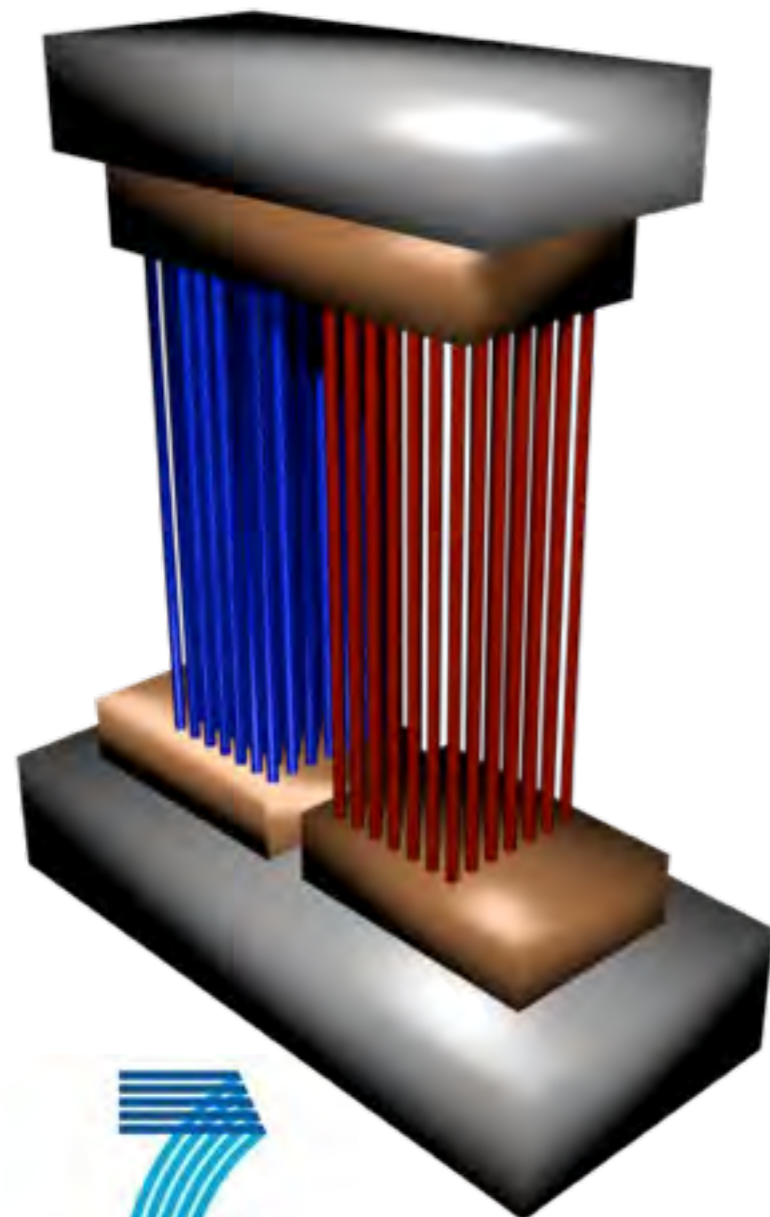


Generate Renewable Energy Efficiently using Nanofabricated Silicon (GREEN Silicon)



**L. Ferre Llin, F. Mirando, A. Samarelli, A. Odia,
J.M.R. Weaver & P. Dobson, D.J. Paul**

University of Glasgow, U.K.

S. Cecchi, G. Isella, D. Chrastina

L-NESS, Politecnico de Milano, Como, Italy

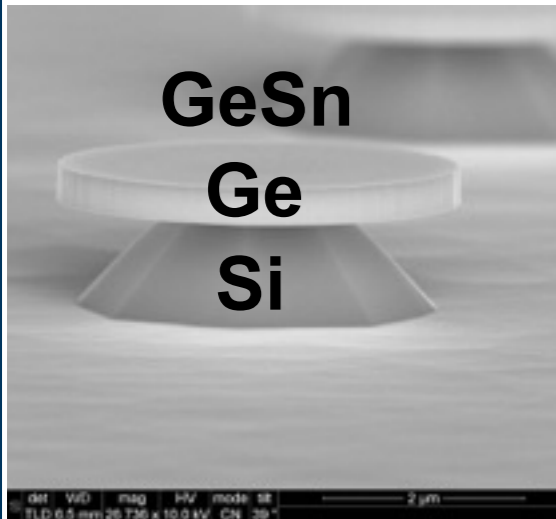
T. Etzelstorfer & J. Stangl

University of Linz, Austria

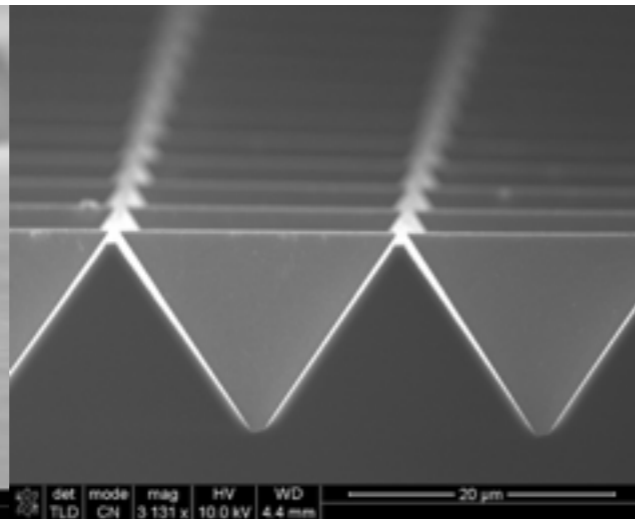
E. Müller Gubler

ETH Zürich, Switzerland

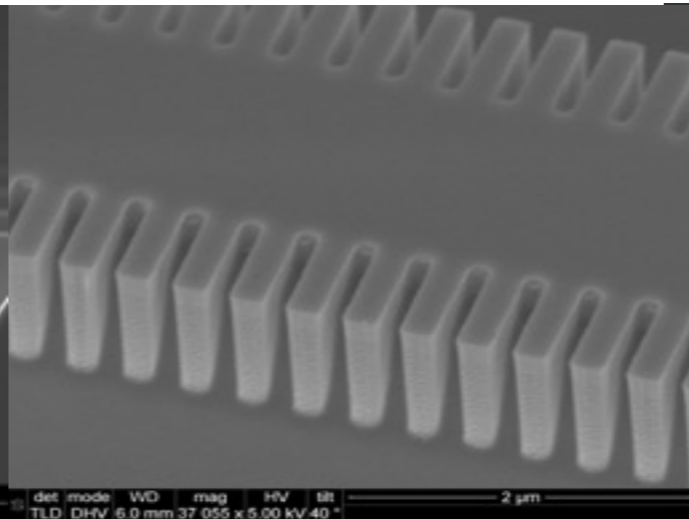
Si Photonics



Si thermal photovoltaics



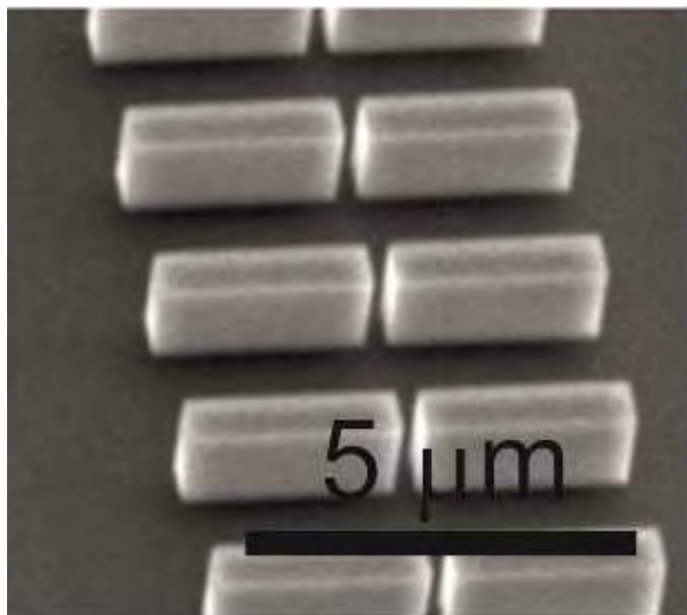
Miniature cold atom systems



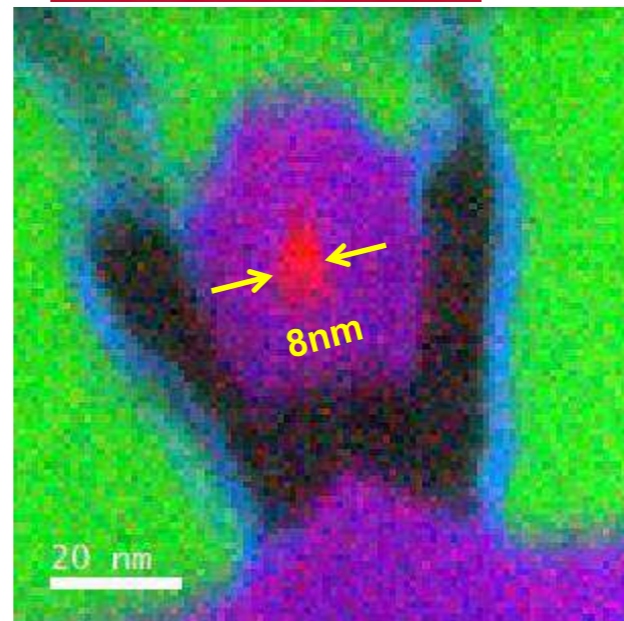
MEMS gravimeters



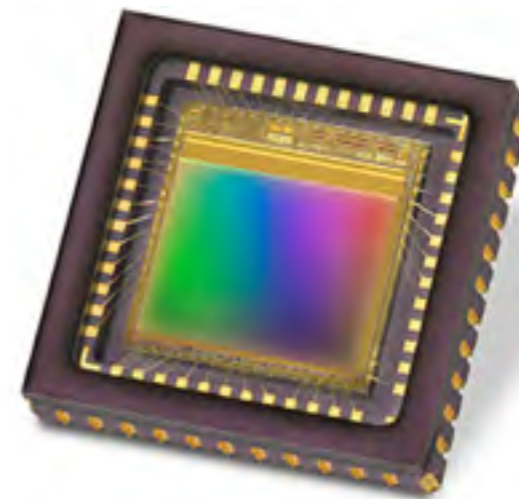
Science & Technology
Facilities Council



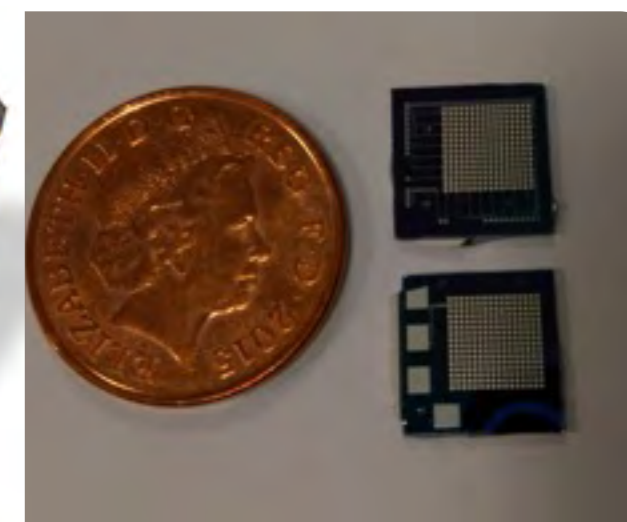
Ge MIR Plasmonics



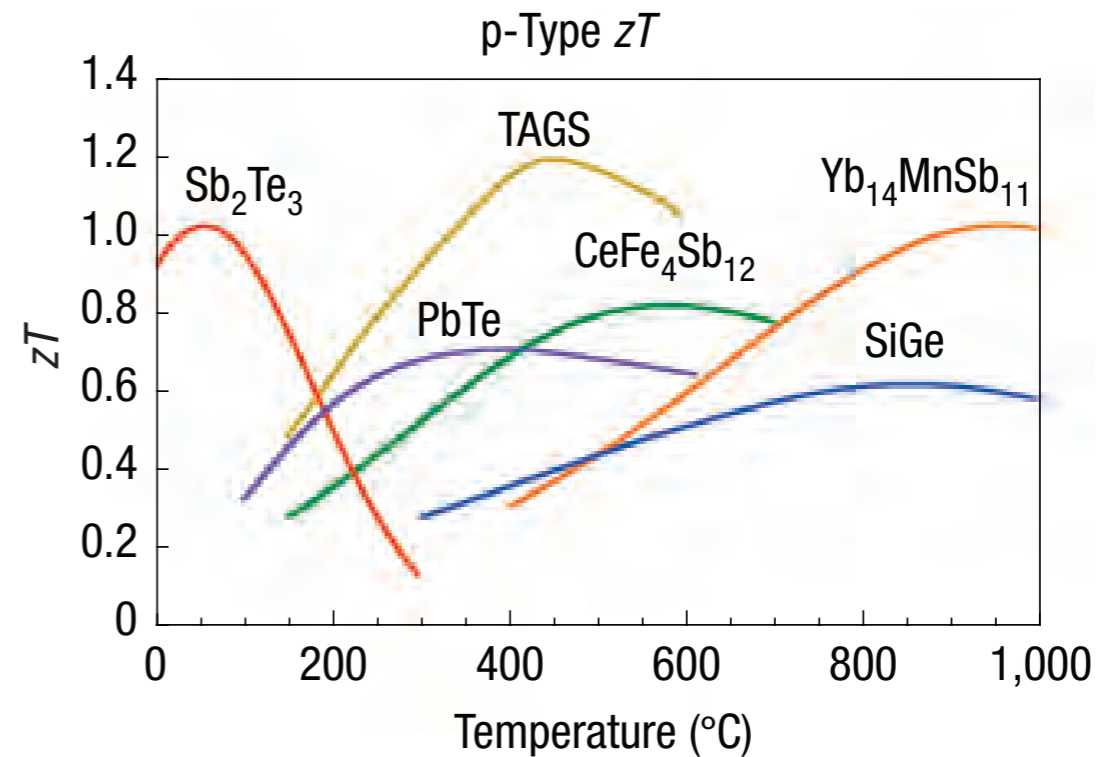
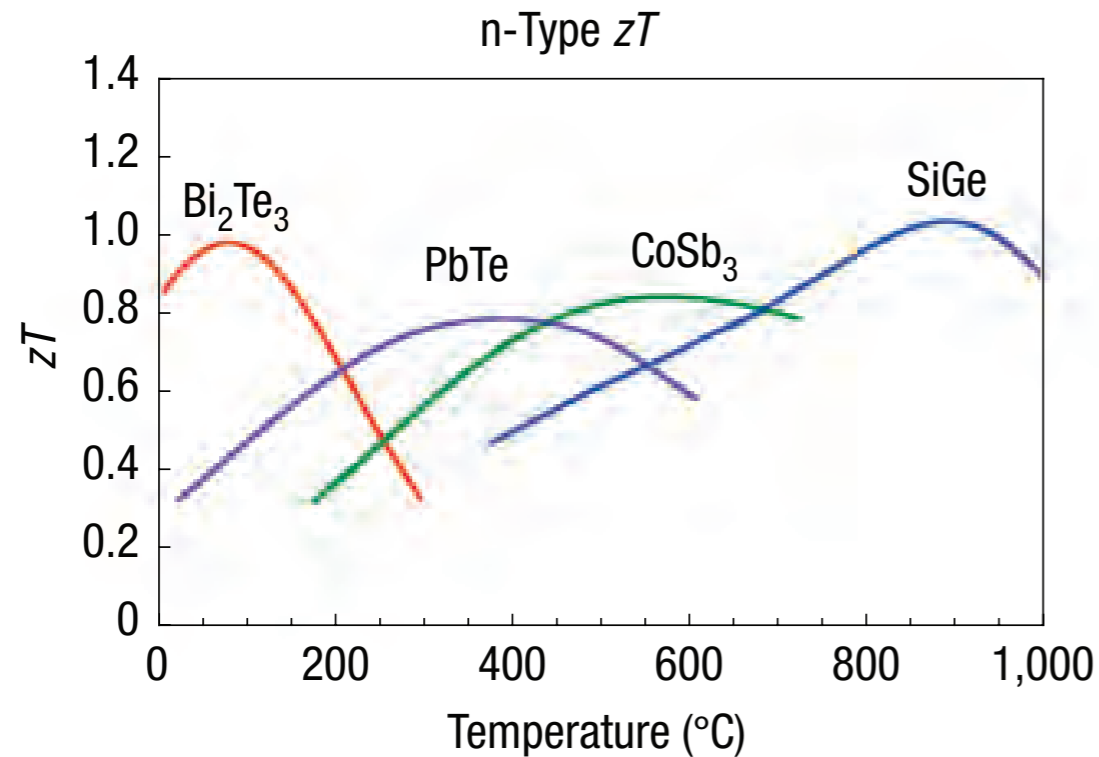
Si SETs & Electrometers



