place value disks	percentage strips
				house icon





$$2 + 8 = 10$$

34 = 3 tens and 4 ones

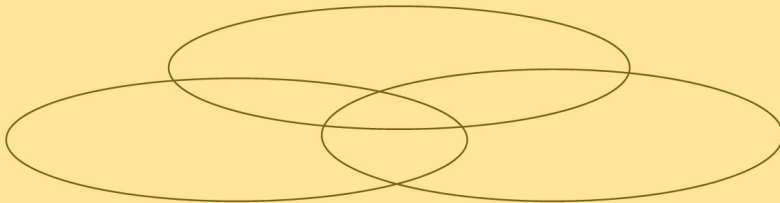
0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10

$$\begin{array}{r} 4,179 \\ + \quad 569 \\ \hline \end{array}$$



REPRESENTATIONS

Research and Information



What are your strengths?



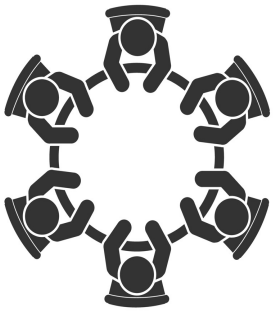
What are your opportunities for growth?



What are your plans for next Monday?
Next month?
Next year?

MATH

MATH



What are your strengths with multiple representations?

What are your opportunities for growth?

What are your plans for next Monday?

Next month?

Next year?



Model and Practice



Instructional Platform

INSTRUCTIONAL DELIVERY

Vocabulary

Representations

Model and
Practice

INSTRUCTIONAL STRATEGIES



MODEL AND PRACTICE

Research and Information

MODELING

PRACTICE

SUPPORTS





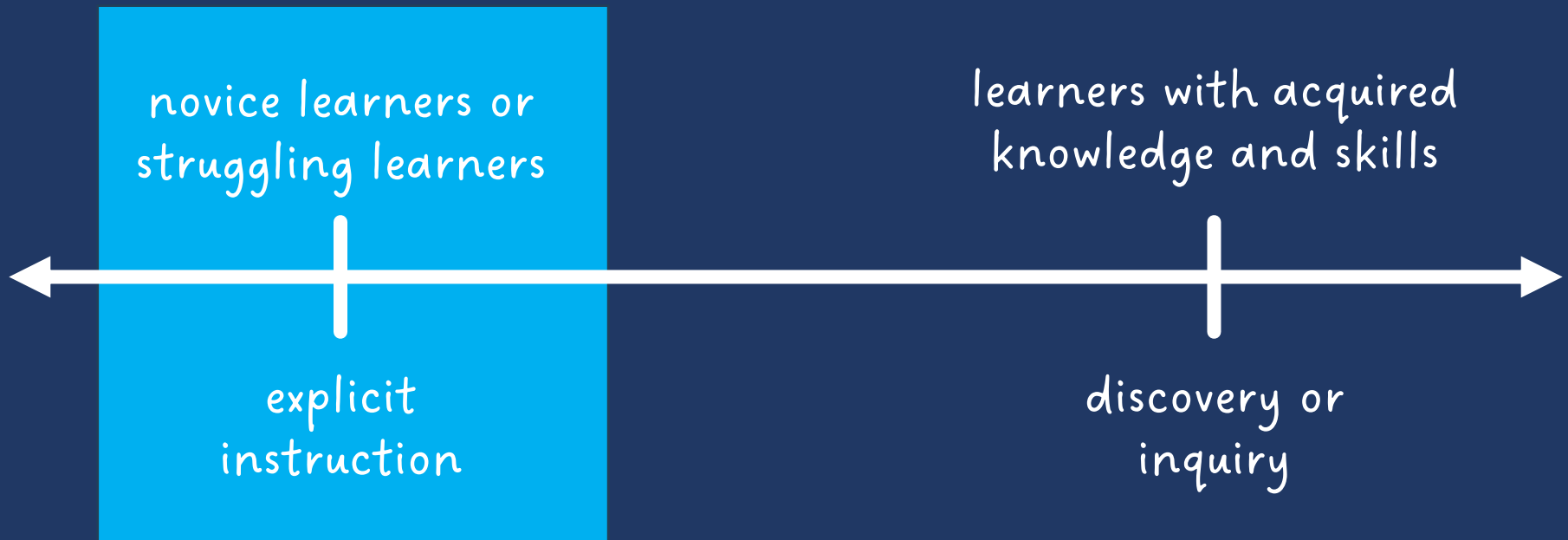
Over a half century of research supports explicit (i.e., direct, systematic) instruction.
(Stockard et al., 2018)

When compared to discovery approaches, explicit instruction demonstrates higher outcomes.
(Alfieri et al., 2011; Kroesbergen et al., 2004; Poncy et al., 2010)

Numerous meta-analyses and large-scale studies have identified explicit instruction as essential for the teaching and learning of mathematics.
(Chodura et al., 2015; Ennis & Losinski, 2019; Jitendra et al., 2018; Kong et al., 2021; Morgan et al., 2015; Nelson & McMaster, 2019; Powell et al., 2021).



What's the continuum of mathematics support?



Anita Archer (2019)



MODEL AND PRACTICE

Research and Information

MODELING

PRACTICE

SUPPORTS



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



Modeling is a dialogue between the teacher and students.

MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



Modeling includes a step-by-step explanation of how to do a math problem.

A teacher may do 1 modeled problem or several.

MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



Modeling
needs to
include
planned
examples.

MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback

These examples
should be
sequenced so
easier skills
lead to more
difficult skills.



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

Practice continues as a dialogue between the teacher and students.

