Schema-Based Word-Problem Instruction





Sarah R. Powell, Ph.D.

Associate Professor The University of Texas at Austin







srpowell@utexas.edu







Say hello.

Introduce yourself and the mathematics you support.





When you see this icon, it's time to use the Chat Box.

Raise your Zoom hand at anytime.

Drop questions in the Chat Box at anytime.





9:00-9:15	How students solve word problems
9:15-9:20	How you solve a word problem
9:20-9:40	Ineffective strategies
9:40-10:00	Attack strategies + BREAKOUT ROOM
10:00-10:30	Total problems
10:30-11:00	Difference problems
11:00-11:45	Change problems + BREAKOUT ROOM
11:45-12:15	LUNCH
12:15-12:45	Equal groups problems
12:45-1:15	Comparison problems
1:15-1:45	Ratios/Proportions problems + BREAKOUT ROOM
1:45-2:30	Multi-step problems
2:30-3:00	Wrap-up



How Students Solve Word Problems



How did these students solve these problems?









peper fold











































How did these students solve these problems?





they choose reading \bigcirc MOPP











17 iting









the Students choses they Love more math dican en tu 22 math Ø



















Copyright 2023 Sarah R. Powell, Ph.D.

J.














The graph shows the favorite subject of third-grade students. How many more students chose Math than chose Writing?







The graph shows the favorite subject of third-grade students. How many more students chose Math than chose Writing?













Undetermined

Repeated information from problem

Didn't provide answer

Wrong information

Wrong (misapplied) operation

UNCOMMON

Addition error

Subtraction error

XA+H





Maya has 120 caramel apples to sell. Each caramel apple is covered with one topping.

- $\frac{1}{5}$ of the caramel apples are covered with peanuts.
- $\frac{1}{3}$ are covered with chocolate chips.
- $\frac{3}{10}$ are covered with coconut.
- The rest are covered with sprinkles.

How many caramel apples are covered with sprinkles?

- **A** 100
- **B** 33
- **C** 25
- **D** 20



How would you solve this problem? What skills are necessary to solve this problem?











Ineffective Strategies



1.Keywords tied to operations





Lincoln had 8 pencils **fewer** than Roscoe. If Roscoe had 18 pencils, how many pencils did Lincoln have?

Lincoln had 8 pencils **fewer** than Roscoe. If Lincoln had 18 pencils, how many pencils did Roscoe have?





XA+H







Description of Single-St	ep Word I	Problem	s (n = 132	?)							
			Schema-				Keyword(s) led				
	Occurren	nce of	An	y	spec	ific	Multi	ple	to con	rect	
	scher	schema		keyword		keywords ^a		keywords ^a		solution ^a	
Schema	n	%	n	%	n	%	n	%	n	%	
Total	27	20.5	26	96.3	23	88.5	5	19.2	21	80.8	
Difference	17	12.9	17	100.0	14	82.4	2	11.8	12	70.6	
Change	11	8.3	7	63.6	5	71.4	5	71.4	2	28.6	
Equal groups	29	22.0	26	89.7	22	84.6	18	69.2	8	30.8	
Comparison	10	7.6	9	90.0	9	100.0	4	44.4	5	55.6	
Ratios or proportions	29	22.0	23	79.3	9	39.1	9	39.1	6	26.1	
Product of measures	9	6.8	9	100.0	8	88.9	1	11.1	5	55.6	
^a When a problem featu	When a problem featured a keyword.										

×A++



Description of Multi-Ste	p Word Prol	blems (n = a	84)				
	Occurrence of schema*		Any keywor	d	Keyword(s) led to correct solution ^b		
Schema	n	%	n	%	n	%	
Total	40	47.6	39	97.5	3	7.7	
Difference	11	13.1	11	100.0	1	9.1	
Change	21	23.8	19	95.0	1	5.3	
Equal groups	49	58.3	48	98.0	1	2.1	
Comparison	7	8.3	7	100.0	0	0.0	
Ratios or proportions	22	25.0	16	76.2	1	6.3	
Product of measures	7	8.3	7	100.0	2	28.6	

^aSum across schemas does not equal 100 because each word problem featured more than one schema.