Ge SPADs & Si Quantum Photonics



SiGe Thermoelectrics

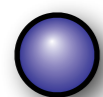
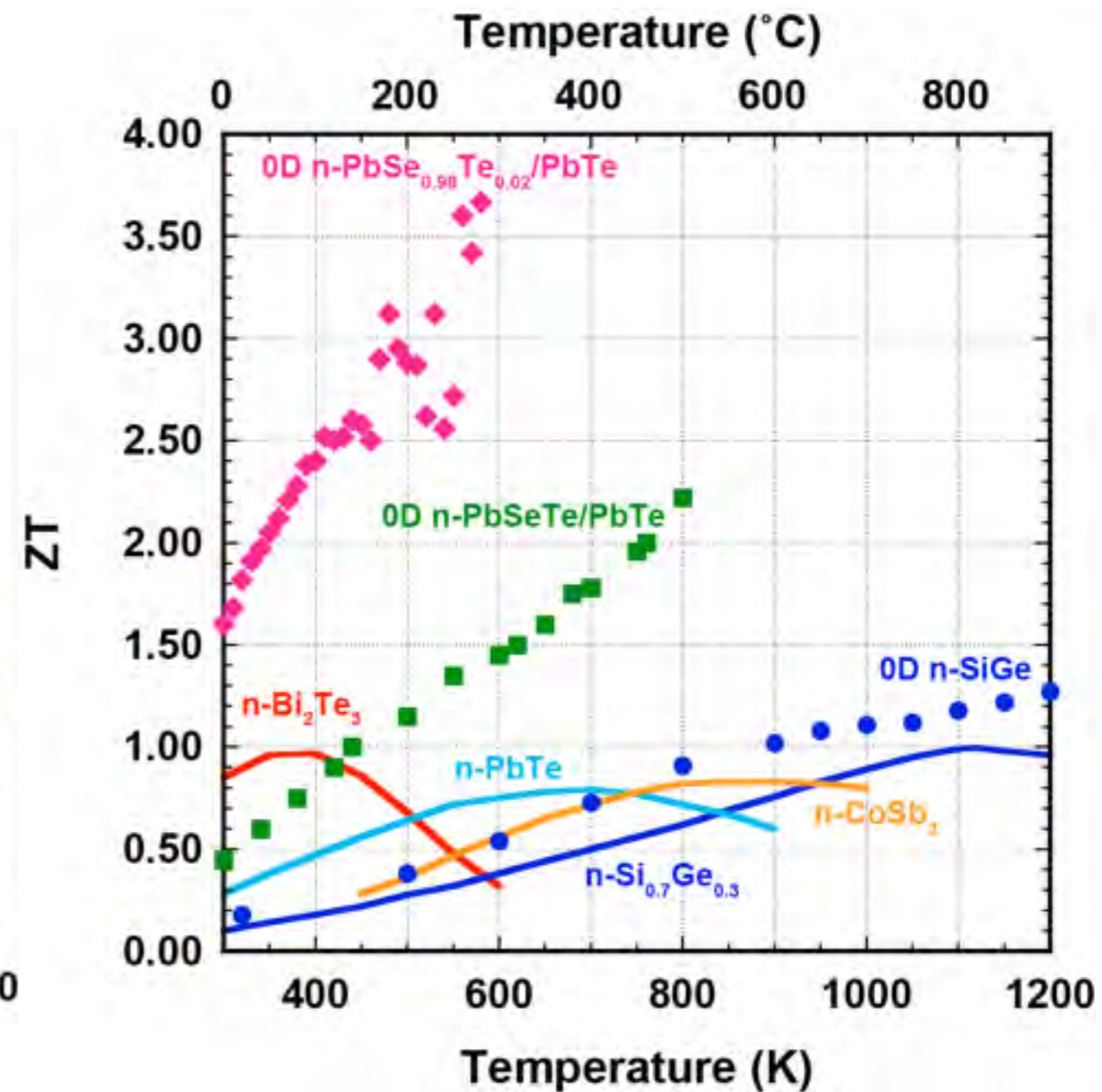
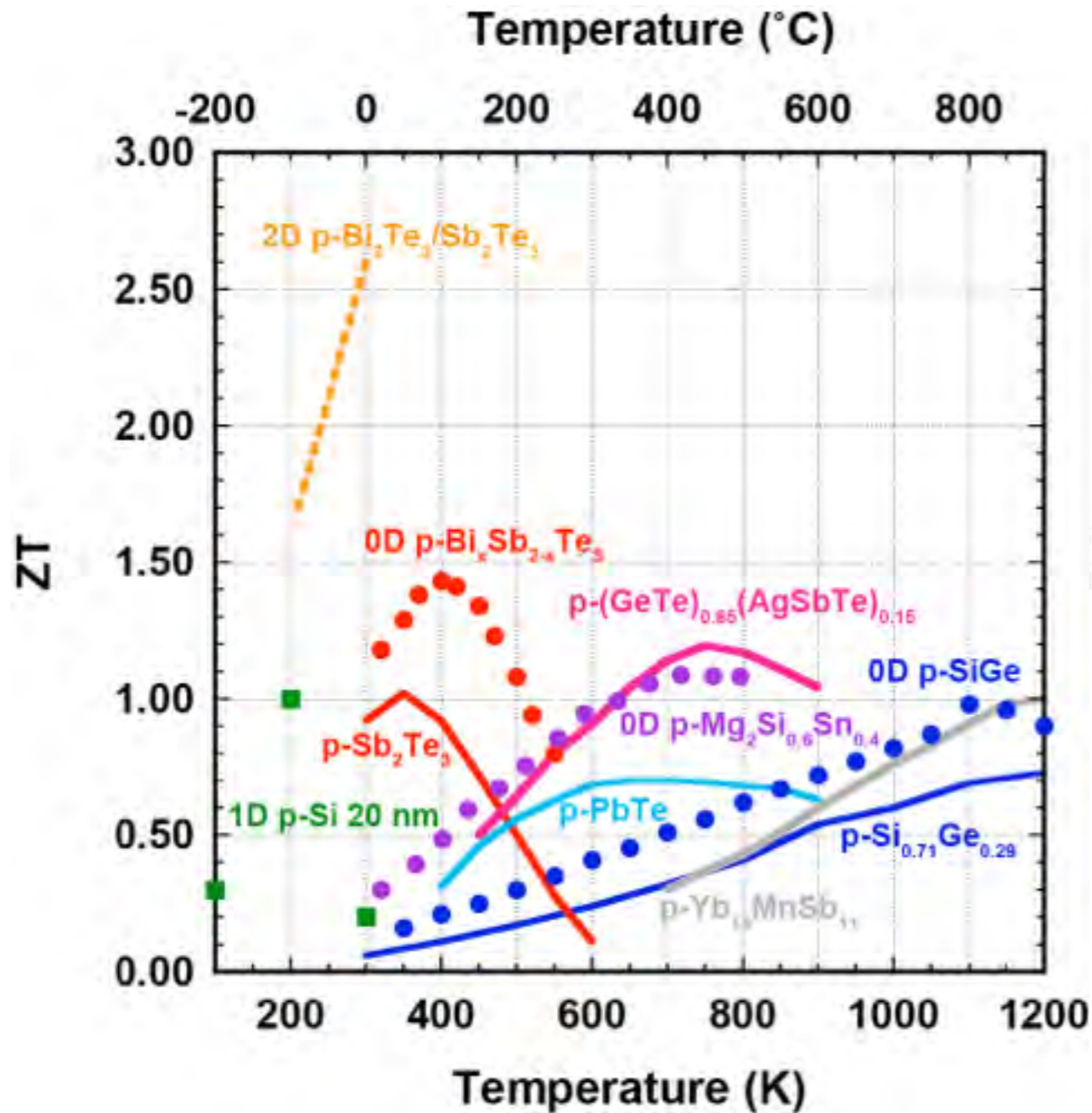


Nature Materials 7, 105 (2008)

- **Bulk n- Bi_2Te_3 and p- Sb_2Te_3 used in most commercial thermoelectrics & Peltier coolers**
- **But tellurium is 9th rarest element on earth !!!**
- **Bulk $Si_{1-x}Ge_x$ ($x \sim 0.2$ to 0.3) used for high temperature satellite applications**

p-type

n-type

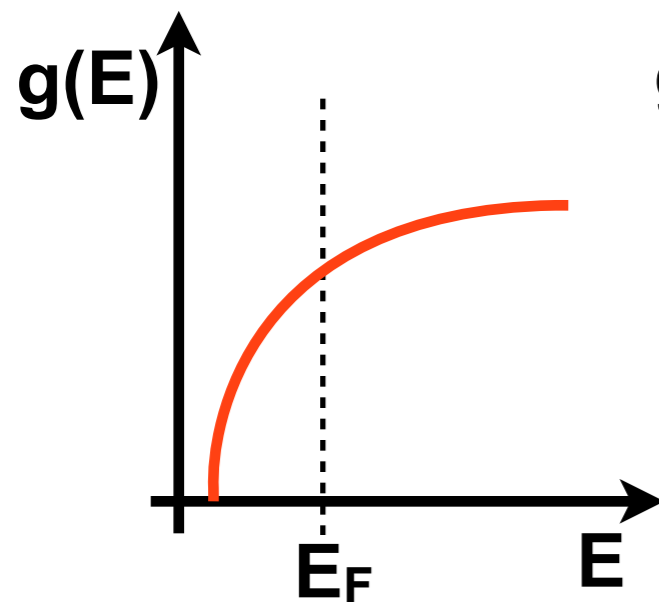


Nanostructures can improve Seebeck coefficient and/or decrease thermal conductivity

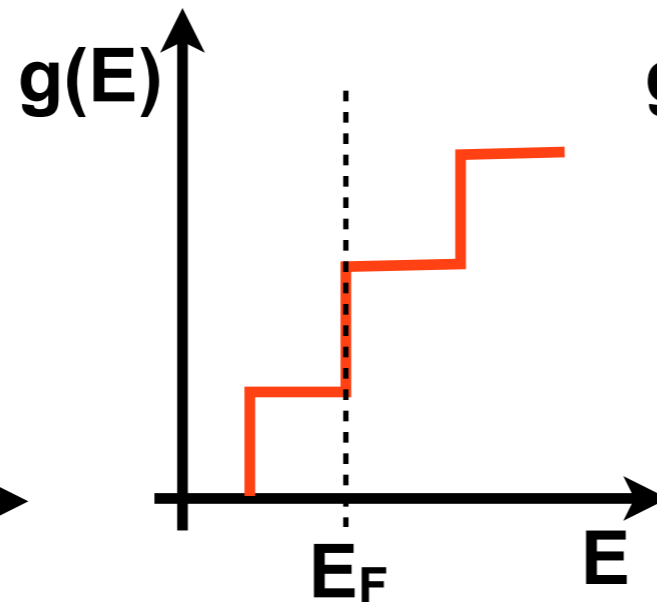
- Increase α through enhanced DOS:

$$\alpha = -\frac{\pi^2}{3q} k_B^2 T \left[\frac{d \ln(\mu(E)g(E))}{dE} \right]_{E=E_F}$$