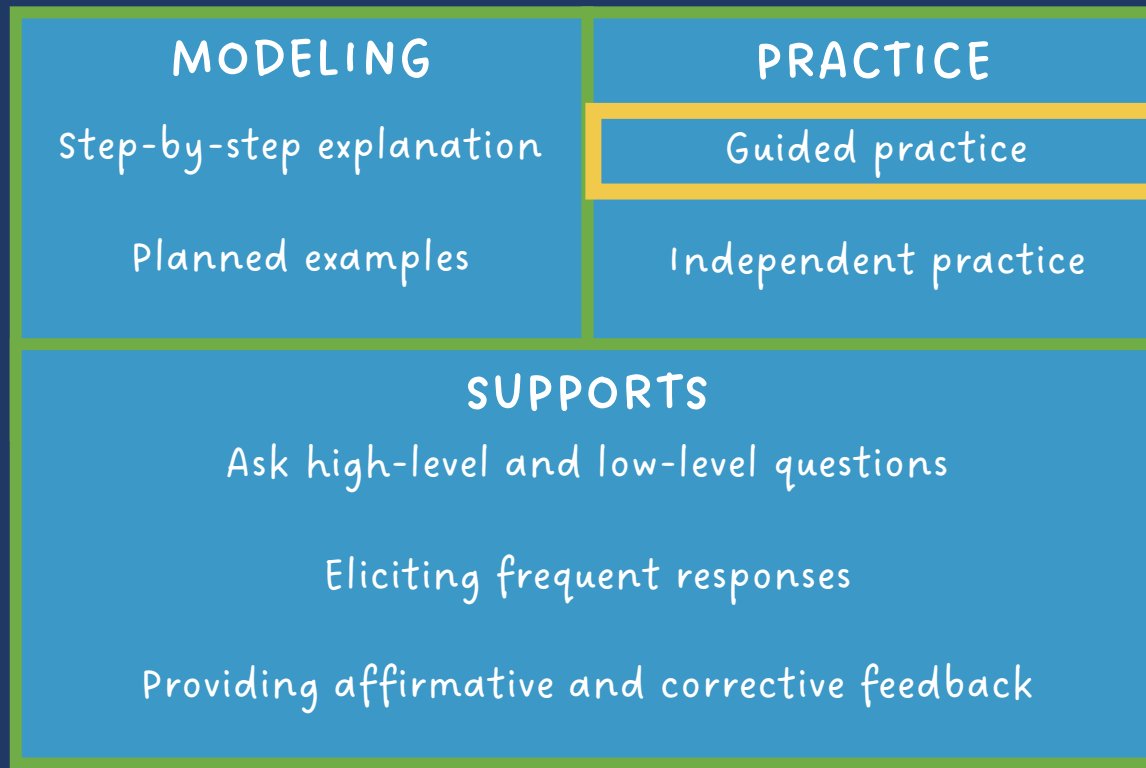
SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



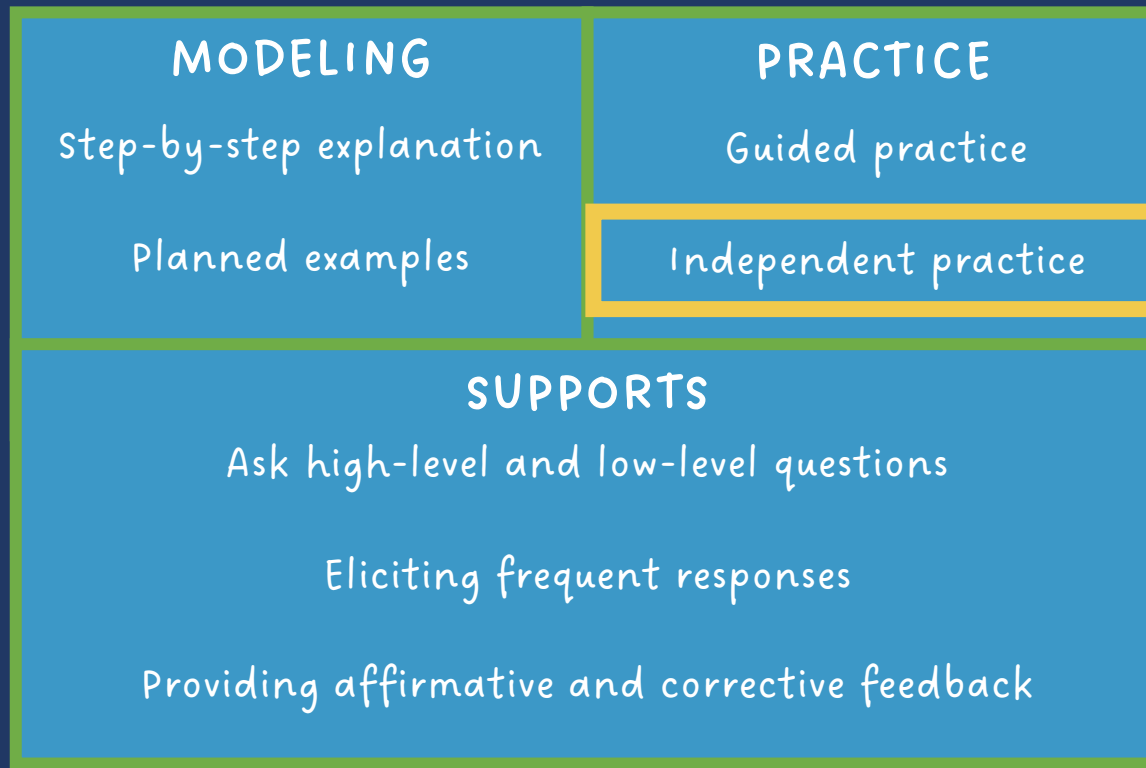


Guided practice is practice in which the teacher and students practice problems together.



“Let’s work on a problem together.”





Independent practice is practice in which the students practice independently with teacher support.



“Now, you’ll practice a problem on your own. Use your attack strategy!”



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

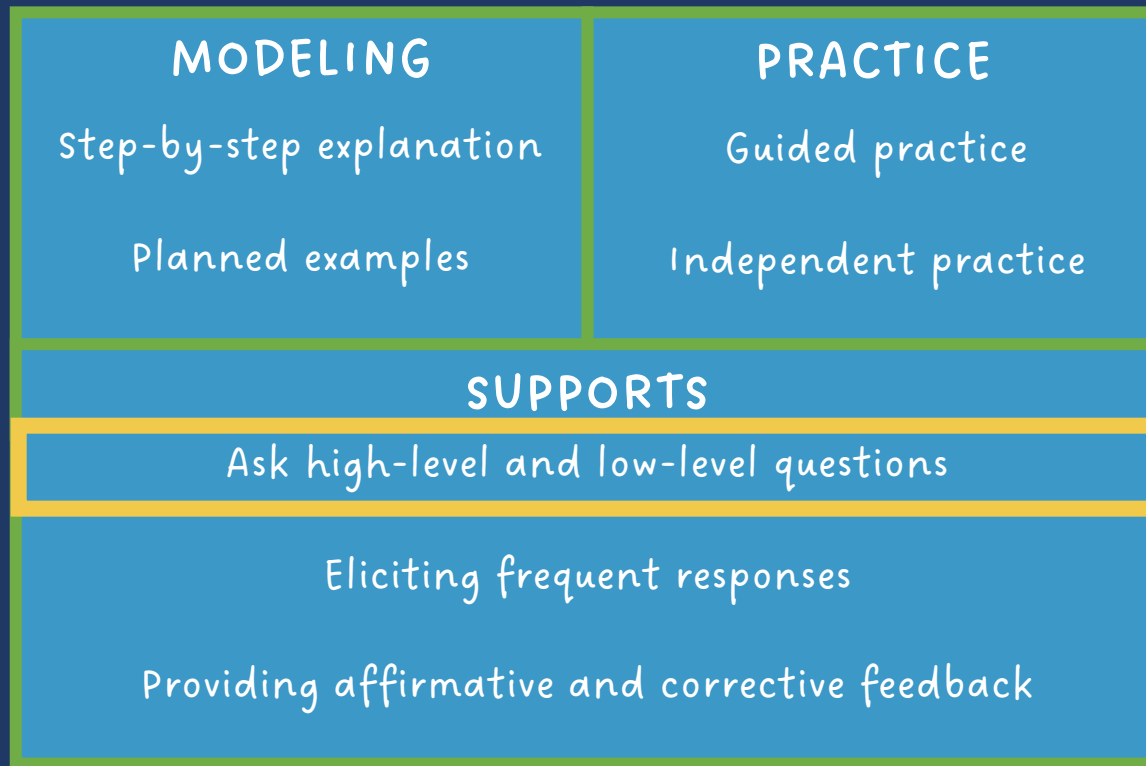
Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback

