## Math 4315 - PDEs Home Work 1

1. Solve the following PDEs using a change of coordinates  $(x, y) \rightarrow (r, s)$ 

(i) 
$$u_x + u_y = 6y,$$
  
(ii)  $u_x - 2u_y = -u, \quad u(x,0) = x$   
(iii)  $yu_x - xu_y = x,$   
(iv)  $2xu_x + 3yu_y = x, \quad u(x,x) = 1,$ 

2. Show that under the change of variables

$$r = R(x+y), \quad s = s(x,y),$$

the PDE

$$u_x - u_y = 0,$$

becomes

 $u_{s} = 0.$ 

For the following boundary conditions, show that it is possible to choose R(x + y) and s(x, y) such that the boundary in the (r, s) plane is s = 0 and the two boundaries can be connected via x = r.

(i) 
$$u(x,0) = f(x)$$
  
(ii)  $u(x,1) = f(x)$   
(iii)  $u(x,x) = f(x)$ 

Due: Sept. 18, 2020.