^bWhen a problem featured a keyword.



Mr. Rivera's taxable income is \$20 each hour before taxes are taken out. Mr. Rivera worked a total of 40 hours each week for 50 weeks.

What is the dollar amount, to the nearest dollar, taken out for taxes based on Mr. Rivera's taxable income?

Jessica rented 1 video game and 3 movies for a total of \$11.50.

- The video game cost \$4.75 to rent.
- The movies cost the same amount each to rent.

What amount, in dollars, did Jessica pay to rent each movie?

The temperature of a substance decreased by 24°C per minute for 3 minutes. What was the overall change of the temperature of the substance?



Keywords are important to identify and understand Keywords are the mathematical vocabulary that help an students understand what the story is about and what they need to do Talk about keywords ("What does *more than* tell you about?")



But, *do not* tie a keyword to a specific operation!



2. Presenting problems by operation







Effective Strategies



Teach an attack strategy

Teach about schemas



Maya has 120 caramel apples to sell. Each caramel apple is covered with one topping.

- $\frac{1}{5}$ of the caramel apples are covered with peanuts.
- $\frac{1}{3}$ are covered with chocolate chips.
- $\frac{3}{10}$ are covered with coconut.
- The rest are covered with sprinkles.

How many caramel apples are covered with sprinkles?

- **A** 100
- **B** 33
- **C** 25
- **D** 20

What was your process for working through this problem?



Attack Strategy

SOLVE

Study the problem. Organize the facts. Line up the plan. Verify the plan with computation Examine the answer.

R-CUBES

Read the problem. Circle key numbers. Underline the question. Box action words. Evaluate steps. Solve and check.





RIDE

Read the problem. Identify the relevant information. Determine the operation and unit for the answer. Enter the correct numbers and calculate, then check the answer.

RIDGES

Read the problem. I know statement. Draw a picture. Goal statement. Equation development. Solve the equation.



STAR

Stop and read the problem carefully.

Think about your plan and the strategy you will use. Act. Follow your plan and solve

the problem.

Review your answer.

RICE

Read and record the problem. Illustrate your thinking. Compute. Explain your thinking.



SUPER

Slowly read the story problem twice. Underline the question and circle the numbers you need. Picture it. Draw the scenario to show what is happening. Explain the problem with a number sentence. Rewrite the answer in a sentence.

SHINES

Slowly and carefully read the problem. Highlight or underline key information. Identify the question by drawing a circle around it. Now solve the problem. Show your work. Examine your work for precision, accuracy, and clarity. Share your answer by writing a sentence.



SOLVE

Study the problem.

Organize the facts.

Line up the plan.

Verify the plan with computation.

Examine the answer.

R-CUBES

Read the problem. Circle key numbers. Underline the question. Box action words. Evaluate steps. Solve and check.









Share your favorite attack strategy.

Describe how you will use the attack strategy in your teaching,



Teach an attack strategy

Teach about schemas





Difference

Change

Equal Groups

Comparison

Ratios/Proportions



Additive Word Problems
Meanings of Addition
Meanings of Subtraction





Count one set, count another set, put sets together, count sum



2 + 3 = 5



Parts put together into a total

Karly saw 4 cardinals and 5 blue jays. How many birds did Karly see?





Start with a set, add the other set, count sum



2 + 3 = 5


An amount that **increases** or decreases

Silas had \$4. Then they earned \$5 for cleaning their room. How much money does Silas have now?



6 + 7 = ____

Share a Total story.

Share a Change/Join story.





Start with a set, take away from that set, count difference



5 - 3 = 2



An amount that increases or **decreases**

Bronwyn had **9** cookies. Then they ate **2** of the cookies. How many cookies does Bronwyn have now?





Compare two sets, count difference



5 - 3 = 2



Greater and less amounts compared for a difference

Rachel has *9* pencils. Jodie has 4 pencils. How many more pencils does Rachel have? (How many fewer does Jodie have? What's the difference between Rachel's and Jodie's pencils?)



14 - 8 = ____

Share a Change/Separate story.

Share a Difference story.