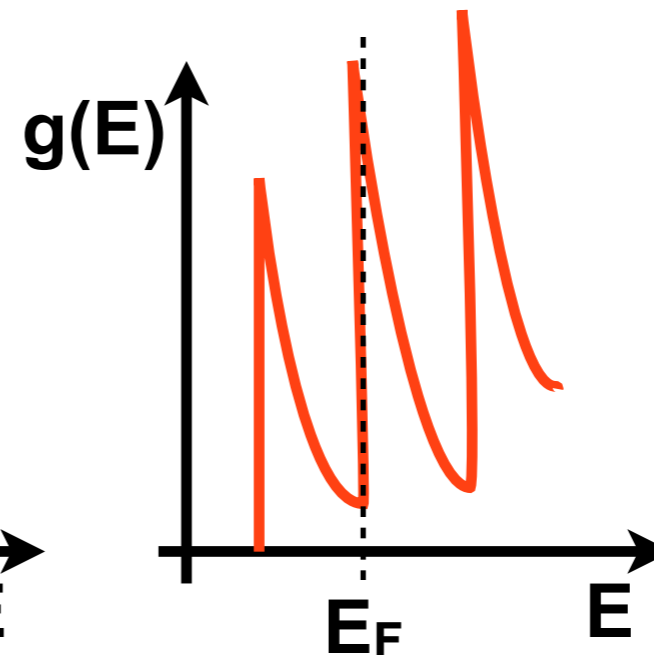
3D
bulk



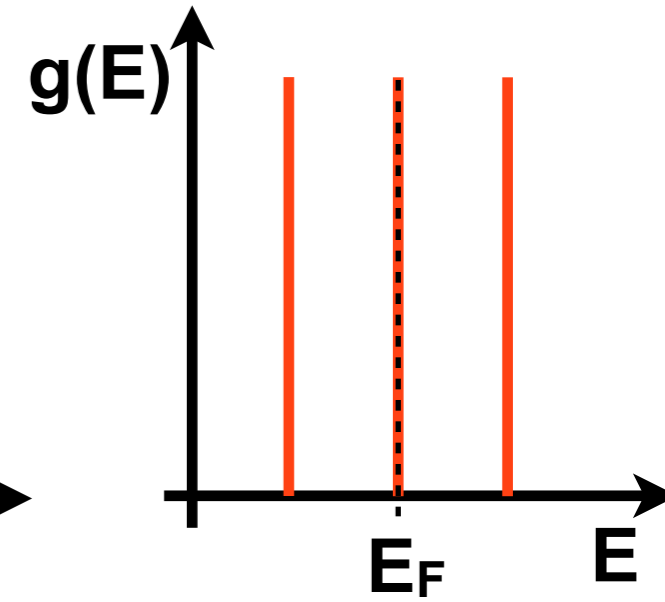
2D
quantum well



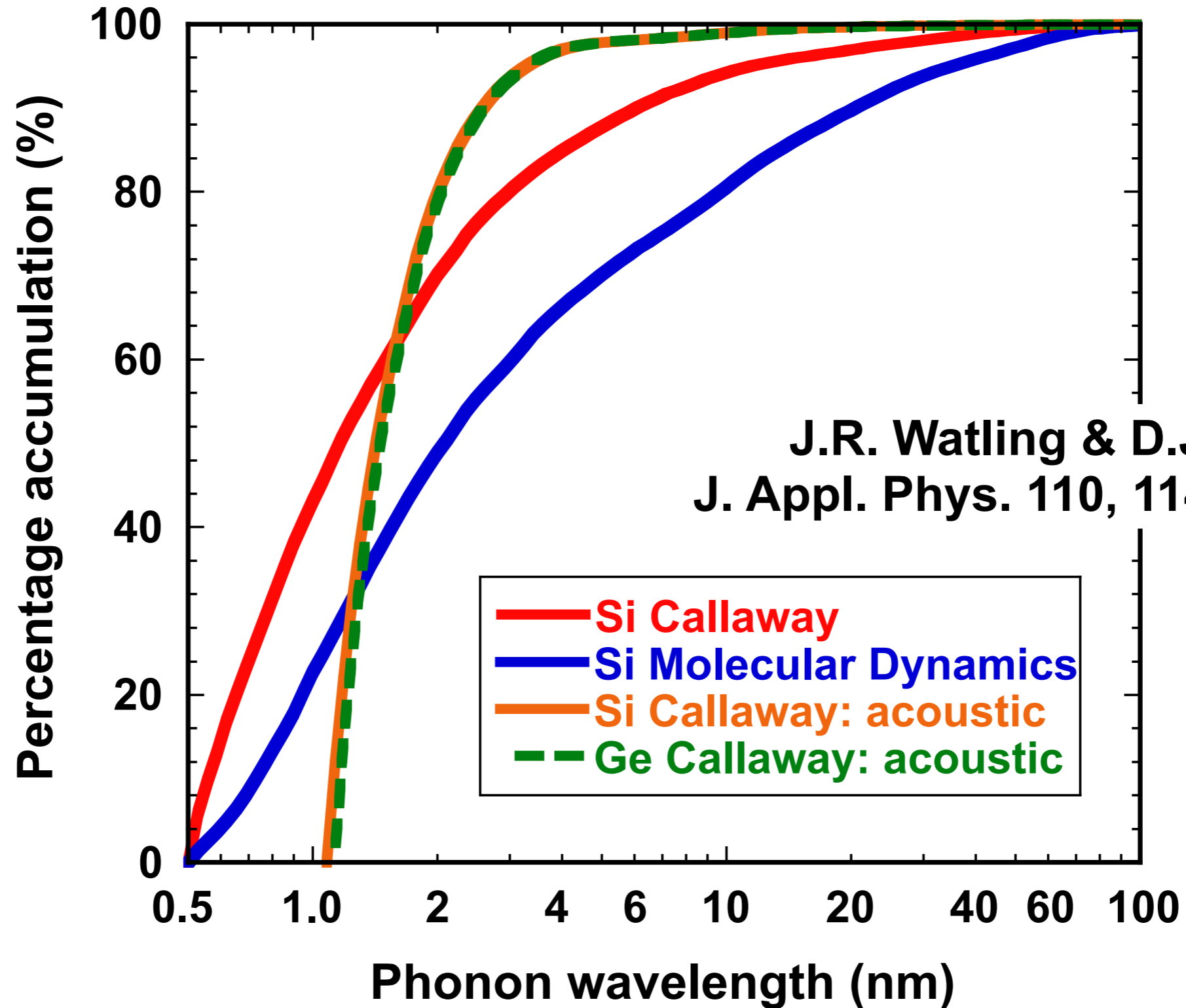
1D
quantum wire



0D
quantum dot



————— α increasing —————>

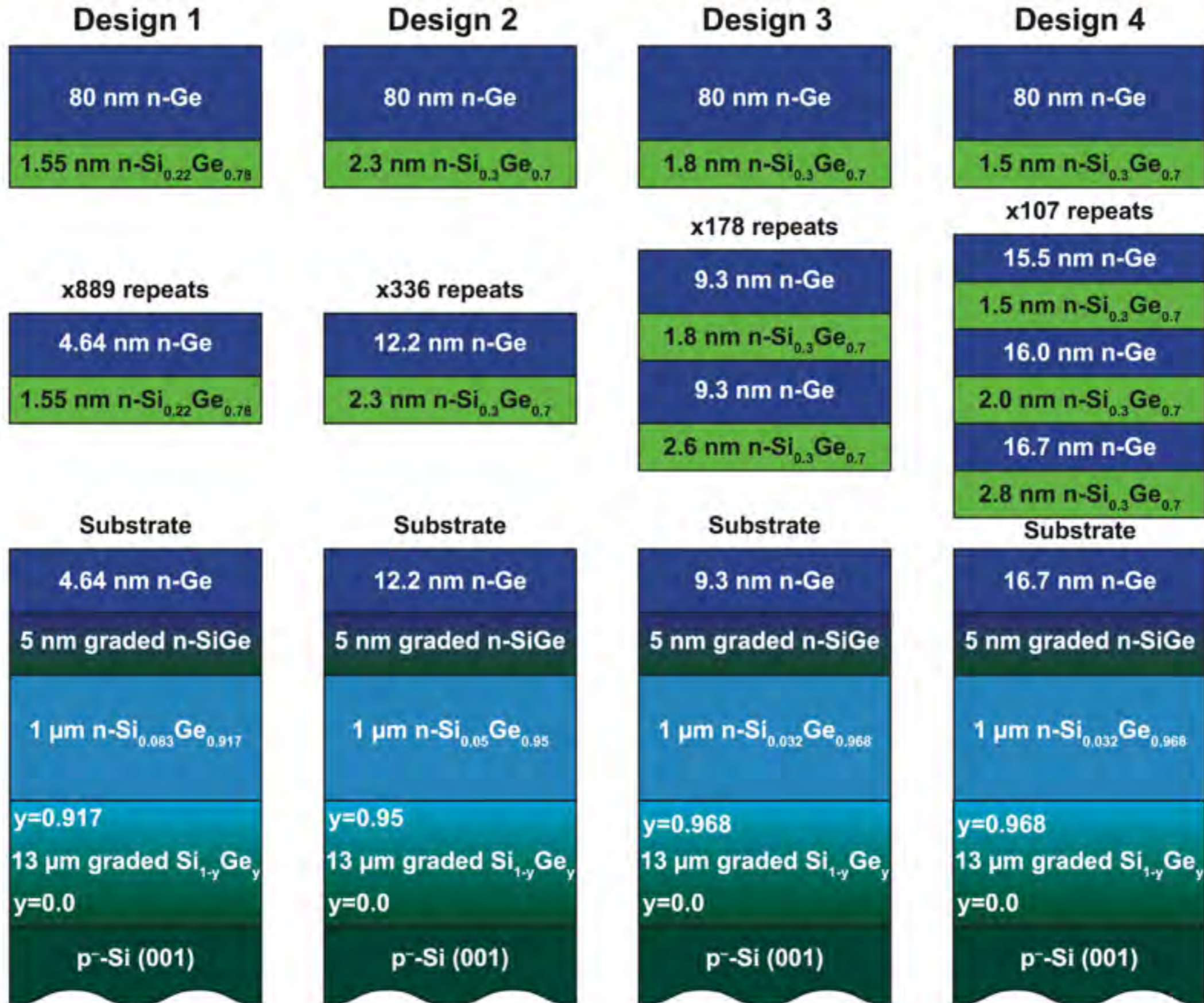


J.R. Watling & D.J. Paul,
J. Appl. Phys. 110, 114508 (2013)

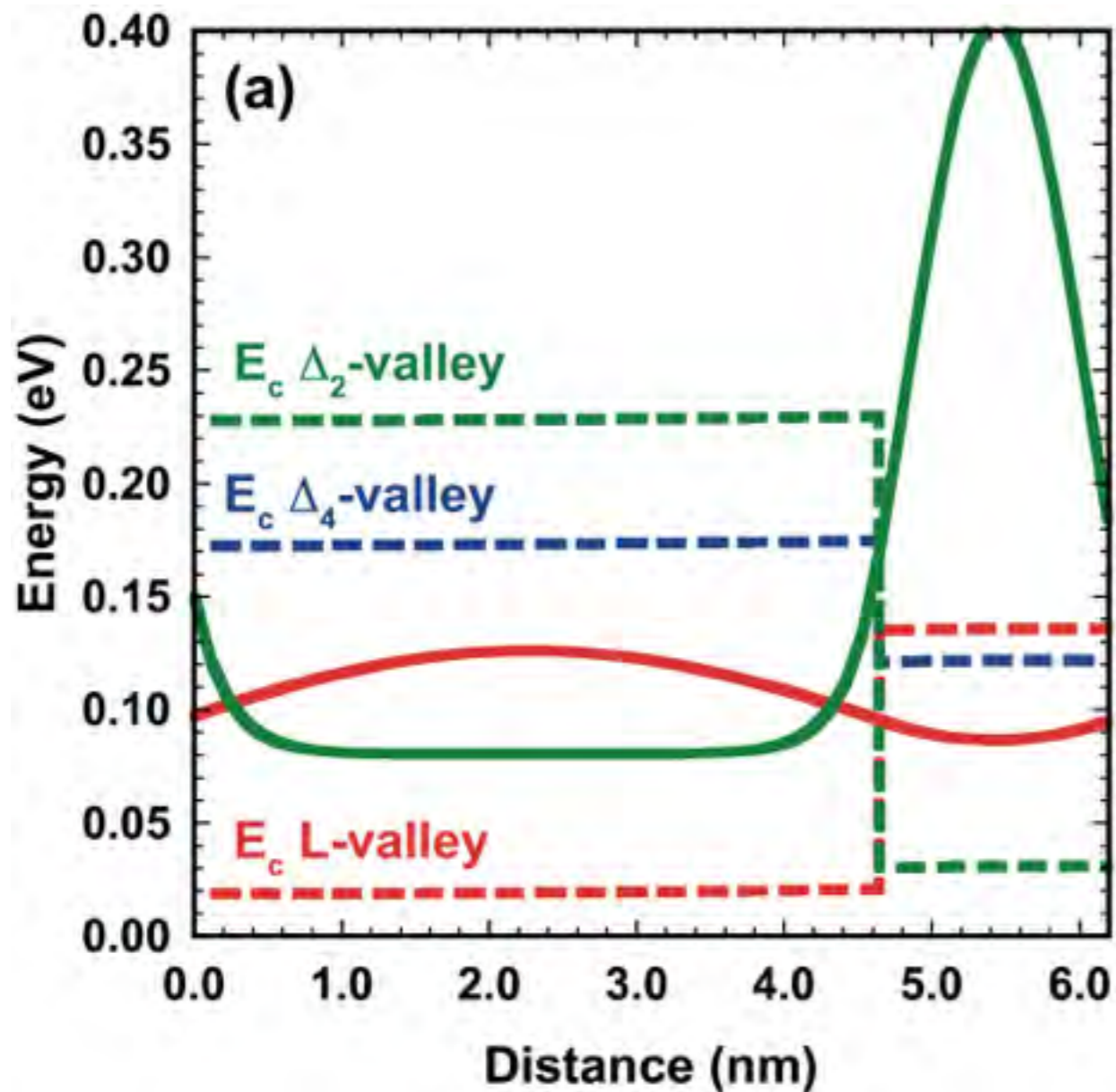
— Si Callaway
— Si Molecular Dynamics
— Si Callaway: acoustic
- - Ge Callaway: acoustic



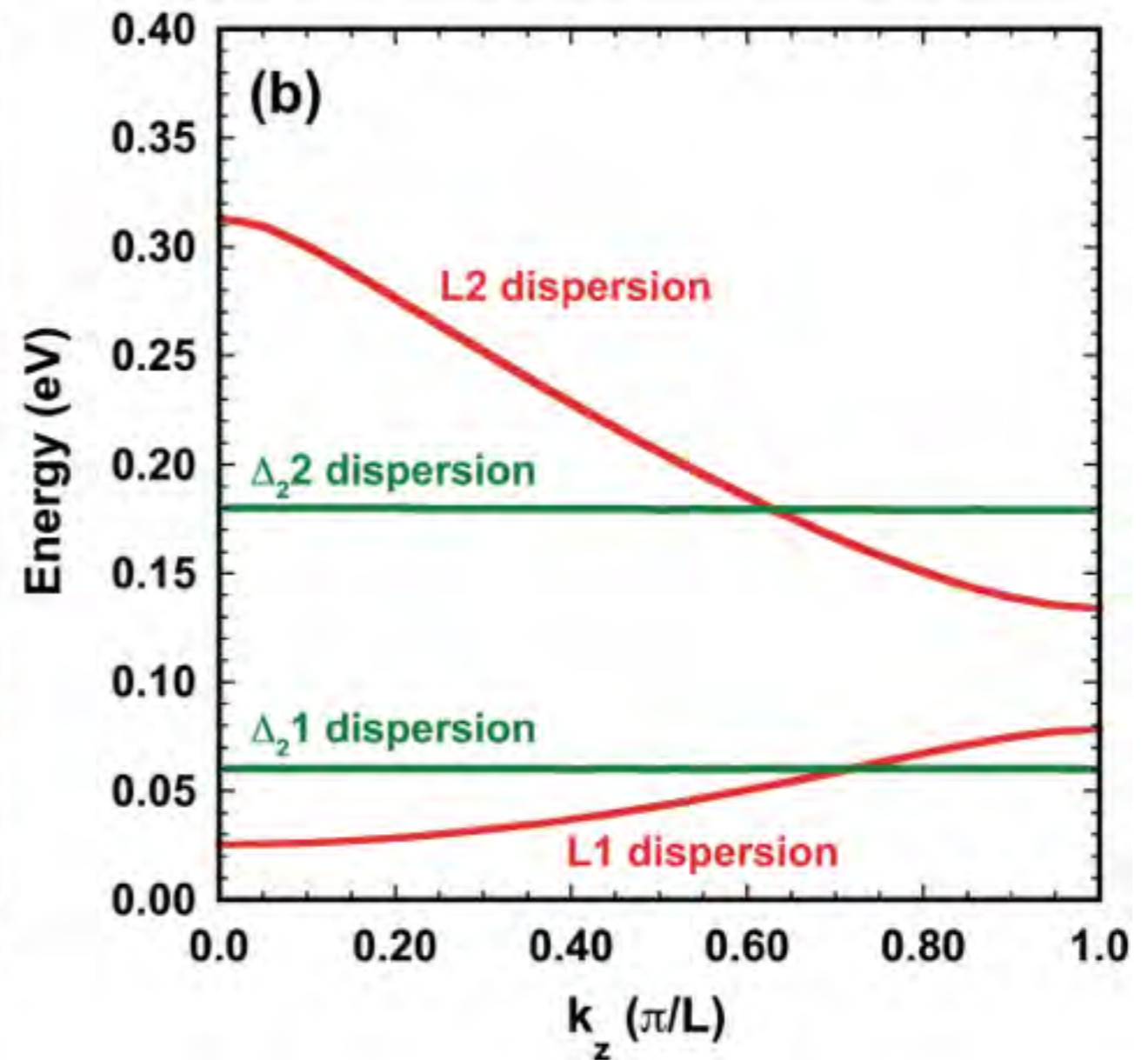
Key wavelengths for scattering phonons 1.2 to 4 nm