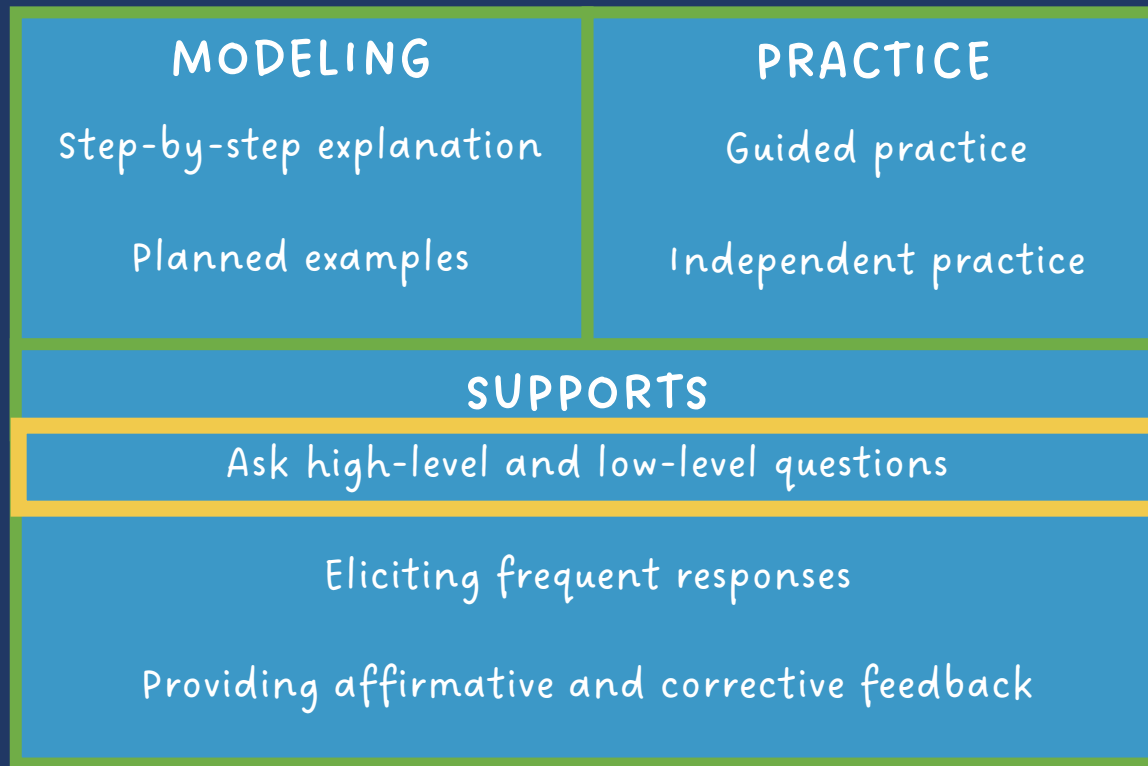
These Supports should be used in both
Modeling and Practice.





During Modeling and Practice, it is essential to engage students and check for understanding.

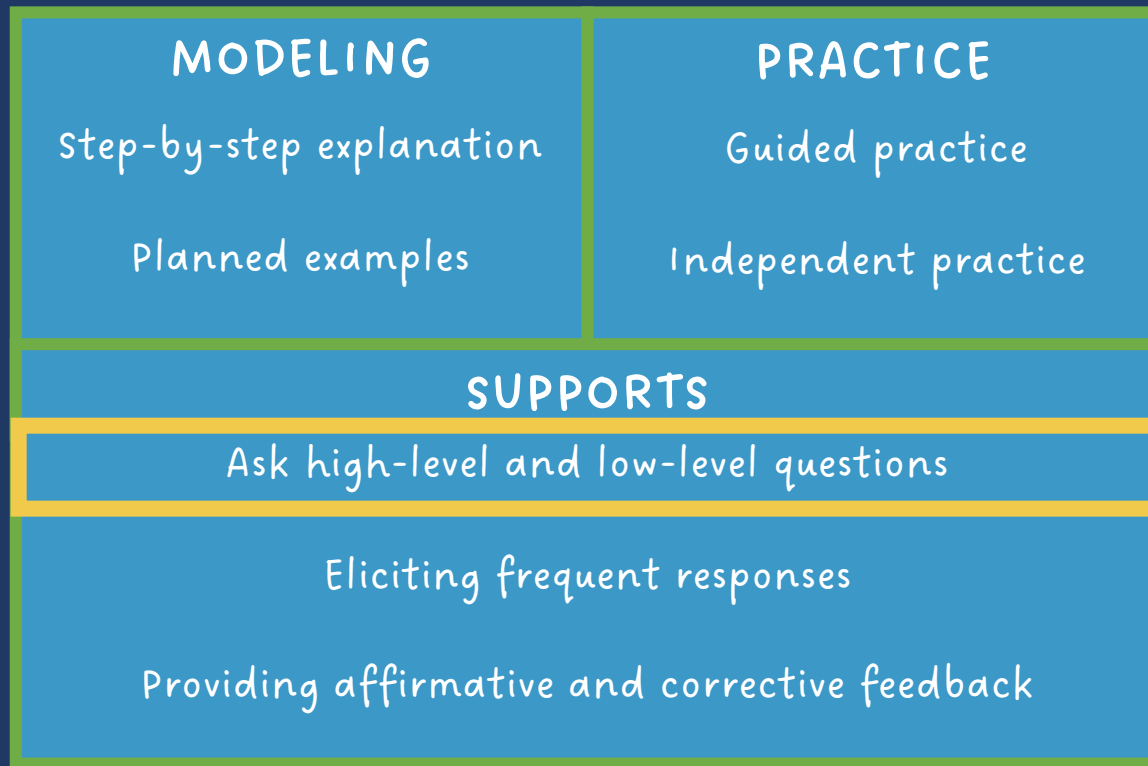




"What is 7 times 9?"

"63."