Schema and Definition	Equations and Graphic Organizers	Examples			Variations
Total (Combine; Part-part- whole) Parts combined for a sum	P1 + P2 = T (part + part = total) (part) (part)	Sum unknown: Lyle has 11 red apples and 18 green apples. How many apples does Lyle have altogether?	Part unknown: Lyle has 29 red and green apples. If 11 of the apples are red, how many green apples does Lyle have?		More than two parts: Lyle has 34 apples. Of the apples, 11 are red, 18 are green, and the rest are yellow. How many yellow apples does Lyle have?
Difference (Compare) Sets compared for a difference	B - s = D (bigger - smaller = difference) G - L = D (greater - less = difference) (greater) (greater) (lesser) (difference)	Difference un- known: Sasha wrote 85 words in her essay, and Tabitha wrote 110 words. How many fewer words did Sasha write than Tabitha?	Bigger/greater unknown: Tabitha wrote 25 more words than Sasha. If Sasha wrote 85 words, how many words did Tabitha write?	Smaller/lesser unknown: Tabitha wrote 110 words in her essay. Sasha wrote 25 words fewer than Tabitha. How many words did Sasha write?	(None)
Change (Join; Separate) An amount that increases or decreases	ST +/- C = E (start +/- change = end) (start) (change) (end)	End (increase) unknown: Jorge had \$52. Then, he earned \$16 babysitting. How much money does Jorge have now?	Change (increase) unknown: Jorge had \$52. Then, he earned some money babysitting. Now, Jorge has \$68. How much did Jorge earn babysitting?	Start (increase) unknown: Jorge has some money, and then he earned \$16 for babysitting. Now, Jorge has \$68. How much money did he have to start with?	Multiple changes: Jorge had \$78. He stopped and bought a pair of shoes for \$42 and then he spent \$12 at the grocery. How much money does Jorge have now?
	(beginning) (end)	End (decrease) unknown: Jorge had \$52. Then, he spent \$29 at the ballpark. How much money does Jorge have now?	Change (decrease) unknown: Jorge had \$52 but spent some money when he went to the ballpark. Now, Jorge has \$23. How much did Jorge spend at the ballpark?	Start (decrease) unknown: Jorge had some money. Then, he spent \$29 at the ballpark and has \$23 left. How much money did Jorge have before going to the ballpark?	



Total

Additive Word Problems		
A. Ali delivered 12 boxes of cookies on Friday and 25 boxes of cookies on Saturday. How many boxes of cookies did Ali deliver?	B. In March and April, it rained a total of 11.4 inches. If it rained 3.9 inches in March, how many inches did it rain in April?	
C. Sam mows lawns and made \$560 last week. She made \$95 on Monday, \$135 on Tuesday, and \$70 on Wednesday. How much did Sam make on Thursday and Friday?	NOTES ABOUT TOTAL PROBLEMS:	





XA+H



"Are parts put together for a total?"







Total

Additive Word Problems		
A. Ali delivered 12 boxes of cookies on Friday and 25 boxes of cookies on Saturday. How many boxes of cookies did Ali deliver?	B. In March and April, it rained a total of 11.4 inches. If it rained 3.9 inches in March, how many inches did it rain in April?	
C. Sam mows lawns and made \$560 last week. She made \$95 on Monday, \$135 on Tuesday, and \$70 on Wednesday. How much did Sam make on Thursday and Friday?	NOTES ABOUT TOTAL PROBLEMS:	



Total





Difference Compare

Greater and **lesser** amounts compared for a **difference**

Adrianna has 10 pencils. Tracy has 4 pencils. How many more pencils does Adrianna have?

Adrianna has 6 more pencils than Tracy. If Tracy has 4 pencils, how many does Adrianna have?

Tracy has 6 fewer pencils than Adrianna. Adrianna has 10 pencils. How many pencils does Tracy have? Difference

Greater amount

Lesser amount





"Are parts put together for a total?"

Difference

"Are amounts compared for a difference?"