Conduction bands

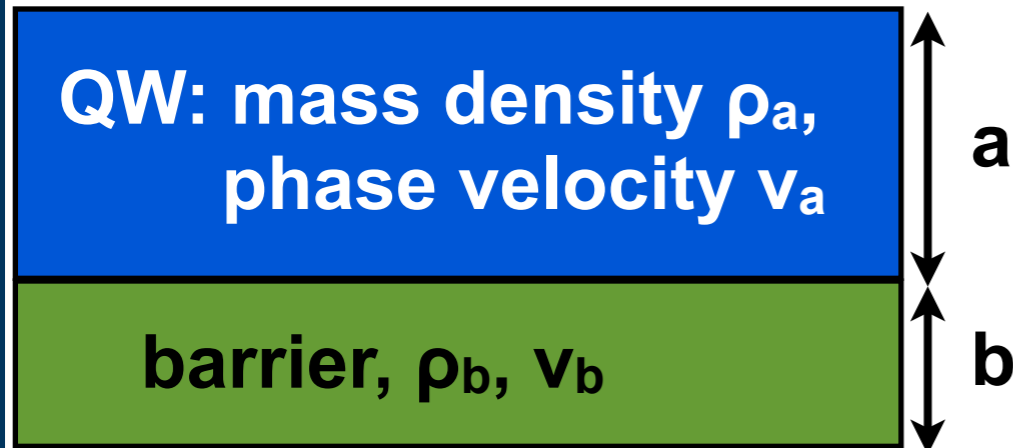


Miniband dispersions



Only L-valley electrons form minibands

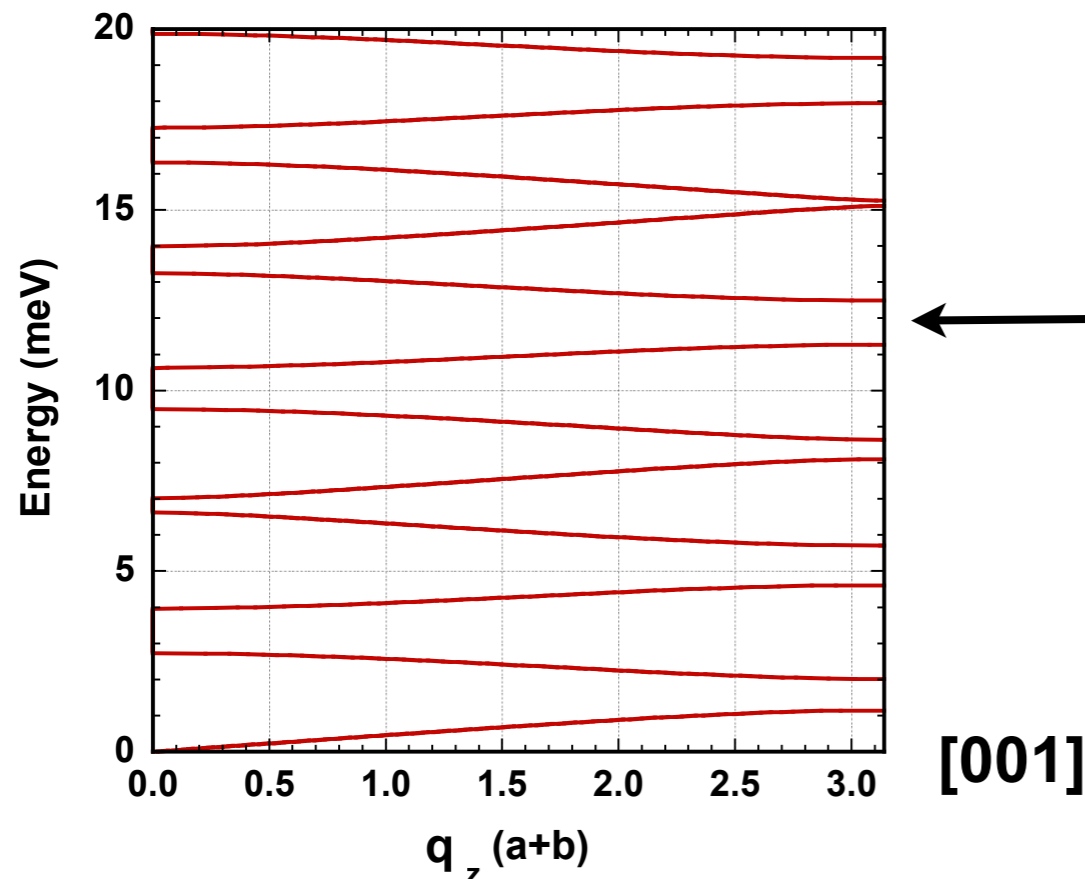
Superlattice $N \rightarrow \infty$



Acoustic mismatch: $\eta = \frac{\rho_b v_b}{\rho_a v_a}$

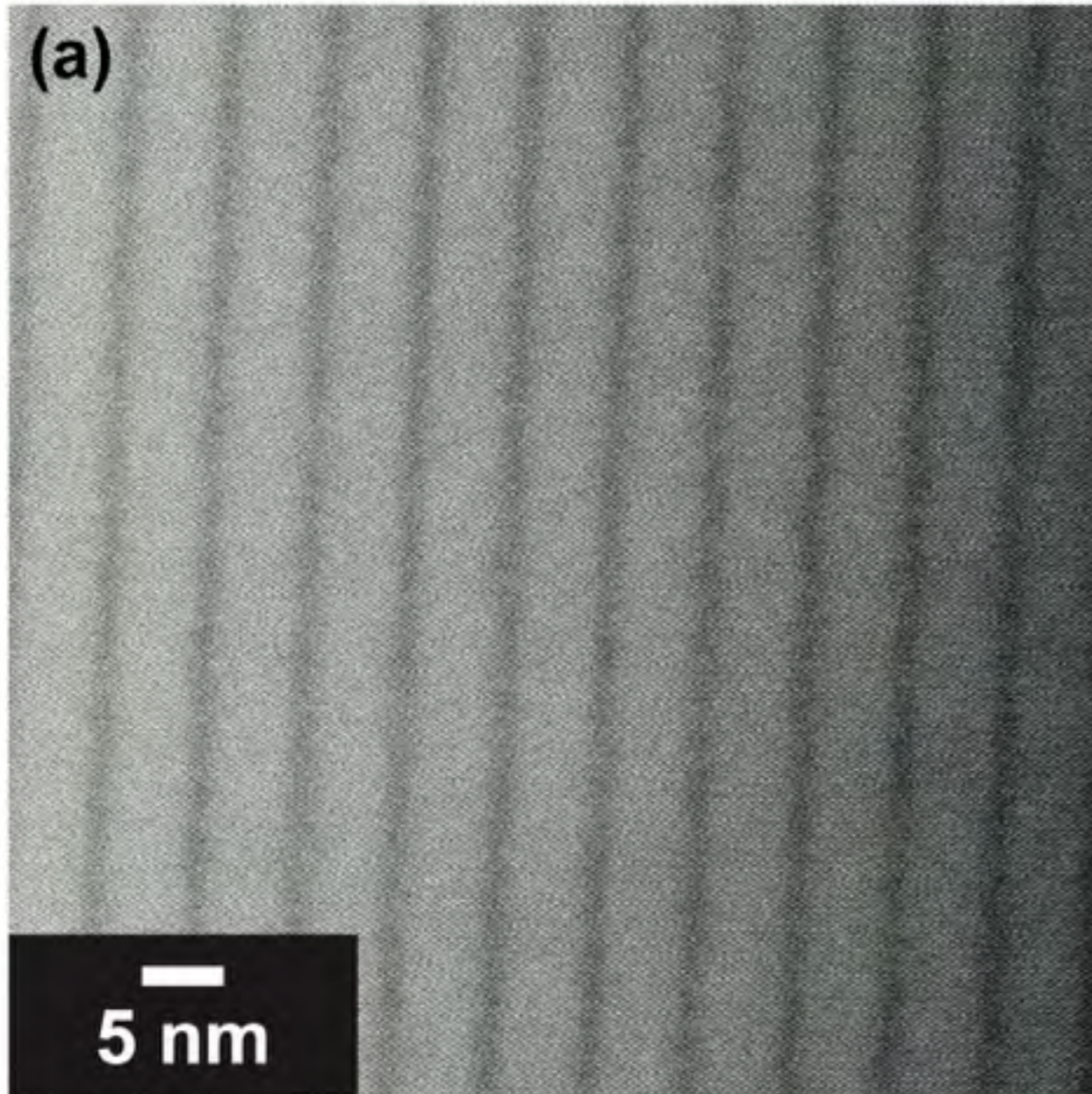
Superlattice zone boundaries: $q_z = \frac{n\pi}{a+b}$

$$\cos q_z (a+b) = \cos q_a a \cos q_b b - \left[\frac{1 + \eta^2}{2\eta} \right] \sin q_a a \sin q_b b$$

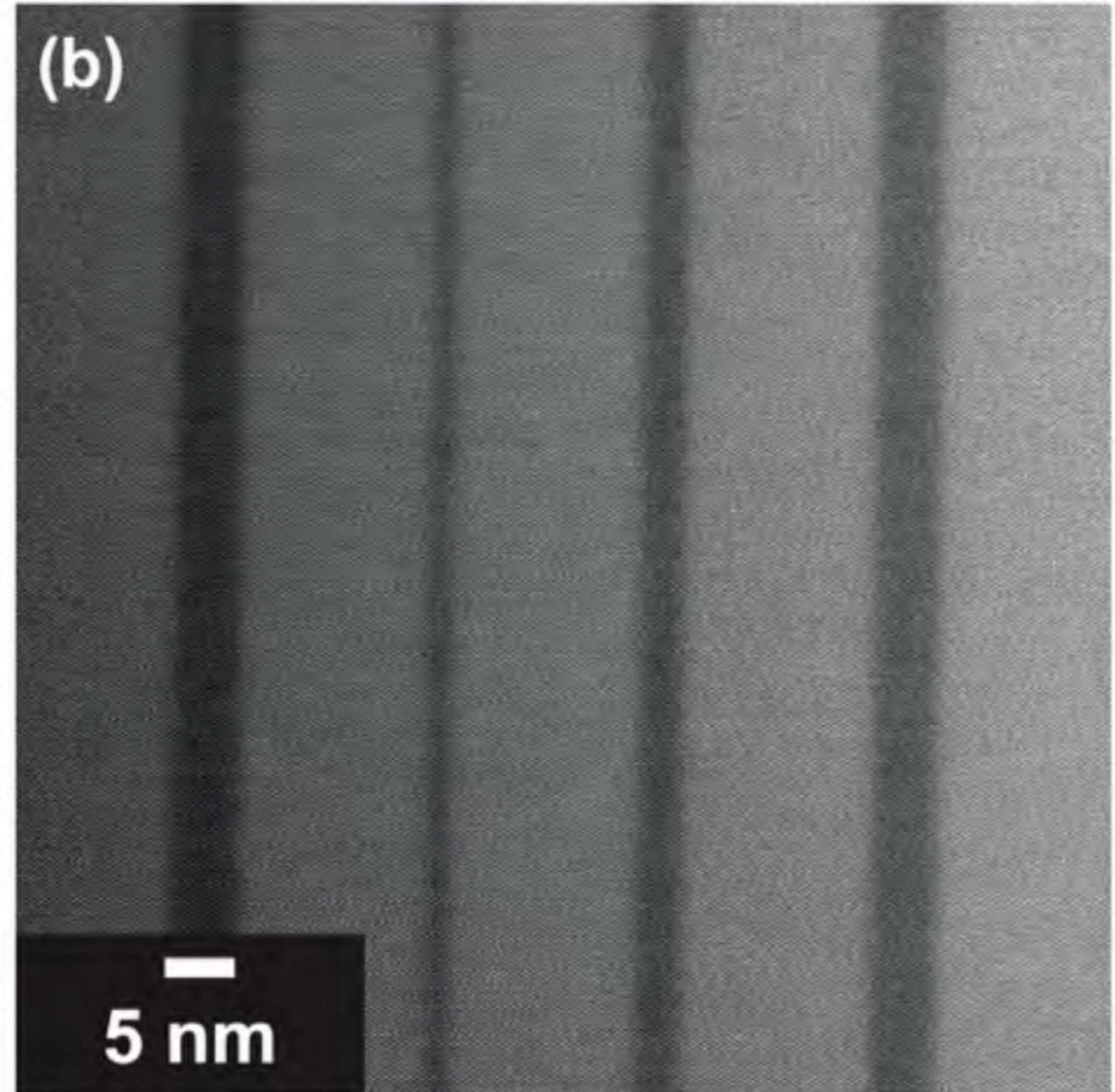


← acoustic phonon bandgap

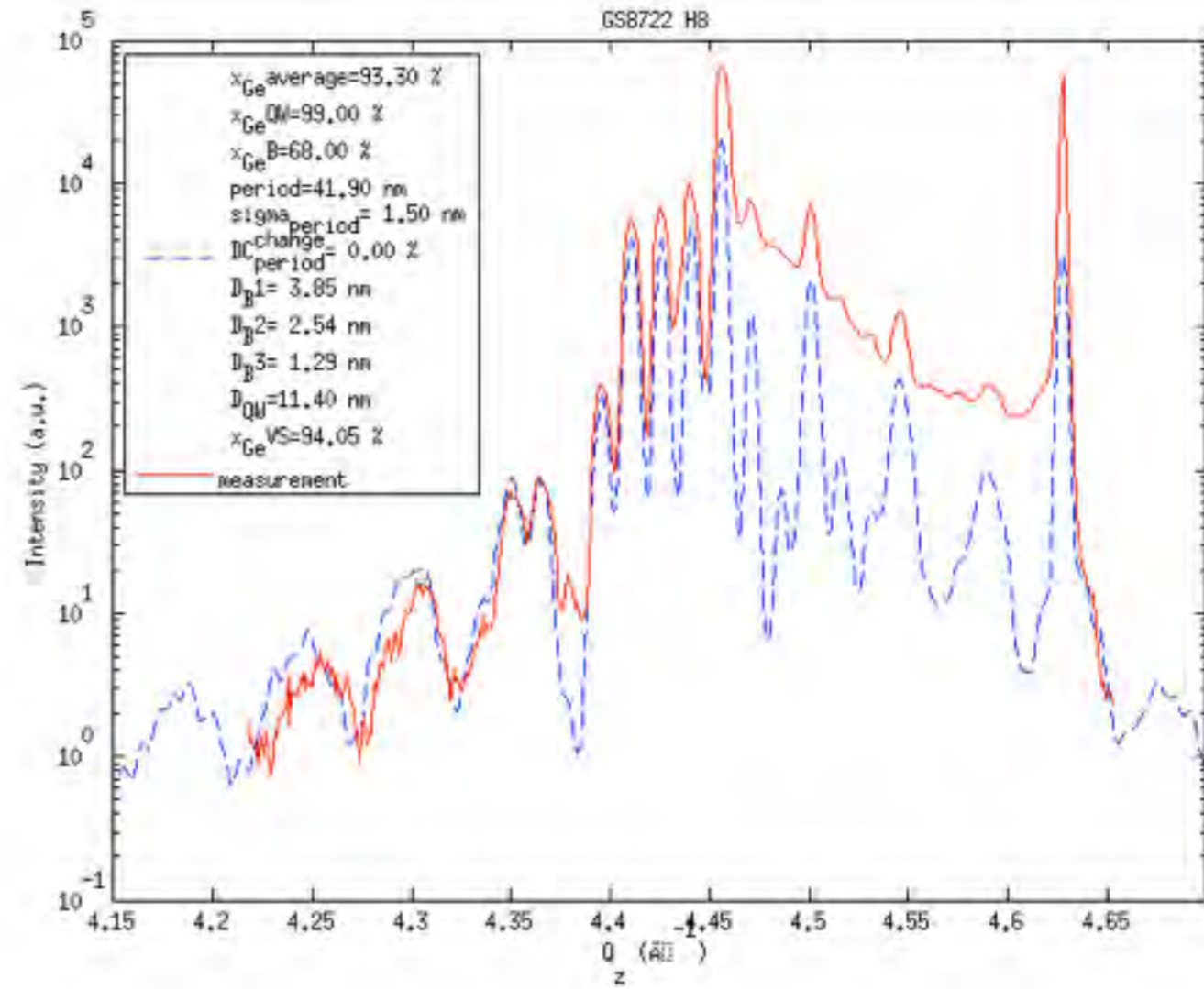
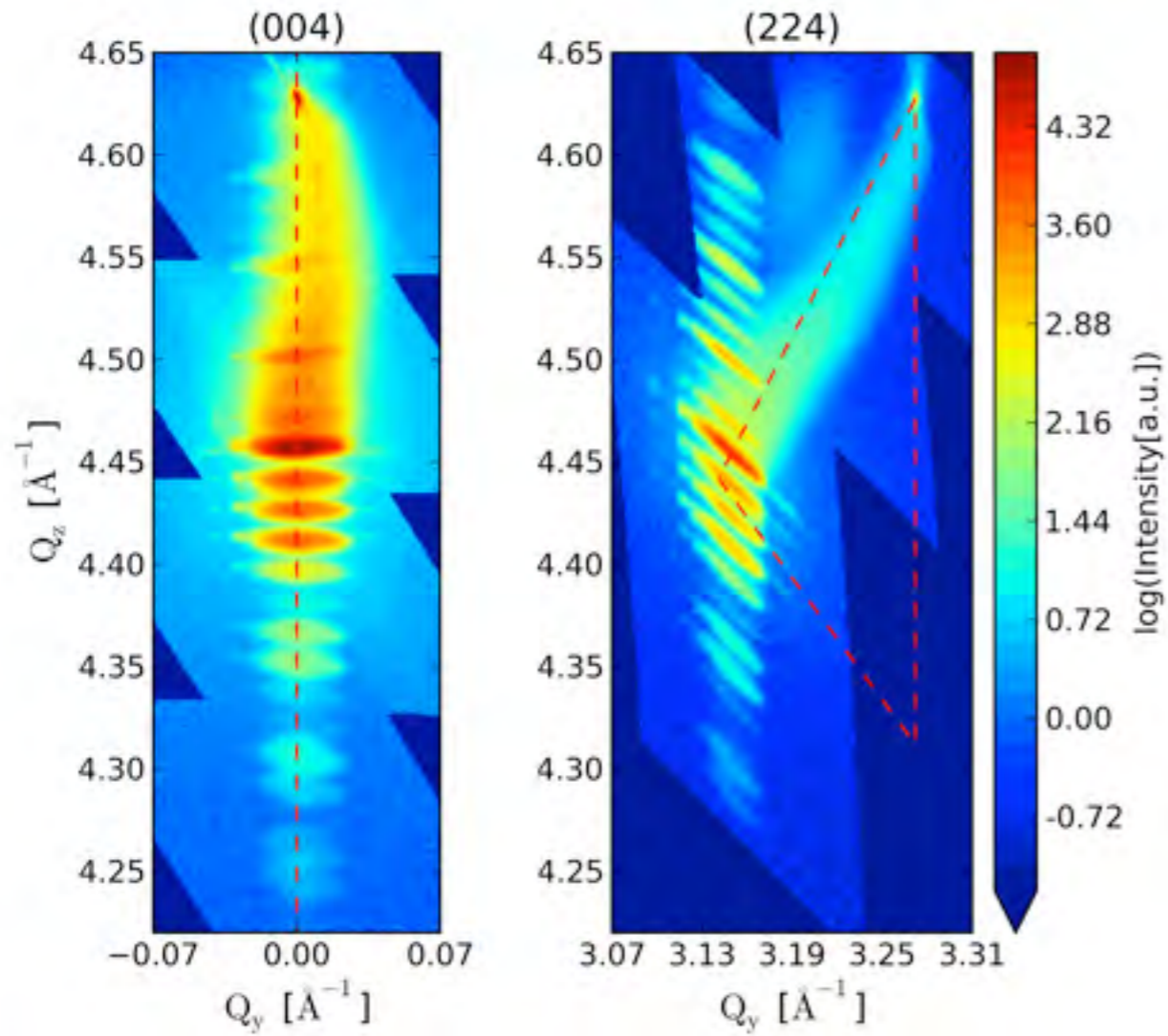
Single barrier