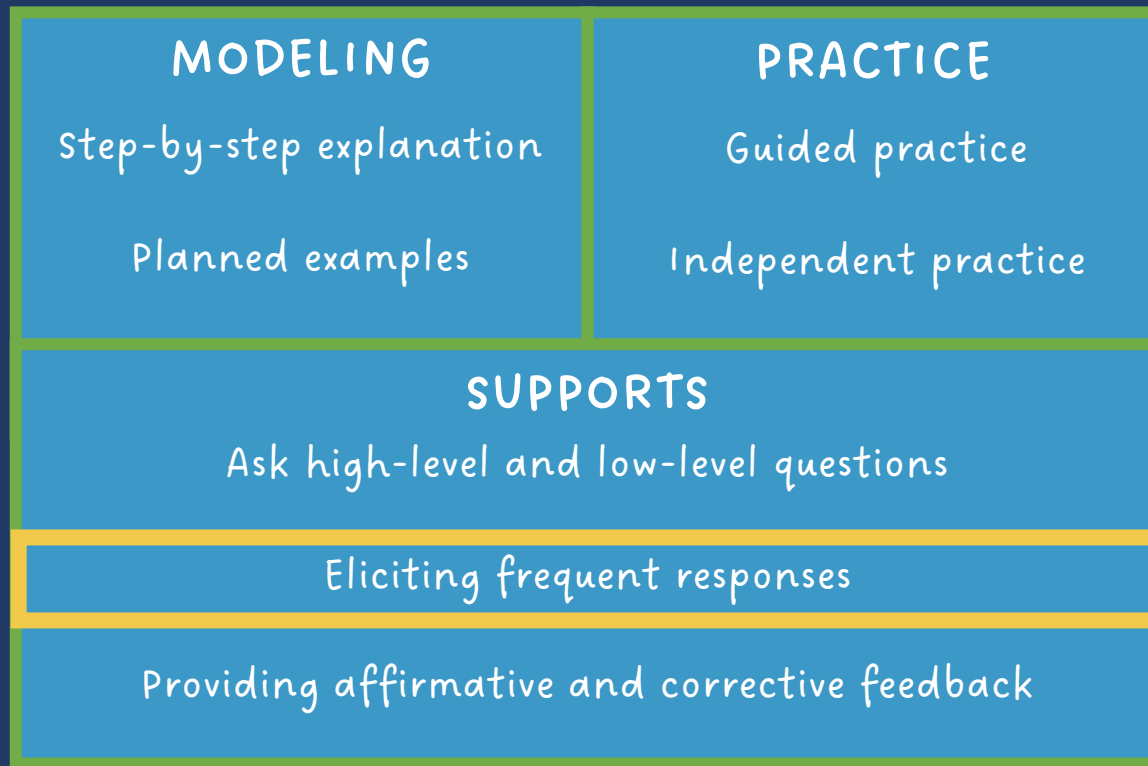




“Why do you have to regroup?”

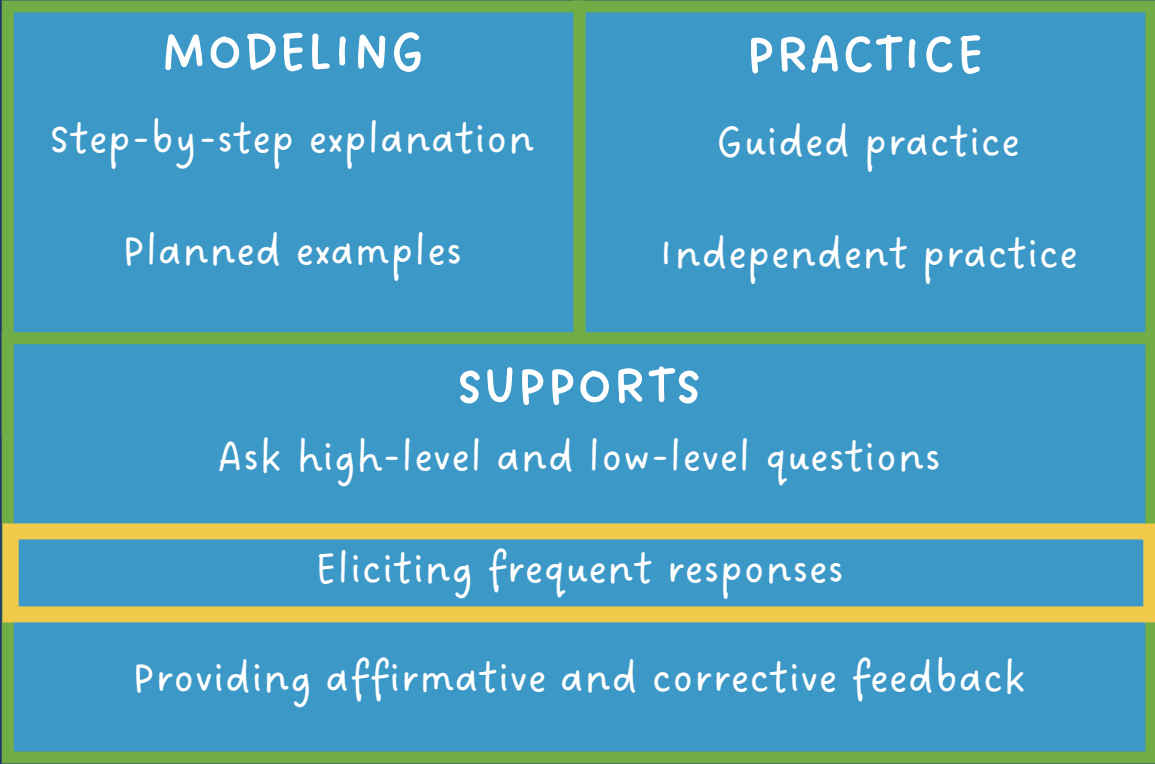
“Because we have 12 ones. When you have more than 9 ones, you have to regroup.”