Difference



Difference

Additive Word Problems		
D. Audrey has 162 wooden beads and 95 glass beads. What is the difference between Audrey's wooden beads and glass beads?	E. Damian's dog eats 9 1/2 cups of dog food each week. Monte's dog eats 4 1/4 cups less each week than Damian's dog. How much does Monte's dog eat in a week?	
F. The temperature in Norfolk was 12 degrees warmer than in Roanoke where the temperature was 79 degrees. It was 86 degrees in Marion. What was the temperature in Norfolk?	NOTES ABOUT DIFFERENCE PROBLEMS:	
	1	





Write a Difference problem.



An amount that increases or decreases

Nickole had 6 notebooks. Then, she bought 3 notebooks. How many notebooks does Nickole have now?

Nickole had 6 notebooks. Then, she bought a few more notebooks. Now, Nickole has 9 notebooks. How many notebooks did she buy?

Nickole had some notebooks. Then, she bought 3 notebooks. Now, Nickole has 9 notebooks. How many notebooks did she have to start with? Change amount

Start amount



Separate

An amount that increases or decreases

Samantha baked 20 cookies. Then, she ate 3 of the cookies. How many cookies does Samantha have now?

Samantha baked 20 cookies. Then, she ate some of the cookies. Now, she has 17 cookies. How many cookies did Samantha eat?

Samantha baked some cookies. She ate 3 of the cookies and has 17 cookies left. How many cookies did Samantha bake?

End amount

Change amount

Start amount



Copyright 2023 Sarah R. Powell, Ph.D.

Change



"Are parts put together for a total?"

Difference

"Are amounts compared for a difference?"

Change

'Does an amount increase or decrease?"







Change

Additive Word Problems		
G. A plant was 3 3/4 inches tall at the beginning of June. By the end of July, the plant was 9 1/8 inches tall. How many inches did the plant grow in 2 months?	H. Martina has some money in her bank ac- count. Then, she spent \$135.69 and has a balance of -\$24.80. How much money did Martina have to begin with?	
I. Hui saved \$70 in January. In February, she spent \$64 of the money she saved. She saved \$92 more in March. How much has Hui saved by the end of March?	NOTES ABOUT CHANGE PROBLEMS:	



Change

Write a Change problem.





Schema Check!





Pablo goes to a stamp show where he can share, buy, and sell stamps.

26. Part A

The first day, Pablo starts with 744 stamps. He buys 27 stamps from his friend. He then sells 139 stamps.

What is the total number of stamps that Pablo has after the first day of the stamp show?



Difference

The graph below shows the number of pounds of plastic the Keller family recycled for five months.



Based on the graph, how many more pounds of plastic did the family recycle in July than in April?

0

s adde s

Total

Mr. Conley delivers packages. The bar graph shows the total number of packages he delivered on five days last week.



Package Delivery

10. Part A

What is the total number of packages Mr. Conley delivered on Monday and Tuesday?

- A 300
- B 340
- © 350
- 360
 360



Schema and Definition	Equations and Graphic Organizers	Examples			Variations
Total (Combine; Part-part- whole) Parts combined for a sum	P1 + P2 = T (part + part = total) (part) (part)	Sum unknown: Lyle has 11 red apples and 18 green apples. How many apples does Lyle have altogether?	Part unknown: Lyle has 29 red and green apples. If 11 of the apples are red, how many green apples does Lyle have?		More than two parts: Lyle has 34 apples. Of the apples, 11 are red, 18 are green, and the rest are yellow. How many yellow apples does Lyle have?
Difference (Compare) Sets compared for a difference	B - s = D (bigger - smaller = difference) G - L = D (greater - less = difference) (greater) (greater) (lesser) (difference)	Difference un- known: Sasha wrote 85 words in her essay, and Tabitha wrote 110 words. How many fewer words did Sasha write than Tabitha?	Bigger/greater unknown: Tabitha wrote 25 more words than Sasha. If Sasha wrote 85 words, how many words did Tabitha write?	Smaller/lesser unknown: Tabitha wrote 110 words in her essay. Sasha wrote 25 words fewer than Tabitha. How many words did Sasha write?	(None)
Change (Join; Separate) An amount that increases or decreases	ST +/- C = E (start +/- change = end) (start) (change) (end)	End (increase) unknown: Jorge had \$52. Then, he earned \$16 babysitting. How much money does Jorge have now?	Change (increase) unknown: Jorge had \$52. Then, he earned some money babysitting. Now, Jorge has \$68. How much did Jorge earn babysitting?	Start (increase) unknown: Jorge has some money, and then he earned \$16 for babysitting. Now, Jorge has \$68. How much money did he have to start with?	Multiple changes: Jorge had \$78. He stopped and bought a pair of shoes for \$42 and then he spent \$12 at the grocery. How much money does Jorge have now?
	(beginning) (end)	End (decrease) unknown: Jorge had \$52. Then, he spent \$29 at the ballpark. How much money does Jorge have now?	Change (decrease) unknown: Jorge had \$52 but spent some money when he went to the ballpark. Now, Jorge has \$23. How much did Jorge spend at the ballpark?	Start (decrease) unknown: Jorge had some money. Then, he spent \$29 at the ballpark and has \$23 left. How much money did Jorge have before going to the ballpark?	