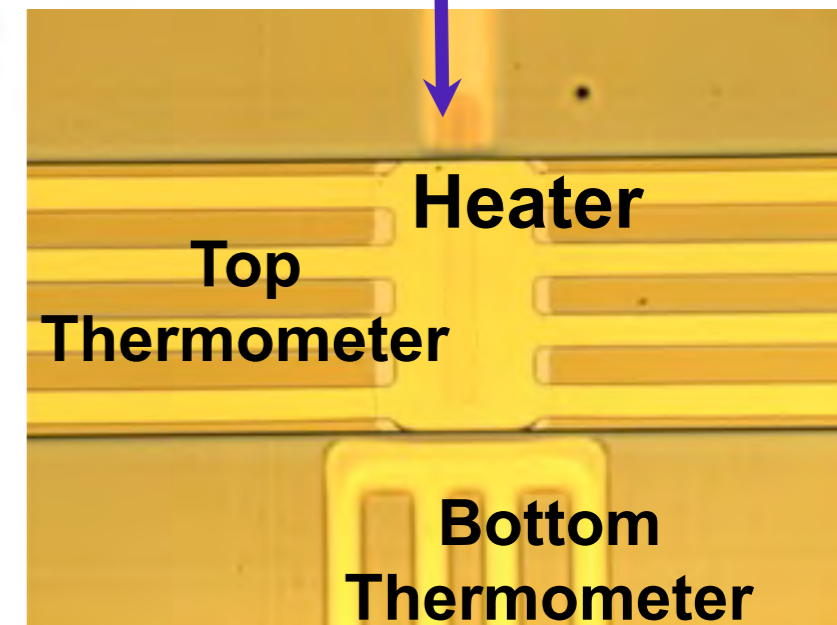
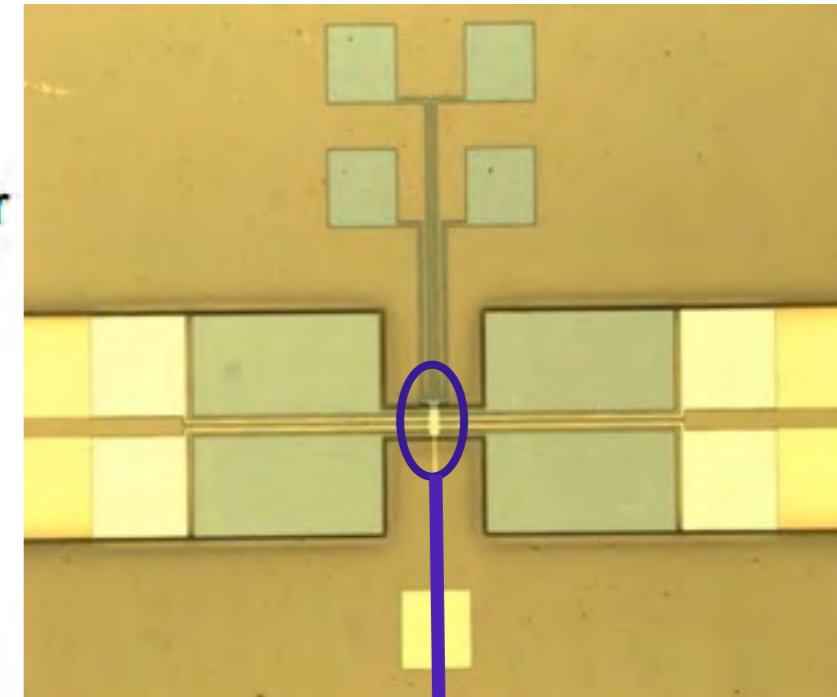
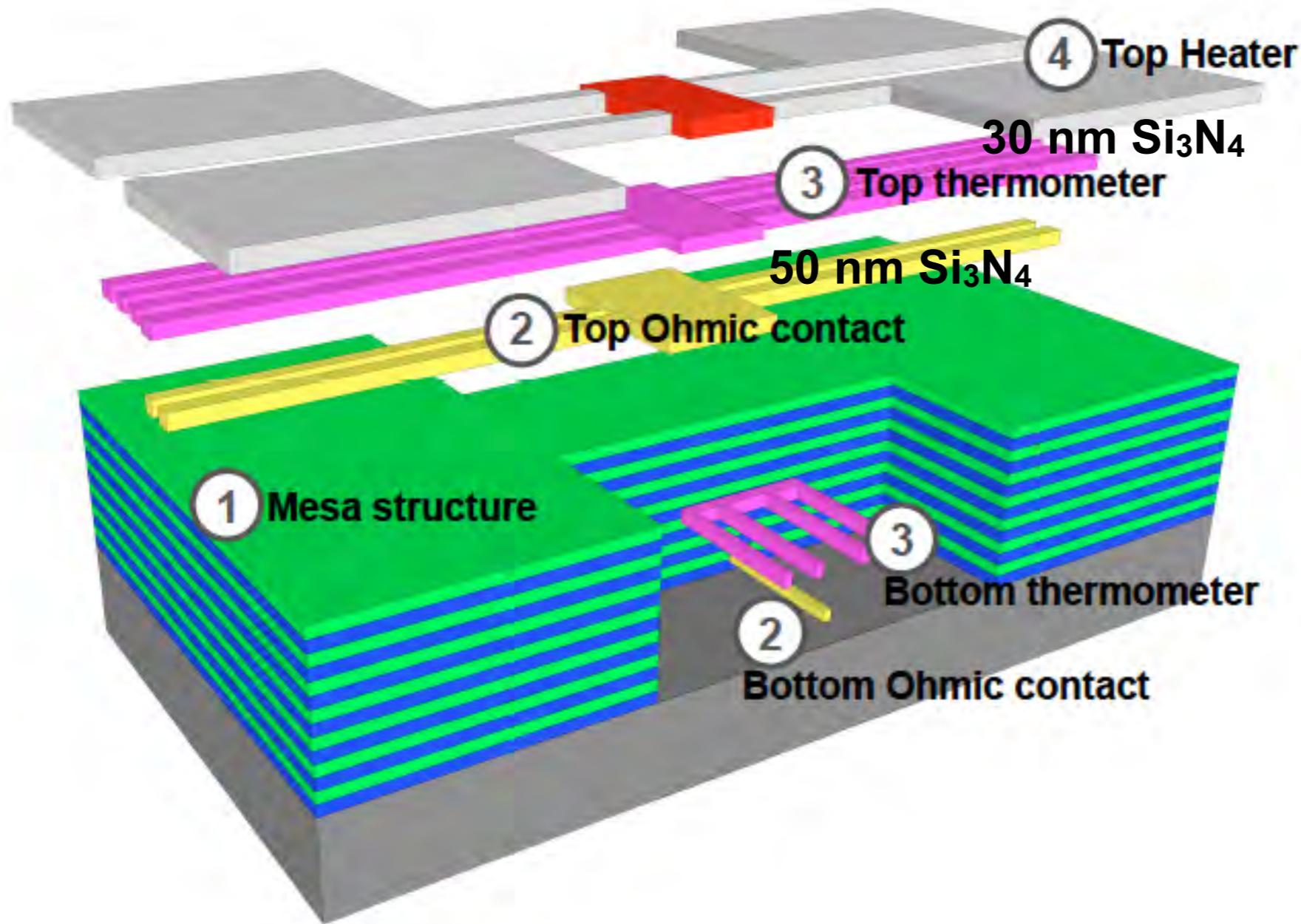


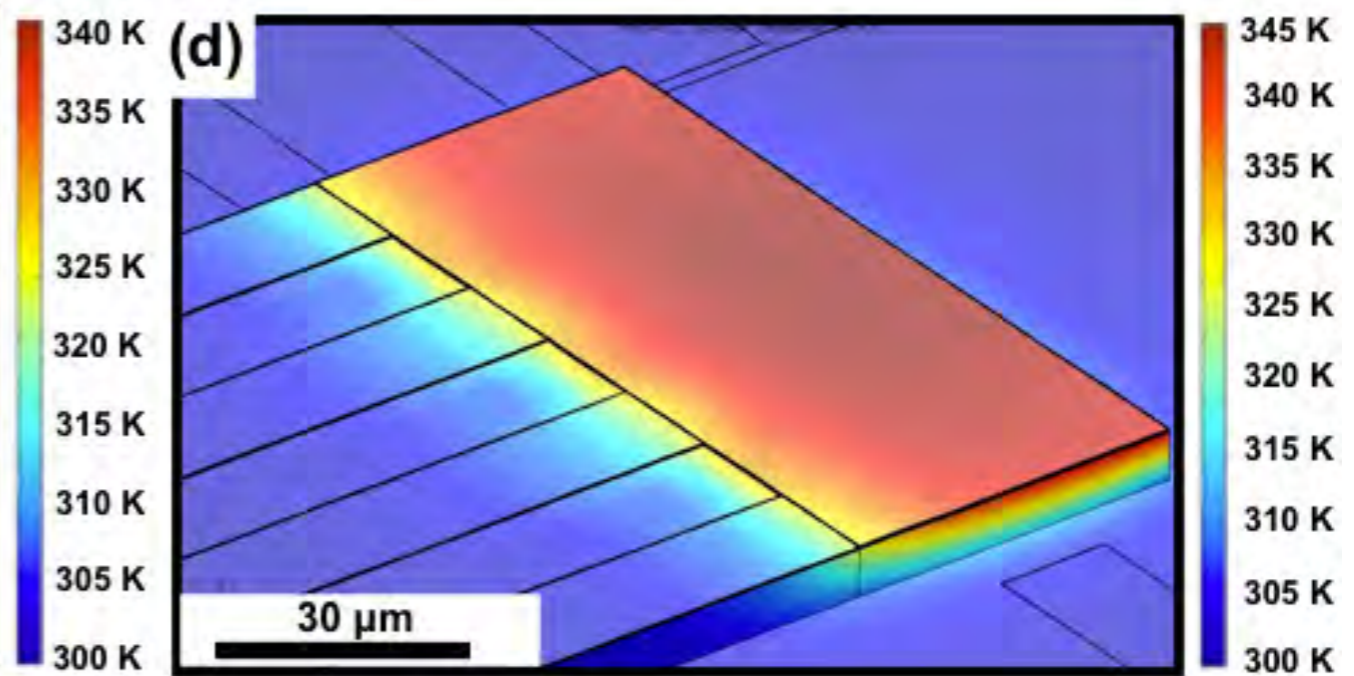
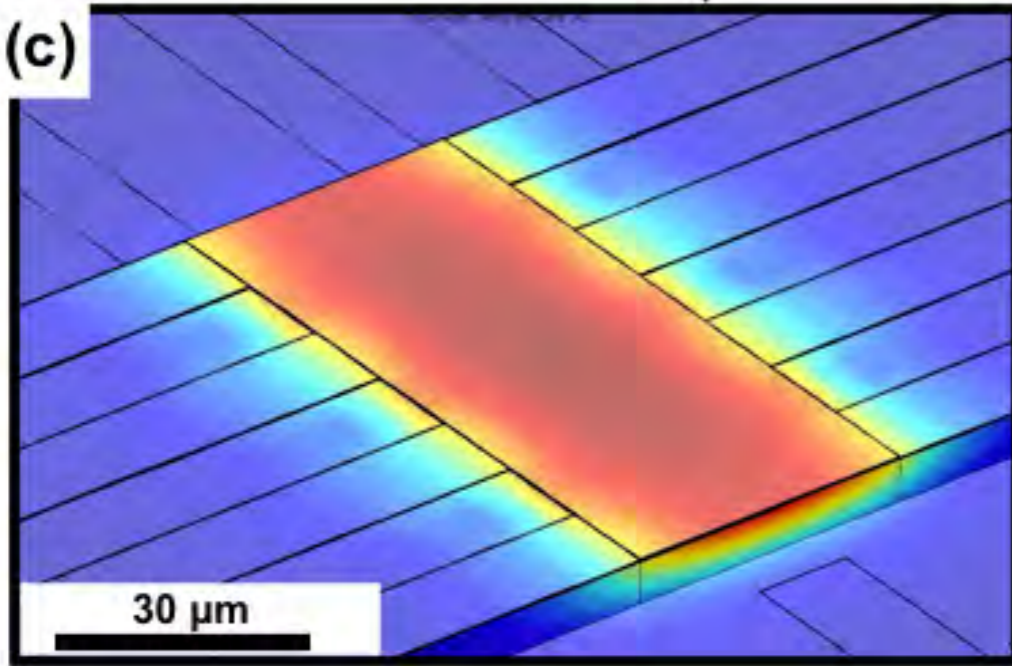
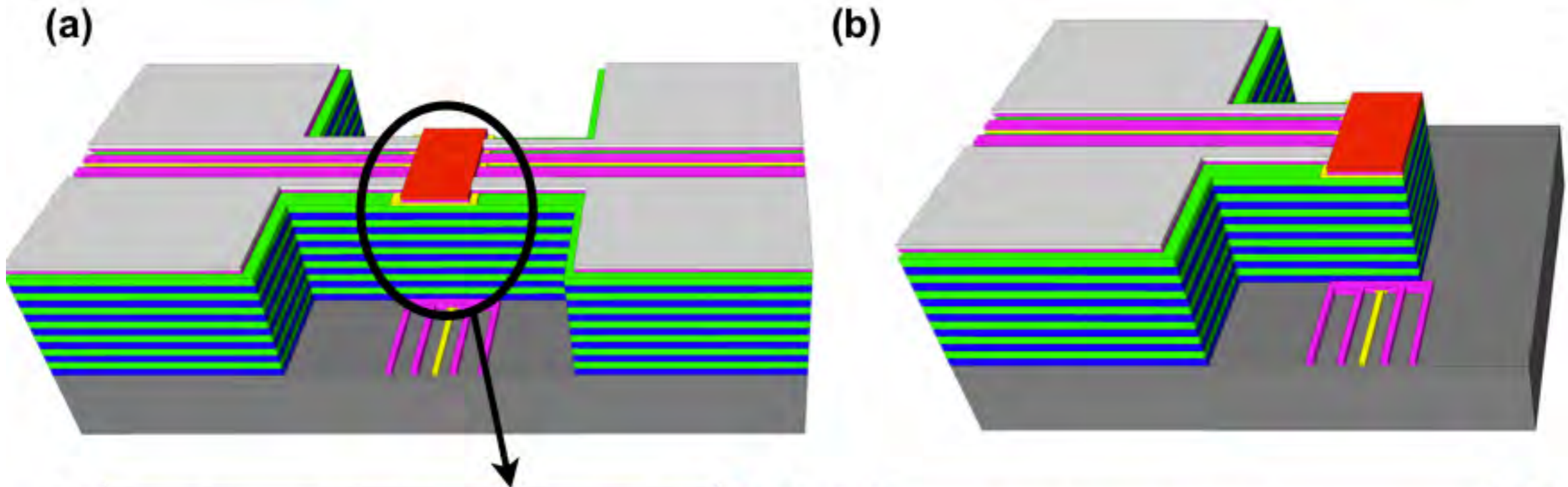
Three barriers