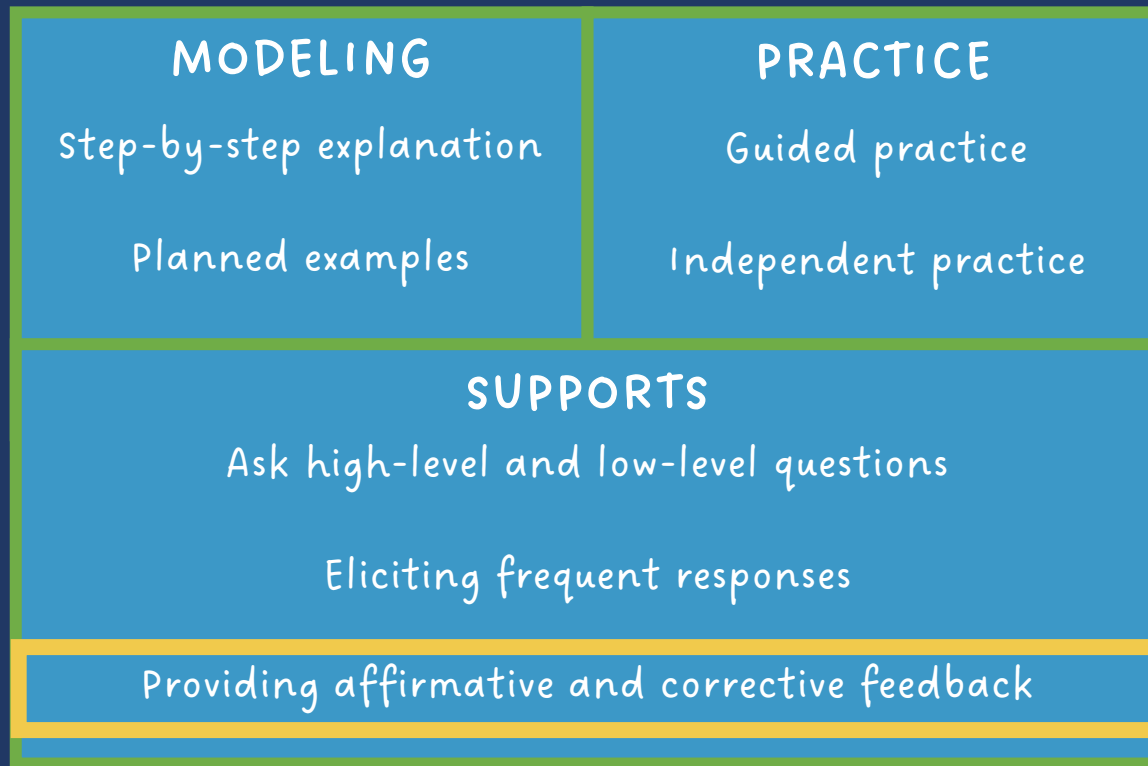




During Modeling and Practice, students should frequently respond. The frequent responses keeps student attention and keeps student learning active.







During Modeling and Practice, students should receive immediate feedback on their responses.



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



“Nice work using your word
problem attack strategy.”



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



"Let's look at that again. Tell me how you added in the hundreds column."



MODELING

Step-by-step explanation

Planned examples

PRACTICE

Guided practice

Independent practice

SUPPORTS

Ask high-level and low-level questions

Eliciting frequent responses

Providing affirmative and corrective feedback



MODEL AND PRACTICE



What are your strengths?



What are your opportunities for growth?



What are your plans for next Monday?

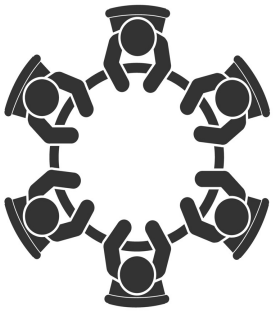
Next month?

Next year?

FLUENCY

Research and Information





What are your strengths with modeling and practice?

What are your opportunities for growth?

What are your plans for next Monday?

Next month?

Next year?



Build Fluency



Instructional Platform

INSTRUCTIONAL DELIVERY

Vocabulary

Representations

Model and
Practice

INSTRUCTIONAL STRATEGIES

Fluency



MODEL AND PRACTICE



What are your strengths?



What are your opportunities for growth?



What are your plans for next Monday?

Next month?

Next year?

FLUENCY

Research and Information





Mathematics fluency, particularly fluency with facts and computation, is related to overall mathematics performance.

(Bailey et al., 2012; Cirino et al., 2019; Koponen et al., 2007, 2017; Vukovic et al., 2014)

Fact fluency practice improves mathematics fact performance.

(Burns et al., 2010; Coddling et al., 2011; McCallum et al., 2004; Nelson et al., 2013; Poncy et al., 2010; Schutte et al., 2015; Stocker & Kubina, 2017)



Fluency is
doing
mathematics
easily and
accurately.

Fluency in
mathematics
makes
mathematics
easier.

Fluency
provides less
stress on
working
memory.

Fluency helps
students build
confidence
with
mathematics.

With fluency, it is important to emphasize both
conceptual learning and procedural learning.



Addition	Subtraction
Multiplication	Division

Counting

Comparing numbers

Representing fractions

Identifying shapes

Counting coins

Telling time

Measurement

Solving equations



Memorization
or automaticity

Ease and
accuracy



FLUENCY

Types of Fluency

Type	Memorization?	
	Yes	No



What are your strengths?



What are your opportunities for growth?



What are your plans for next Monday?

Next month?

Next year?



List different types of fluency. Discuss whether they require memorization.



Addition	Subtraction
Multiplication	Division

Build fluency with math facts.

- Addition: single-digit addends
- Subtraction: single-digit subtrahend
- Multiplication: single-digit factors
- Division: single-digit divisor

$$\begin{array}{r} 5 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ - 4 \\ \hline \end{array}$$

$$\begin{array}{r} 6 \\ \times 7 \\ \hline \end{array}$$

$$\begin{array}{r} 56 \\ \div 8 \\ \hline \end{array}$$



DAILY

BRIEF

Work on small sets of facts

Work on unknown facts
(in combination with known facts)



Dice



Roll the Dice



$$\underline{8} + \underline{7} = \underline{15}$$

$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

Beach Ball

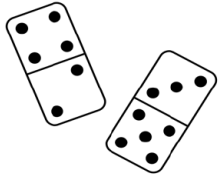


4 plus 6 equals 10.

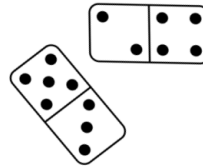
7 plus 6 equals 13.

2 plus 2 equals 4.

Dominoes



Dominoes



$$\underline{4} + \underline{6} = \underline{10}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} \times \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} \times \underline{\quad} = \underline{\quad}$$

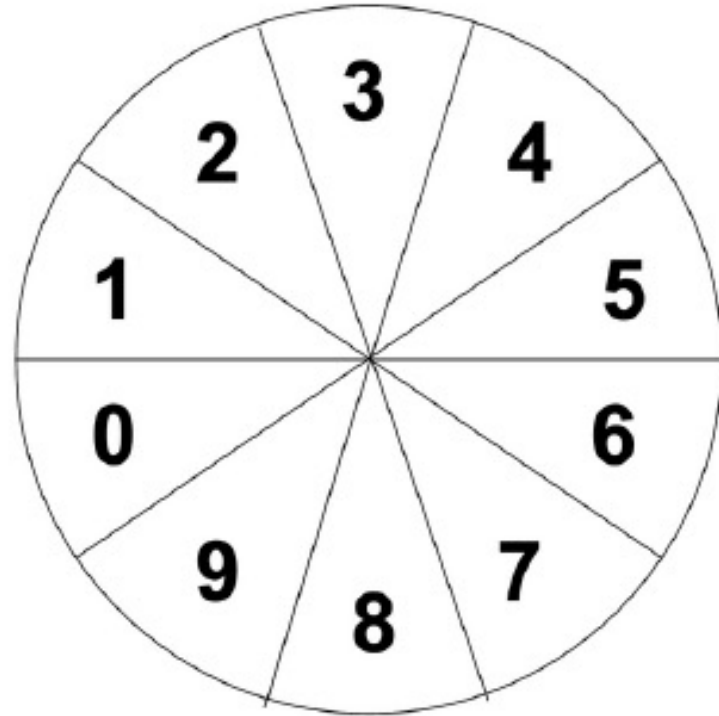


Spinner

2 times 4 equals 8.