Which of these schemas would be important to teach?How do you plan to teach the schemas to your students?What additional information or materials do you need?



Multiplicative Word Problems
Meanings of Multiplication
Meanings of Division



Equal Groups

Show the groups, show the amount for each group, count product



$3 \times 2 = 6$



Equal Groups

Show the groups, show the amount for each group, count product



$3 \times 2 = 6$



Groups multiplied by number in each group for a product

Rhiannon has 2 boxes of crayons. There are 12 crayons in each box. How many crayons does Rhiannon have altogether?





Show a set, then multiply the set



$3 \times 2 = 6$


Set multiplied by a number of times for a product

Vivienne picked 6 apples. Jessica picked 2 times as many apples as Vivienne. How many apples did Jessica pick?



4 × 3 = ____

Share an Equal Groups story.

Share a Comparison story.



Equal Groups (Partitive Division)

Show the dividend, divide equally among divisor, count quotient





Equal Groups (Quotative Division)

Show the dividend, make groups of the divisor, count groups





Groups multiplied by number in each group for a product

Stefanie has 12 apples. She wants to share them equally among her 2 friends. How many apples will each friend receive?

Nicole has 12 apples. She put them into bags containing 6 apples each. How many bags did Nicole use?



15 ÷ 5 = ____

Share a Partitive story.

Share a Quotative story.





Difference

Change

Equal Groups

Comparison

Ratios/Proportions



		-			
Schema and Definition	Graphic Organizers	Examples			Variations
Equal Groups (Vary) A number of equal sets or units	(groups/ units) x = / (product) rate)	Product unknown: Maria bought 5 cartons of eggs with 12 eggs in each carton. How many eggs did Maria buy?	Groups unknown: Maria bought 60 eggs. The eggs were sold in cartons with 12 eggs each. How many cartons of eggs did Maria buy?	Number unknown: Maria bought 5 cartons of eggs for a total of 60 eggs. How many eggs were in each carton?	With rate: Maria bought 5 cartons of eggs. Each carton cost \$2.95. How much did Maria spend on eggs?
Comparison One set as a multiple or part of another set	(set) × (multiplier/ (product)	Product unknown: Malik picked 7 flowers. Danica picked 3 times as many flowers. How many flowers did Danica pick?	Set unknown: Danica picked 3 times as many flowers as Malik. If Danica picked 21 flowers, how many flowers did Malik pick?	Times unknown: Malik picked 7 flowers. Danica picked 21 flowers. How many times more flowers did Danica pick?	With fraction: Malik picked 25 red and yellow flowers. If 1/5 of the flowers were yellow, how many were red?
Proportions		Subject unknown: Sally typed 56 words in 2 minutes. How many words could Sally type in 7 minutes?	Object unknown: Sally typed 56 words in 2 minutes. How many minutes would it take Sally to type 192 words?		With percentage: Watson received an 80% on his science quiz. If the test had 40 questions, how many questions did Watson answer correctly?
		Base unknown: Justin baked cookies and brownies. The ratio of cookies to brownies was 3:5. If he baked 15 cookies, how many brownies did he bake?	Compared unknown: Justin baked cookies and brownies. The ratio of cookies to brownies was 3:5. If he baked 25 brownies, how many cookies did he bake?	Ratio unknown: Justin baked 15 cookies and 25 brownies. What's the ratio of cookies to brownies?	Wth unit rate: Paula bought 5 boxes of markers. She spent \$9.75. What is the price of one box of markers?