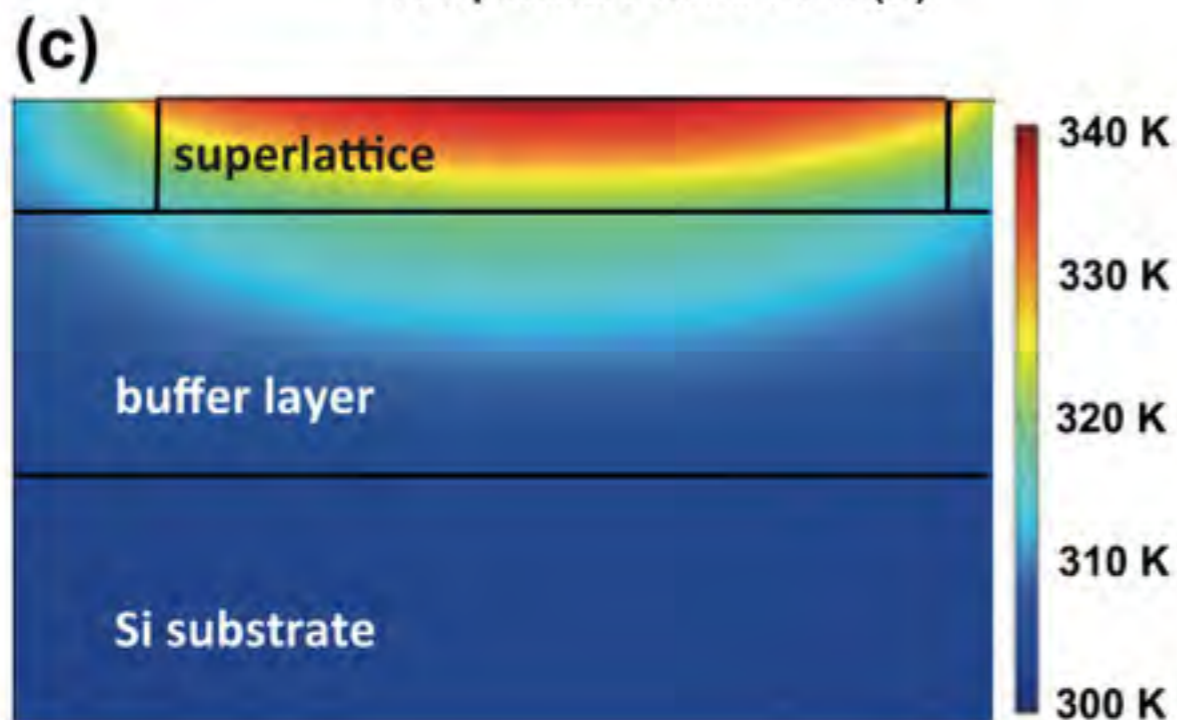
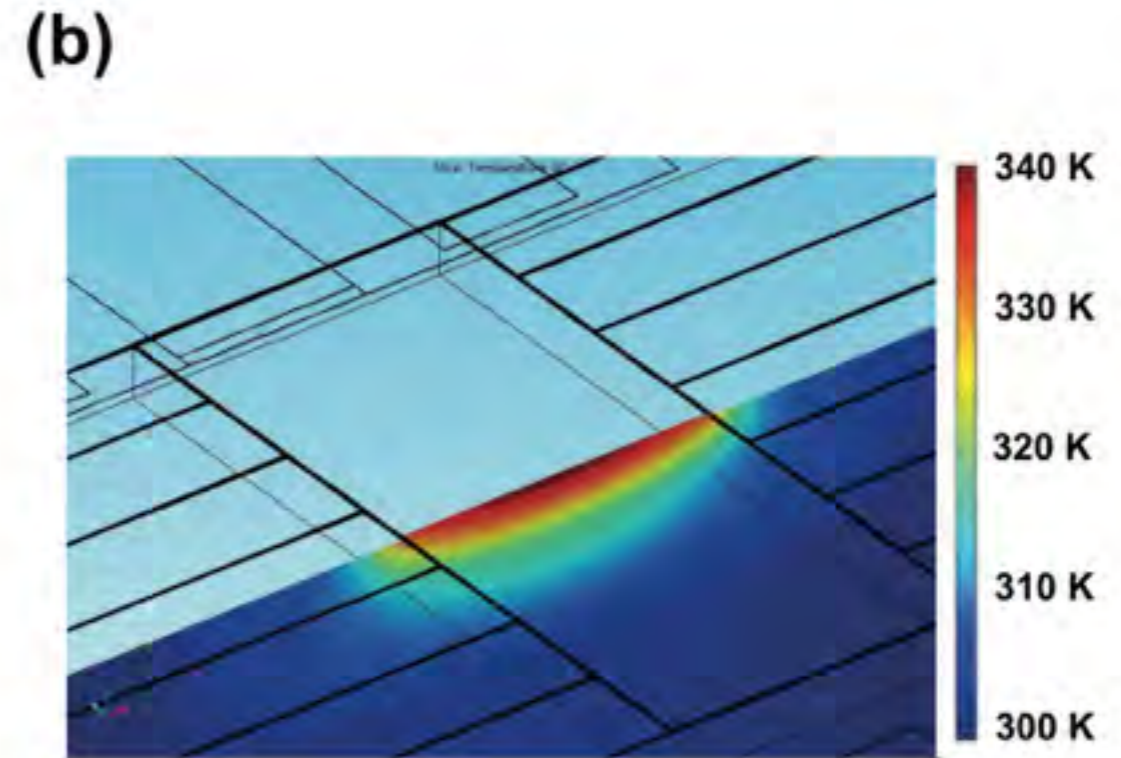
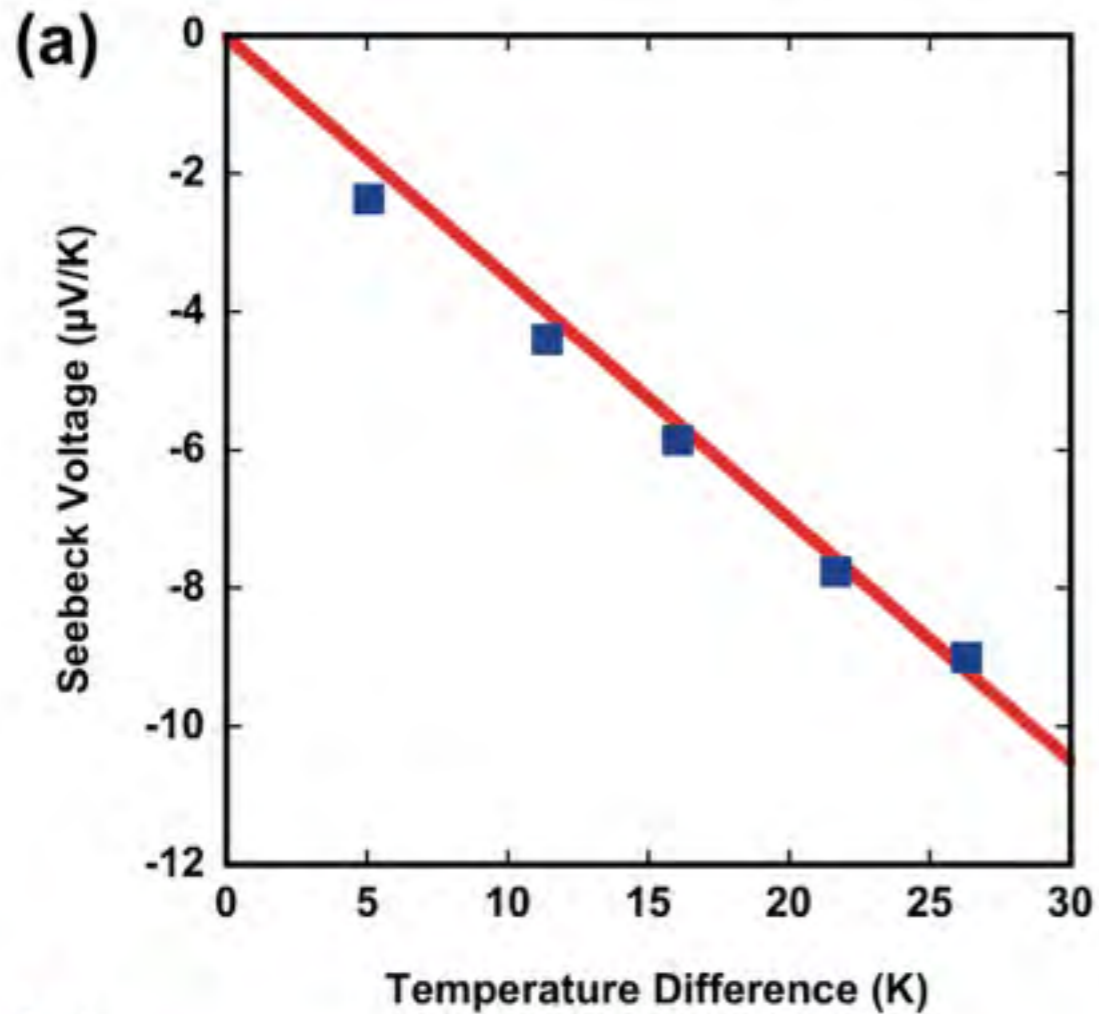


3 barriers with wide Ge QWs

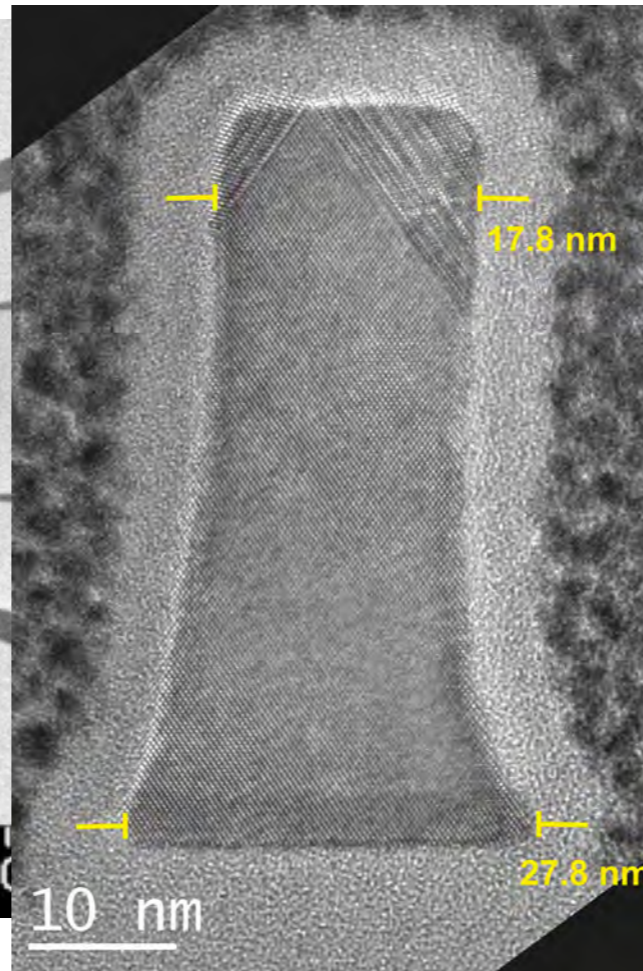
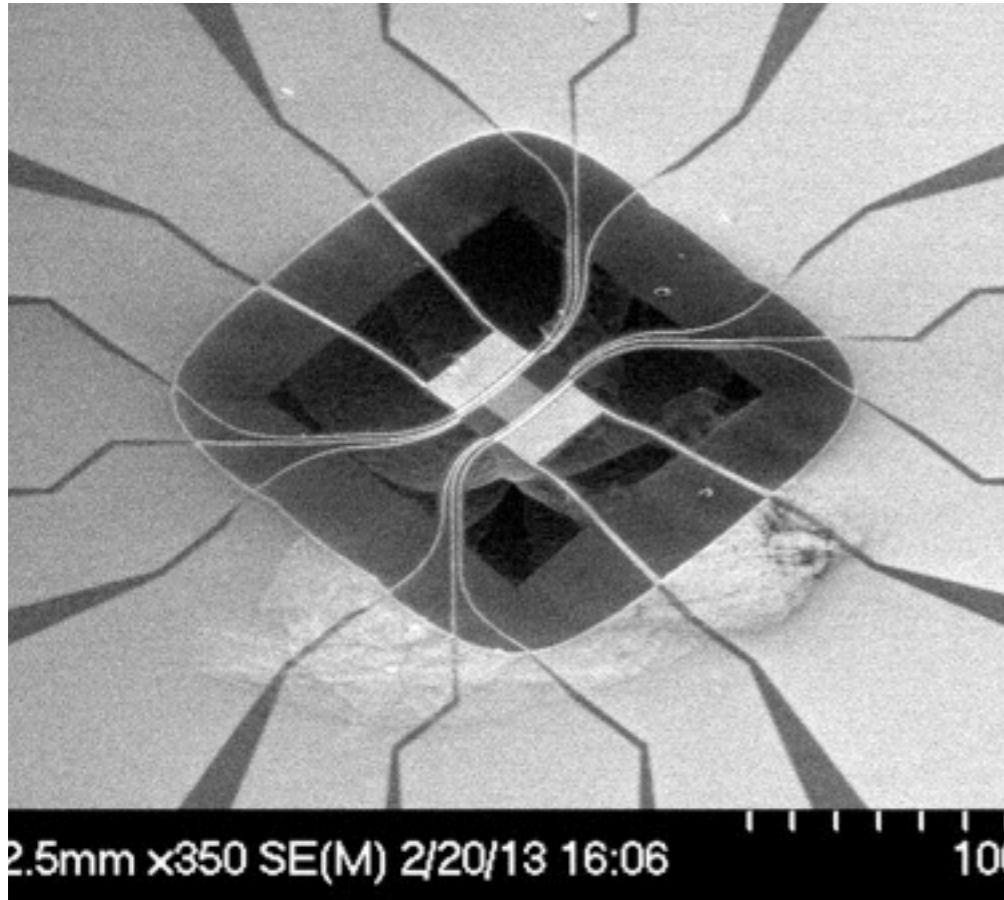