6 times 9 equals 54.

7 times 1 equals 7.



Playing Cards

Cards



$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$\underline{6} - \underline{2} = \underline{4}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

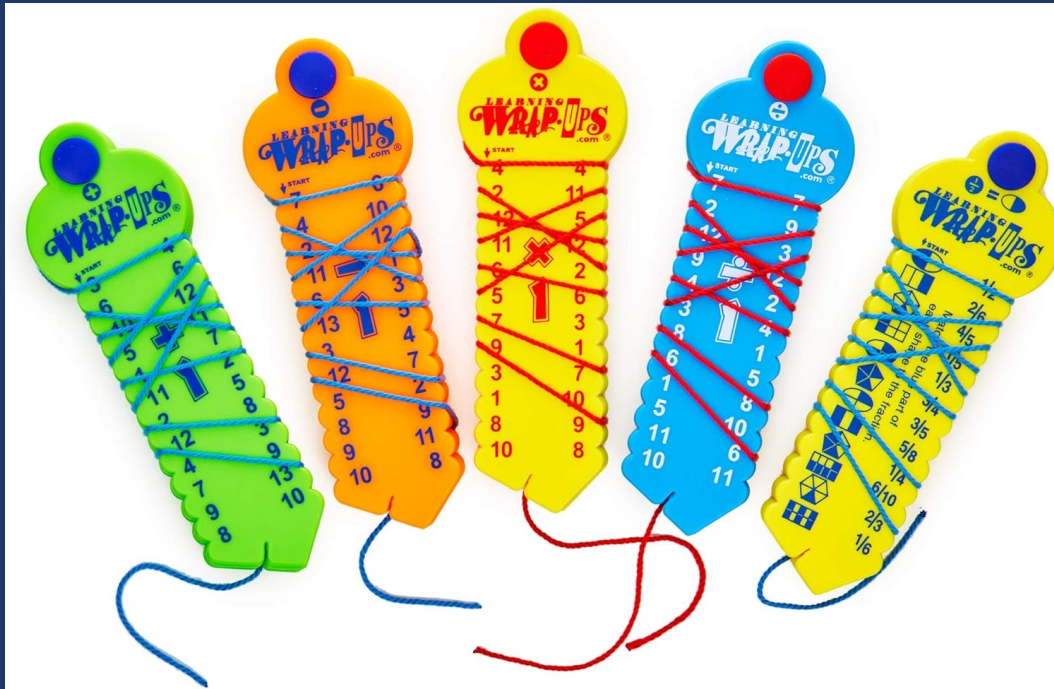
$$\underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$

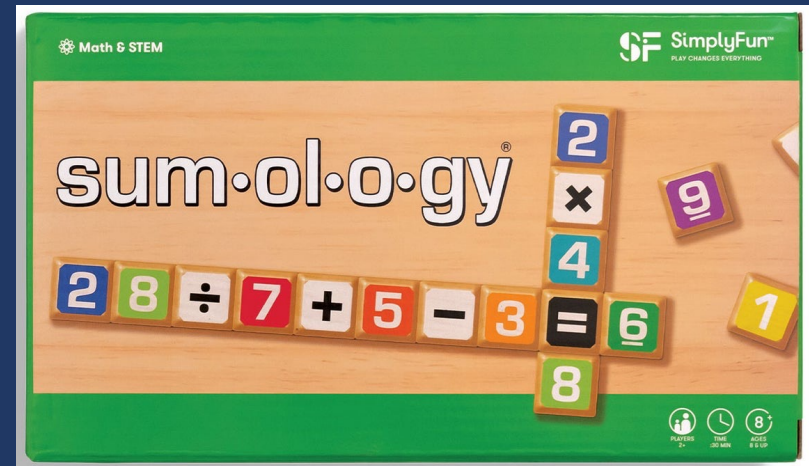
$$\underline{\quad} - \underline{\quad} = \underline{\quad}$$



Wrap-Ups



Mobi Math

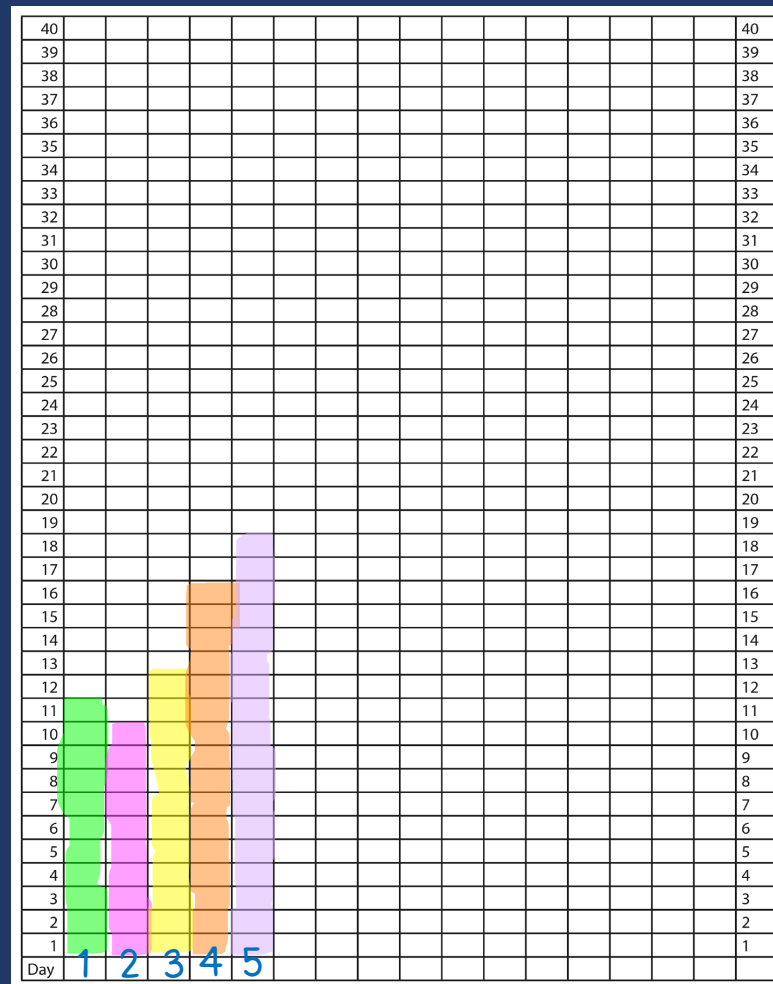


Flash Cards

$$\begin{array}{r} 7 \\ - 6 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ - 4 \\ \hline \end{array}$$

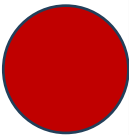
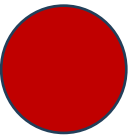
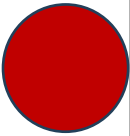
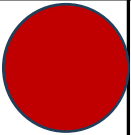
$$\begin{array}{r} 11 \\ - 3 \\ \hline \end{array}$$



Bingo

Math Bingo

Your teacher will call out a math problem. Quickly solve the problem. If you have the answer on your bingo card, cover it with a chip. The middle space is free!
The first person to finish the pattern your teacher decides wins!
(5 in a row, 4 corners, etc.)