Equal Groups Array Vary

Groups multiplied by number in each group for a product

Toni has 2 boxes of crayons. There are 12 crayons in each box. How many crayons does Toni have altogether?

Toni has 24 crayons. They want to place them equally into 2 boxes. How many crayons will Toni place in each box?

Toni has 24 crayons. They put them into boxes with 12 crayons each. How many boxes did Toni use?

Product

Number in each group

Groups



"Are there groups with an equal number in each group?"









Multiplicative Word Problems				
A. Lola baked 6 pies. For each pie, Lola used 5 apples. How many apples did Lola use?	B. Jane bought 112 light bulbs. The light bulbs come in packs of 4. How many packs of light bulbs did Jane buy?			
C. Zachary has 3 feet of string. He makes braclets, and each bracelet needs 5 1/4 inches of string. How many bracelets could Zachary make?	NOTES ABOUT EQUAL GROUPS PROBLEMS:			





Write an Equal Groups problem.



Set multiplied by a number of times for a product

Brooke ran 6 minutes. Shaleeni ran 4 times longer than Brooke. How many minutes did Shaleeni run?





"Are there groups with an equal number in each group?"

Comparison

"Is a set compared a number of times?"









Comparison

Multiplicative Word Problems				
D. Enrique has 2 times as many pencils as Ava. Ava has 6 pencils. How many pencils does Enrique have?	E. Susan has 7 times as many books as Mo. Mo has 18 books. How many books Susan has?			
	NOTES ABOUT COMPARISON PROBLEMS:			
F. Sally typed 56 words in 2 minutes. At this rate, how many words could Sally type in 7 minutes?	G. An airplane's altitude changed -378 feet over 7 minutes. What was the mean change of altitude in feet per minute?			
	·			



Comparison



Write a Comparison problem.



Description of **relationships** among quantities

Melissa baked cookies and brownies. The ratio of cookies to brownies was 3:5. If she baked 25 brownies, how many cookies did she bake?

Emma typed 56 words in 2 minutes. At this rate, how many words could Emma type in 7 minutes?



"Are there groups with an equal number in each group?"

Comparison

"Is a set compared a number of times?"

Ratios/Proportions

"Are there relationships among quantities - if this, then this?"









Multiplicative Word Problems				
D. Enrique has 2 times as many pencils as Ava. Ava has 6 pencils. How many pencils does Enrique have?	E. Susan has 7 times as many books as Mo. Mo has 18 books. How many books Susan has?			
	NOTES ABOUT COMPARISON PROBLEMS:			
F. Sally typed 56 words in 2 minutes. At this rate, how many words could Sally type in 7 minutes?	G. An airplane's altitude changed -378 feet over 7 minutes. What was the mean change of altitude in feet per minute?			





Write a Ratios or Proportions problem.





Schema Check!



Mr. Kowolski ordered 35 boxes of granola bars. Each box contained 24 granola bars.

What is the total number of granola bars Mr. Kowolski ordered?



A company makes 625 cell phone cases each day. How many cell phone cases does the company make in 31 days?



Danielle's full-grown dog weighs 10 times as much as her puppy. The puppy weighs 9 pounds.

Enter the number of pounds the full-grown dog weighs.