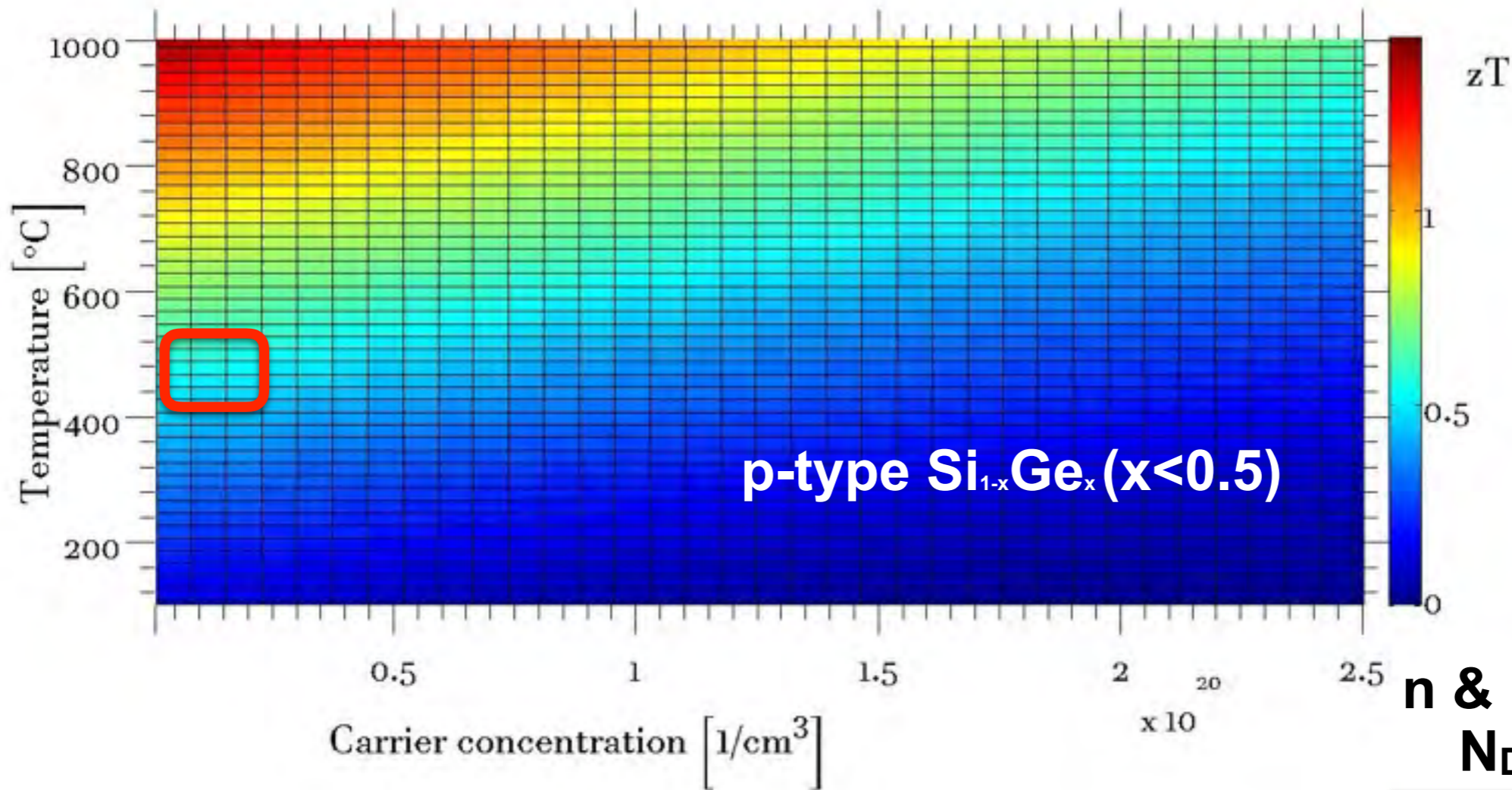
45 nm Wide n-Silicon Nanowires



- $\sigma = 20,300 \text{ S/m}$
4 terminal
- $\kappa = 7.78 \text{ W/mK}$
- $\alpha = -271 \text{ } \mu\text{V/K}$
- $ZT = 0.057$

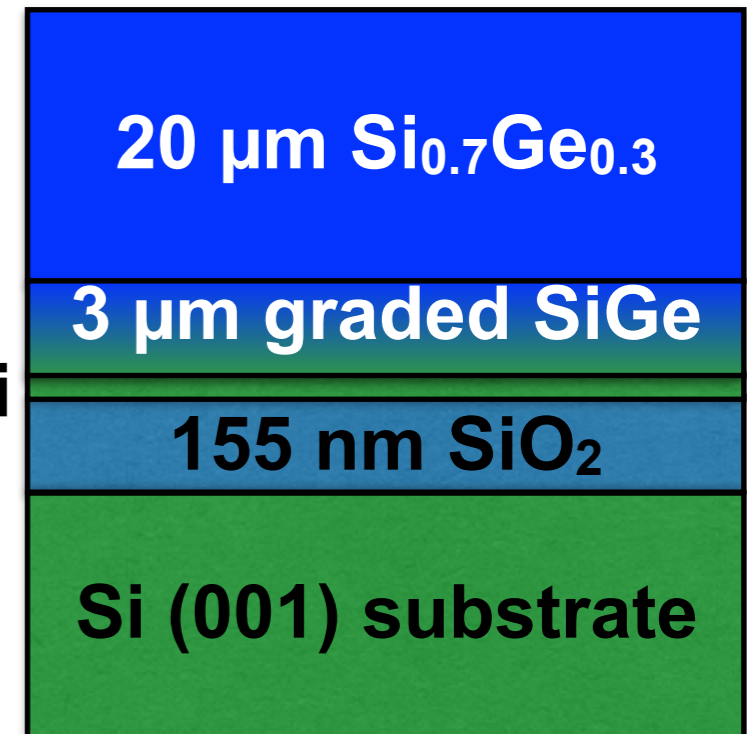


- ZT enhanced by x117
- $\alpha^2\sigma = 1.49 \text{ mW m}^{-1}\text{K}^{-2}$
- What enhancements with SiGe ?



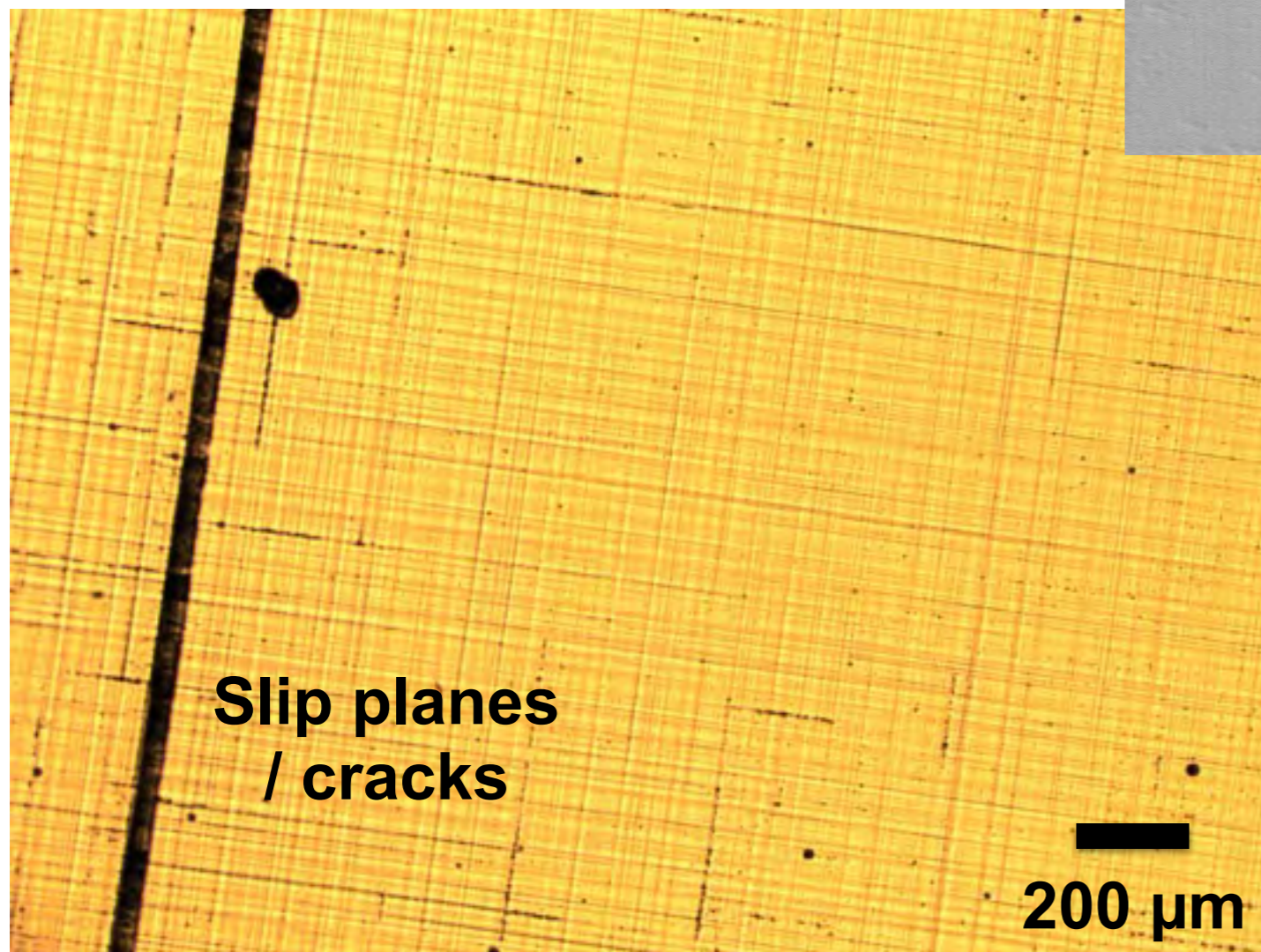
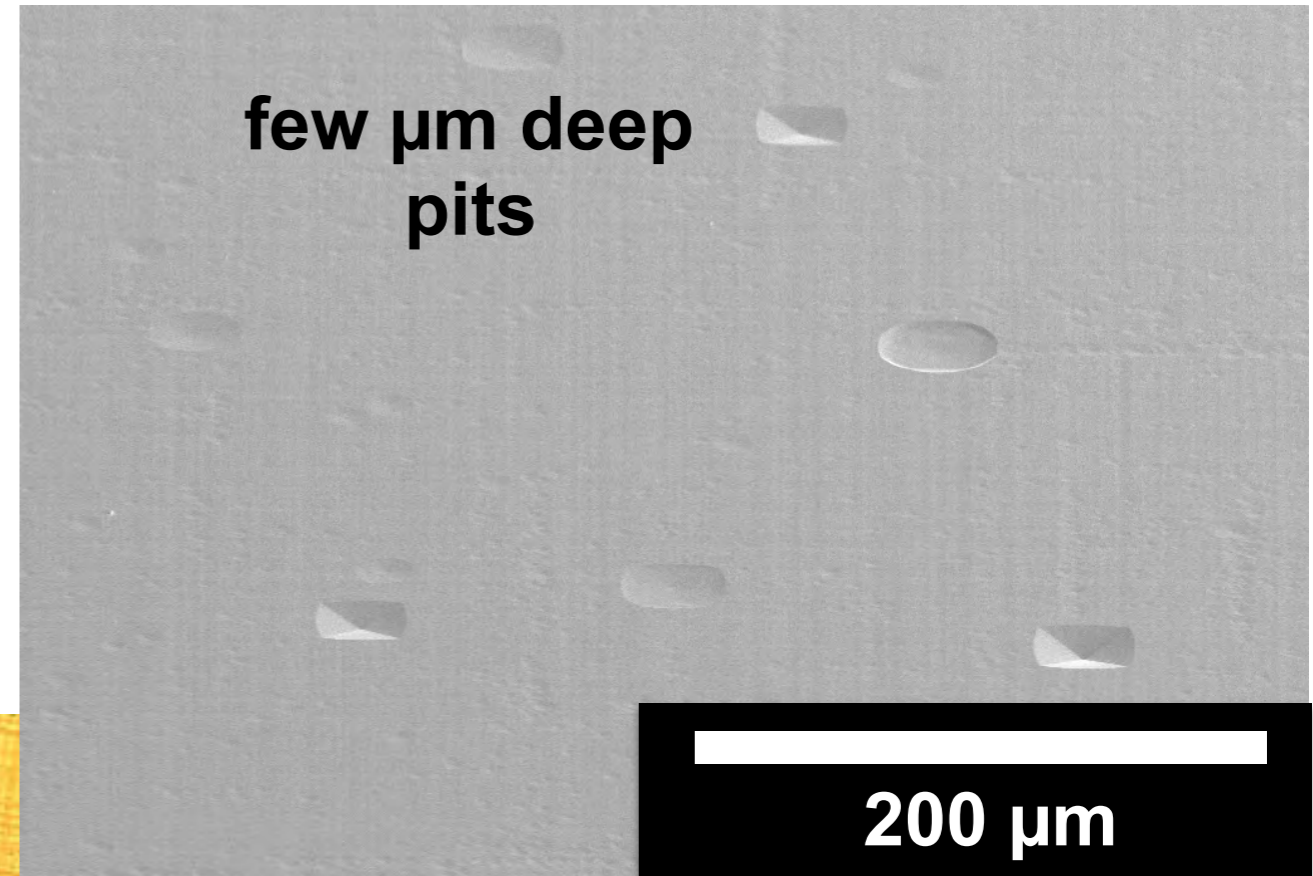
n & p-doped wafers
 $N_{D,A} = 10^{19} \text{ cm}^{-3}$

55 nm i-Si



ASM 2000E LPCVD system

200 mm SOITEC 55 nm Si,
155 nm box substrates



n & p-doped wafers
 $N_{D,A} = 10^{19} \text{ cm}^{-3}$

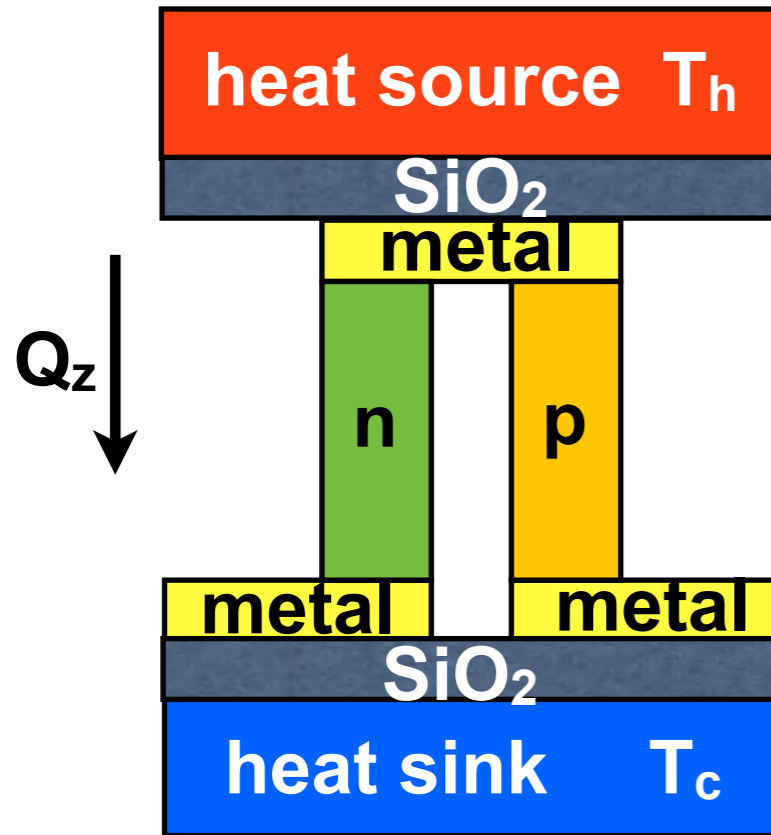
20 μm $\text{Si}_{0.7}\text{Ge}_{0.3}$

3 μm graded SiGe

155 nm SiO_2

Si (001) substrate

55 nm i-Si



- Fourier's law of heat conduction

$$Q = -\kappa \nabla T$$

- Assume 1D heat flow

$$Q_z = -\kappa(T) \frac{dT}{dx}$$

Fourier heat conduction

Peltier effect

$$Q_z A_{\text{chip}} = -\kappa_{\text{SiGe}}(T) N_{\text{legs}} A_{\text{legs}} \frac{T_H - T_C}{L} + N_{\text{leg}} \alpha(T) I T_H$$