12		24	100	
15	0	42	16	20
8	35		6	4
	2	40	27	7
50	10	30	48	14

8 times 10 equals...

3 times 1 equals...

2 plus 3 equals...



Magic Squares

Magic Squares Board

- Place the sum or product in the bottom right corner.
- In the bottom row, create a fact with a sum or product of the bottom right corner.
- In the right column, create a fact with a sum or product of the bottom right corner.
- Create two columns with a sum or product of the bottom number.
- Create two rows with a sum or product of the right column number.
- Write the created facts below.

0	2	2
5	4	9
5	6	11

$$0 + 2 = 2$$

$$2 - 0 = 2$$

$$5 + 4 = 9$$

$$9 - 5 = 4$$

4	5	9
2	0	2
6	5	11

7	3	10
1	0	1
8	3	11

6	1	7
3	2	5
9	3	12

4	4	8
2	2	4
6	6	12

5	1	6
4	3	7
9	4	13

5	1	6
3	4	7
8	5	13

6	3	9
2	3	5
8	6	14

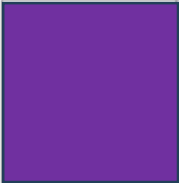
1	5	6
6	2	8
7	7	14

6	2	8
3	4	7
9	6	15



Cover, Copy, Compare

Cover, Copy, Compare

	$\begin{array}{r} 9 \\ \times 6 \\ \hline 54 \end{array}$	$\begin{array}{r} 8 \\ \times 6 \\ \hline 48 \end{array}$	
$\begin{array}{r} 7 \\ \times 8 \\ \hline 56 \end{array}$		$\begin{array}{r} 6 \\ \times 5 \\ \hline 30 \end{array}$	
$\begin{array}{r} 9 \\ \times 9 \\ \hline 81 \end{array}$		$\begin{array}{r} 7 \\ \times 9 \\ \hline 63 \end{array}$	
$\begin{array}{r} 6 \\ \times 7 \\ \hline 42 \end{array}$		$\begin{array}{r} 8 \\ \times 5 \\ \hline 40 \end{array}$	
$\begin{array}{r} 8 \\ \times 8 \\ \hline 64 \end{array}$		$\begin{array}{r} 7 \\ \times 7 \\ \hline 49 \end{array}$	

File folder

$6 + 3 = 9$

$1 + 7 = 8$

$6 + 4 = 10$

$7 + 3 =$

$2 + 7 =$

$5 + 6 =$

$4 + 7 =$

$7 + 8 =$

$6 + 7 =$

$7 + 9 =$

$7 + 6 =$

$8 + 7 =$

$7 + 0 =$

$9 + 6 =$

$6 + 0 =$

$6 + 8 =$



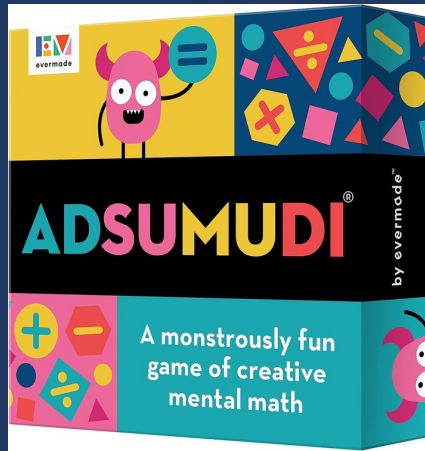
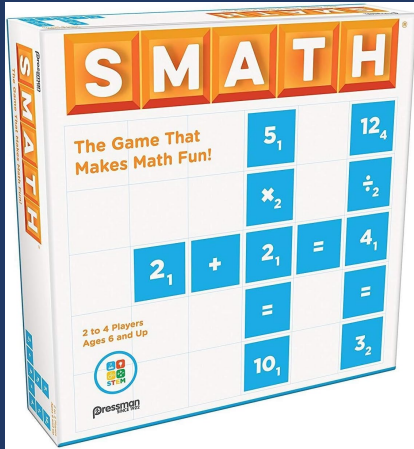
Taped Problems

Taped Problems

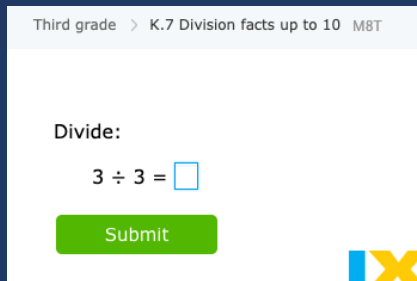
$\begin{array}{r} 8 \\ \times 8 \\ \hline 64 \end{array}$	$\begin{array}{r} 7 \\ \times 7 \\ \hline 49 \end{array}$	$\begin{array}{r} 8 \\ \times 7 \\ \hline \end{array}$
$\begin{array}{r} 6 \\ \times 5 \\ \hline \end{array}$	$\begin{array}{r} 6 \\ \times 7 \\ \hline \end{array}$	$\begin{array}{r} 6 \\ \times 8 \\ \hline \end{array}$
$\begin{array}{r} 5 \\ \times 7 \\ \hline \end{array}$	$\begin{array}{r} 5 \\ \times 5 \\ \hline \end{array}$	$\begin{array}{r} 5 \\ \times 6 \\ \hline \end{array}$
$\begin{array}{r} 6 \\ \times 6 \\ \hline \end{array}$	$\begin{array}{r} 8 \\ \times 6 \\ \hline \end{array}$	$\begin{array}{r} 7 \\ \times 6 \\ \hline \end{array}$
$\begin{array}{r} 7 \\ \times 8 \\ \hline \end{array}$	$\begin{array}{r} 8 \\ \times 5 \\ \hline \end{array}$	$\begin{array}{r} 7 \\ \times 5 \\ \hline \end{array}$



Games




Technology



Get your free 30-day trial

Help your students attain math fact fluency success whether in-person, remote, or through hybrid learning

Game-based system to improve math fact fluency for grades 2-6 in less than 30 days!



Games / Flashcard

Flashcard

subtraction Level 3 1:51

13
- 6



DAILY

BRIEF

Work on small sets of facts

Work on unknown facts
(in combination with known facts)



FLUENCY

Types of Fluency

Type	Memorization?	
	Yes	No



What are your strengths?