		-			
Schema and Definition	Graphic Organizers	Examples			Variations
Equal Groups (Vary) A number of equal sets or units	(groups/ units) x = / (product) rate)	Product unknown: Maria bought 5 cartons of eggs with 12 eggs in each carton. How many eggs did Maria buy?	Groups unknown: Maria bought 60 eggs. The eggs were sold in cartons with 12 eggs each. How many cartons of eggs did Maria buy?	Number unknown: Maria bought 5 cartons of eggs for a total of 60 eggs. How many eggs were in each carton?	With rate: Maria bought 5 cartons of eggs. Each carton cost \$2.95. How much did Maria spend on eggs?
Comparison One set as a multiple or part of another set	(set) × (multiplier/ (product)	Product unknown: Malik picked 7 flowers. Danica picked 3 times as many flowers. How many flowers did Danica pick?	Set unknown: Danica picked 3 times as many flowers as Malik. If Danica picked 21 flowers, how many flowers did Malik pick?	Times unknown: Malik picked 7 flowers. Danica picked 21 flowers. How many times more flowers did Danica pick?	With fraction: Malik picked 25 red and yellow flowers. If 1/5 of the flowers were yellow, how many were red?
Proportions		Subject unknown: Sally typed 56 words in 2 minutes. How many words could Sally type in 7 minutes?	Object unknown: Sally typed 56 words in 2 minutes. How many minutes would it take Sally to type 192 words?		With percentage: Watson received an 80% on his science quiz. If the test had 40 questions, how many questions did Watson answer correctly?
		Base unknown: Justin baked cookies and brownies. The ratio of cookies to brownies was 3:5. If he baked 15 cookies, how many brownies did he bake?	Compared unknown: Justin baked cookies and brownies. The ratio of cookies to brownies was 3:5. If he baked 25 brownies, how many cookies did he bake?	Ratio unknown: Justin baked 15 cookies and 25 brownies. What's the ratio of cookies to brownies?	Wth unit rate: Paula bought 5 boxes of markers. She spent \$9.75. What is the price of one box of markers?





Which of these schemas would be important to teach?How do you plan to teach the schemas to your students?What additional information or materials do you need?





Difference

Change

Equal Groups

Comparison

Ratios/Proportions



Total	Difference	Change	Equal Groups	Comparison	Ratio/ Proportion
-------	------------	--------	-----------------	------------	----------------------



Teach an attack strategy

Teach about schemas







Solve the problem

What skills are necessary to solve this problem?









Multi-Step Problems		
A. Leslie had 3 pizzas. Each pizza was cut into 8 pieces. Leslie ate 2 pieces. How many pieces were left?	B. Mr. Kahn gave away 8 blue balloons and 6 red balloons. He gave away 3 times the number of white balloons as red balloons. What was the total number of balloons Mr. Kahn gave away?	
C. An egg farm packages 264 total cartons of eggs each month. The farm has 3 different sizes of cartons. The small carton hold 8 eggs, and 1/6 of the total cartons are small. The medium carton holds 12 eggs, and 2/3 of the total cartons are medium. The large carton holds 18 eggs, and the rest of the total cartons are large. Determine how many each size of carton is needed each month. Then determine how many eggs are needed to fill the 264 cartons.		



Teach an attack strategy

Teach about schemas








Pirate Math Equation Quest



https://intensiveintervention.org/intensive-intervention-math-course





Intensive Intervention in Mathematics Course Content

NCII, through a collaboration with the University of Connecticut, developed a set of course content focused on developing educators' skills in designing and delivering intensive mathematics instruction. This content is designed to support faculty and professional development providers with instructing purservice and in-service educators who are developing and/or refining their implementation of intensive mathematics intervention.

Intensive instruction was recently identified as a high-leverage practice in special education^a, and DBI is a research based approach to delivering intensive instruction across content areas (NCII, 2013). This course provides learners with an opportunity to extend their understanding of intensive instruction through in-depth exposure to DBI in mathematics, complete with exemplars from actual classroom teachers.

NCII, through a collaboration with the University of Connecticut and the National Center on Leadership in Intensive Intervention and with support from the CEEDAR Center , developed course content focused on enhancing educators' skills in intensive mathematics intervention. The course includes eight modules that can support faculty and professional development providers with instructing pre-service and in-service educators who are learning to implement intensive mathematics intervention through data-based individualization (DBI). The content in this course complements concepts covered in the Features of Explicit Instruction Course and so we suggest that users complete both courses.

MODULE 5: INTENSIVE MATHEMATICS INTERVENTION: INSTRUCTIONAL STRATEGIES





https://www.amazon.com/Teaching-Math-Middle-School-Students/dp/1598572741





Sarah R. Powell, Ph.D.

Associate Professor The University of Texas at Austin







srpowell@utexas.edu