What are your opportunities for growth?

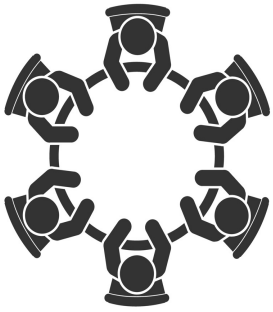


What are your plans for next Monday?

Next month?

Next year?





What are your strengths with building fluency?

What are the opportunities for growth?

What are your plans for next Monday?

Next month?

Next year?



Word Problems



Instructional Platform

INSTRUCTIONAL DELIVERY

Vocabulary

Representations

Model and
Practice

INSTRUCTIONAL STRATEGIES


Fluency


Word Problems




WORD PROBLEMS

Research and Information

 What are your strengths?

 What are your opportunities for growth?

 What are your plans for next Monday?
Next month?
Next year?

MATH

MATH



Key words tied to operations is an ineffective word-problem strategy.

(Karp et al., 2019; Powell et al., 2022)

Using a meta-cognitive strategy improves word-problem performance.

(Freeman-Green et al., 2015; Krawec et al., 2012; Montague et al., 2011; Swanson et al., 2014)

A focus on schemas improves word-problem performance.

(Alghamdi et al., 2020; Cook et al., 2020; Flores et al., 2016; Fuchs et al., 2021; Griffin et al., 2019; Jitendra et al., 2013; Lein et al., 2020; Peltier et al., 2020; Powell et al., 2022; Xin & Xhang, 2009; Zheng et al., 2013)





1. Keywords tied to operations





2. Presenting problems by operation




Teach an attack strategy


Teach about schemas




WORD PROBLEMS

Research and Information

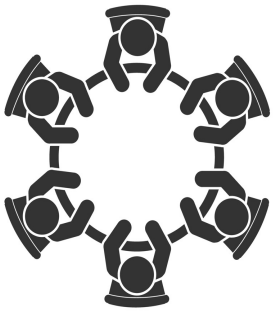
 What are your strengths?

 What are your opportunities for growth?

 What are your plans for next Monday?
Next month?
Next year?

MATH

MATH



What are your strengths with word-problem solving?

What are your opportunities for growth?

What are your plans for next Monday?

Next month?

Next year?



Students require modeling and practice on how to use the language of mathematics.

Students should use hands-on tools, virtual manipulatives, drawings, and other visuals to understand mathematics concepts and procedures.

Teachers should use systematic and explicit instruction to help students develop a strong foundation for specific mathematics skills.

Teachers should use fluency building activities to build counting fluency and fluency with the operations.

Students should learn how to set up and solve word problems by combining an attack strategy with a focus on word-problem schemas.



Instructional Platform

INSTRUCTIONAL DELIVERY

Vocabulary

Representations

Model and
Practice

INSTRUCTIONAL STRATEGIES

Fluency

Word Problems



<https://intensiveintervention.org>

National Center on
INTENSIVE INTERVENTION

at American Institutes for Research

Search

Intensive
Intervention ▾

Tools
Charts ▾

Implementation
Support ▾

Intervention
Materials ▾

Information
For... ▾

Intensive Intervention in Mathematics Course Content

NCII, through a collaboration with the University of Connecticut, developed a set of course content focused on developing educators' skills in designing and delivering intensive mathematics instruction. This content is designed to support faculty and professional development providers with instructing pre-service and in-service educators who are developing and/or refining their implementation of intensive mathematics intervention.

Intensive instruction was recently identified as a [high-leverage practice in special education](#), and DBI is a research based approach to delivering intensive instruction across content areas (NCII, 2013). This course provides learners with an opportunity to extend their understanding of intensive instruction through in-depth exposure to DBI in mathematics, complete with exemplars from actual classroom teachers.

NCII, through a collaboration with the University of Connecticut and the [National Center on Leadership in Intensive Intervention](#) and with support from the [CEEDAR Center](#), developed course content focused on enhancing educators' skills in intensive mathematics intervention. The course includes eight modules that can support faculty and professional development providers with instructing pre-service and in-service educators who are learning to implement intensive mathematics intervention through data-based individualization (DBI). The content in this course complements concepts covered in the [Features of Explicit Instruction Course](#) and so we suggest that users complete both courses.



**MODULE 5: INTENSIVE
MATHEMATICS INTERVENTION:
INSTRUCTIONAL STRATEGIES**





Instructional Routines for Mathematics Intervention

The purpose of these mathematics instructional routines is to provide educators with materials to use when providing intervention to students who experience difficulty with mathematics. The routines address content included in the grades 2-8 Texas Essential Knowledge and Skills (TEKS). There are 23 modules that include routines and examples – each focused on different mathematical content. Each of the 23 modules include vocabulary cards and problem sets to use during instruction. These materials are intended to be implemented explicitly with the aim of improving mathematics outcomes for students.



<https://spedsupportstage.tea.texas.gov/resource-library/instructional-routines-mathematics-intervention>





Myths That Undermine Maths Teaching

Sarah R. Powell, Elizabeth M. Hughes, and Corey Peltier



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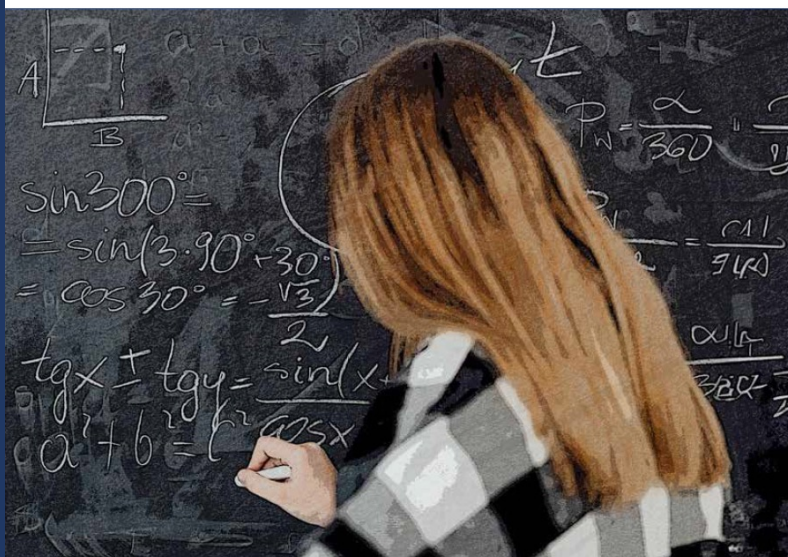
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MATHS PRACTICES YOU CAN COUNT ON

A Guide to Five Research-Validated
Practices in Mathematics

Sarah R. Powell, Sarah G. King, and Sarah A. Benz



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Assisting Students Struggling with Mathematics: Intervention in the Elementary Grades

Educator's Practice Guide

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