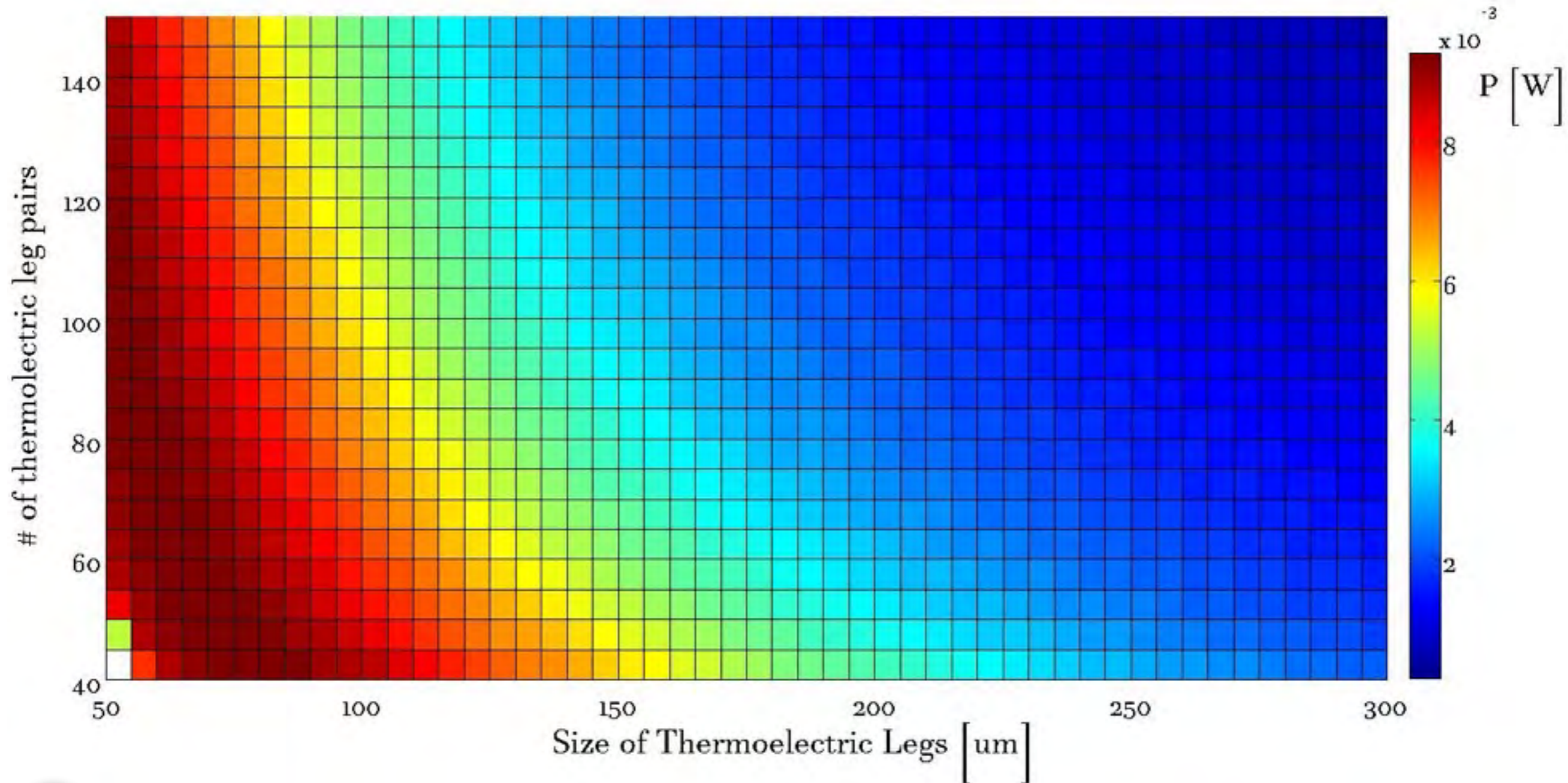
$$-R_{\text{int}}(T) I^2 + \kappa_{\text{air}} A_{\text{air}} \frac{T_H - T_C}{L} + h_C A_{\text{air}} (T_H - T_C)$$

Joule heating

thermal conduction through air

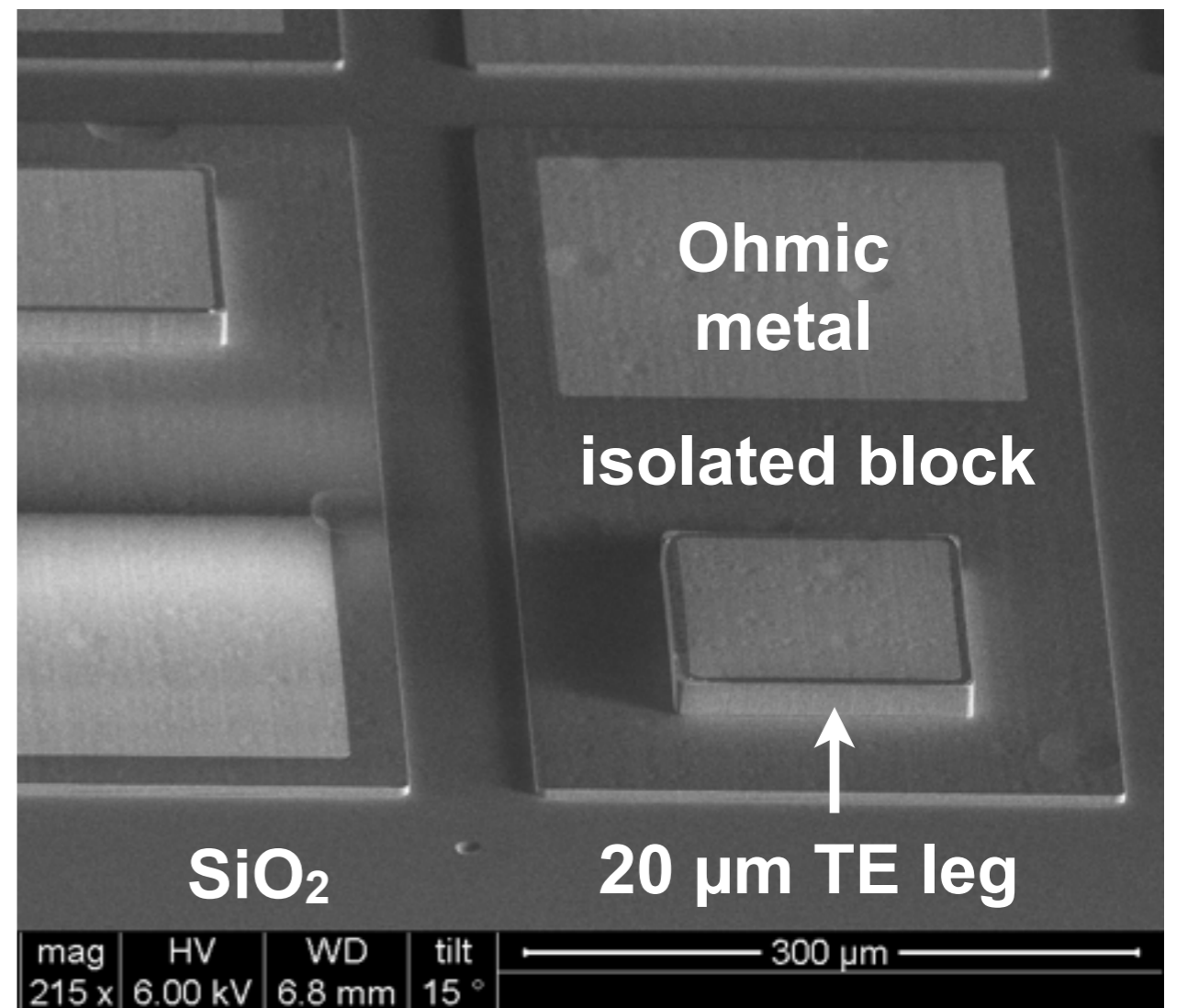
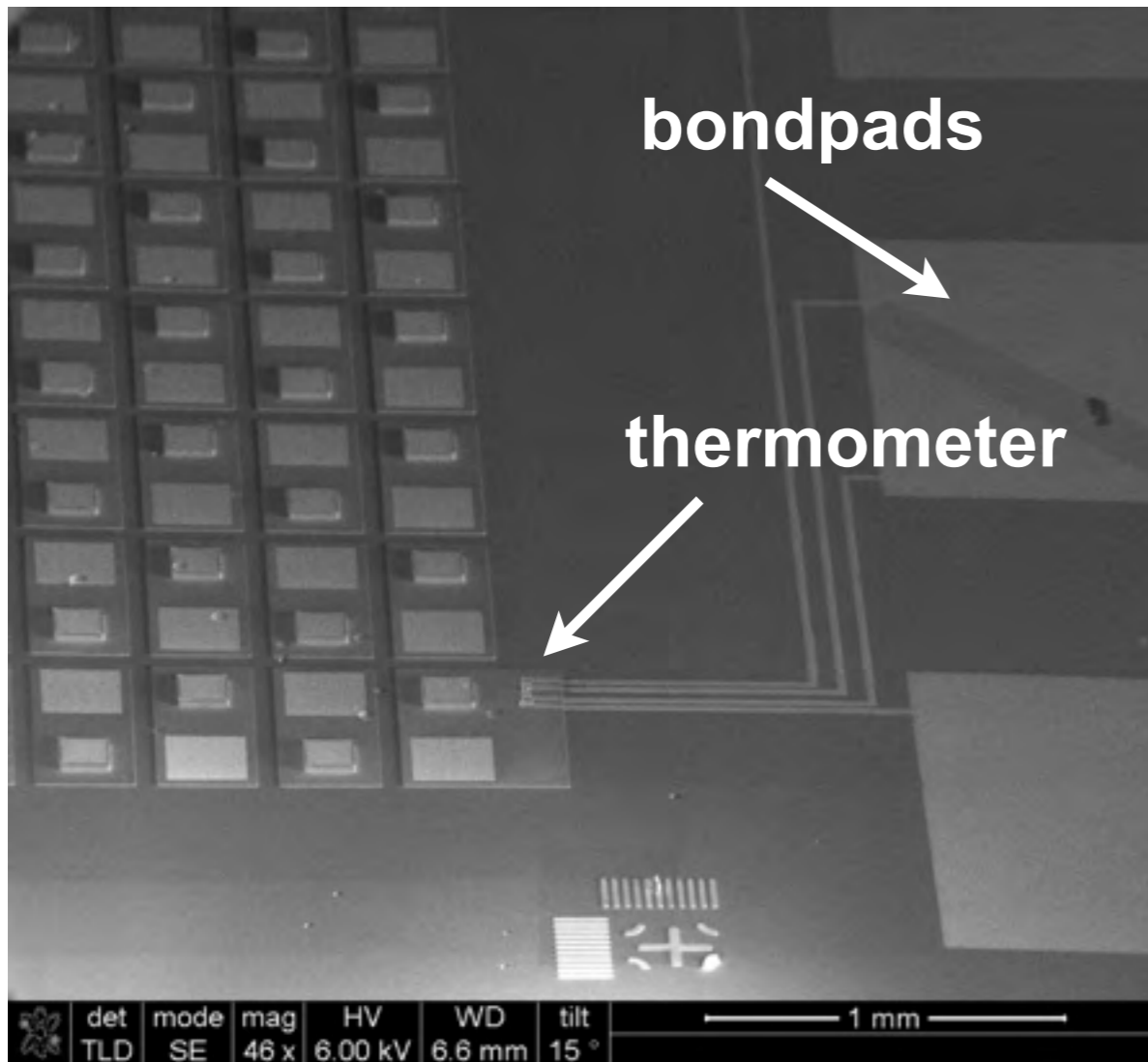
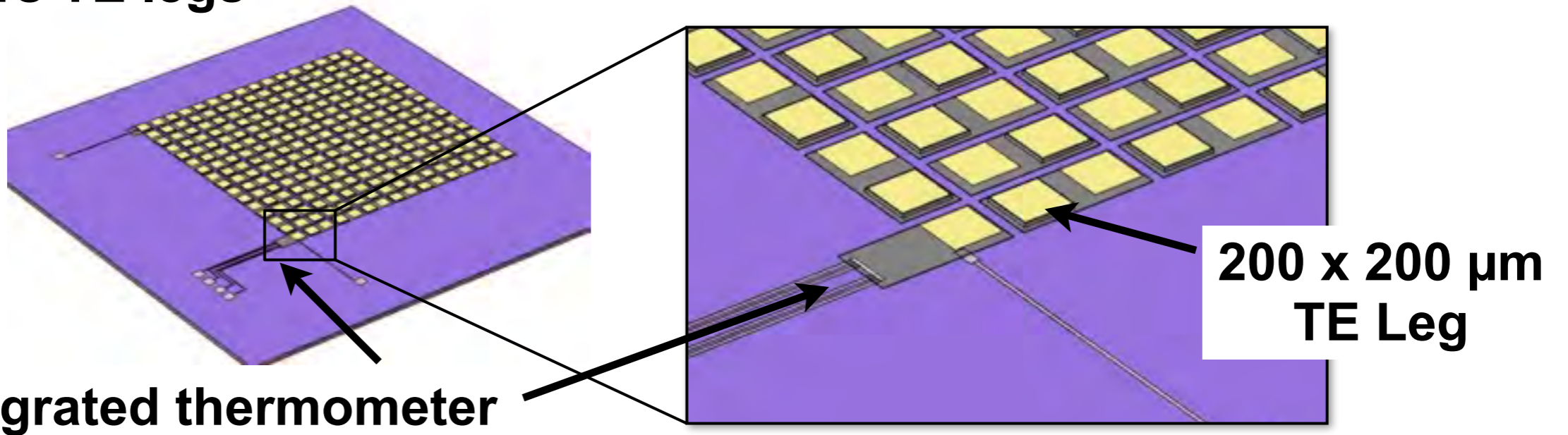
thermal convection through air

- Input heat, $Q_z = 5\text{ W/cm}^2$
- Operating temperature, $T_H = 500\text{ }^\circ\text{C}$

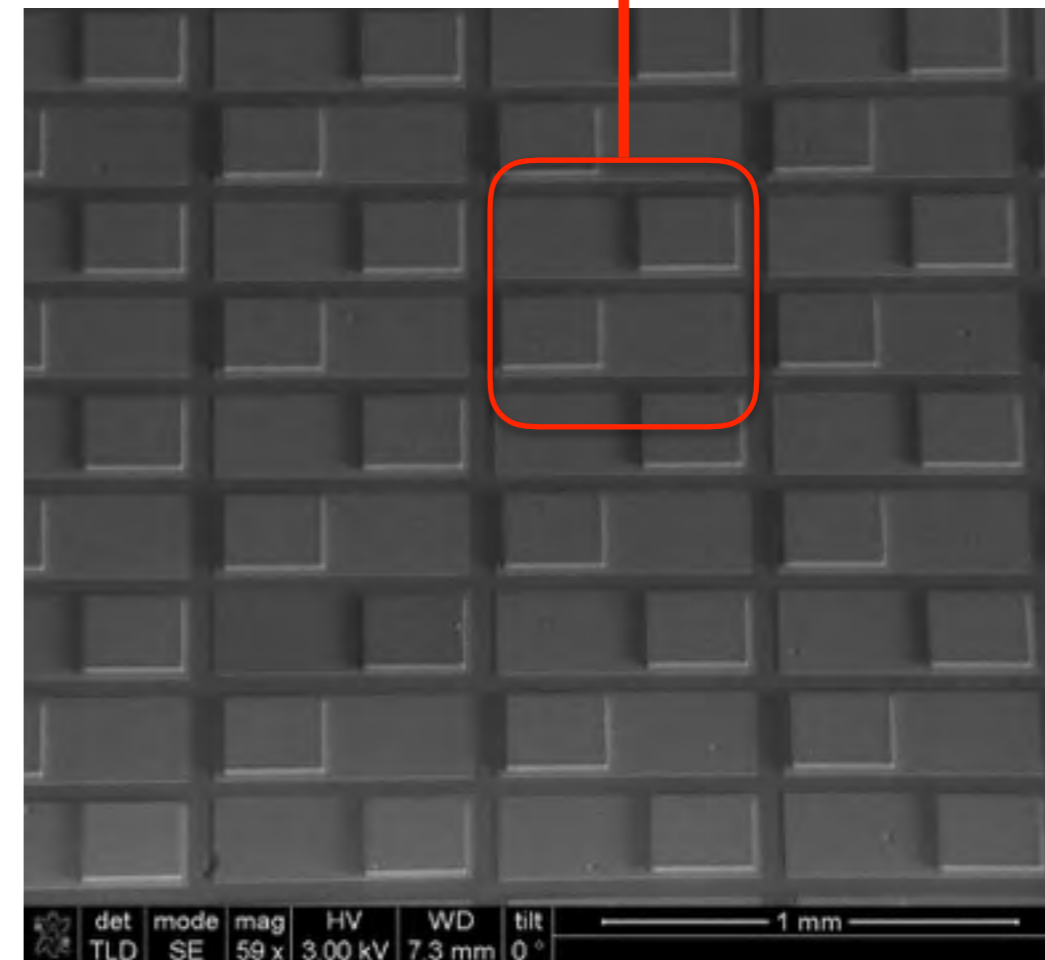
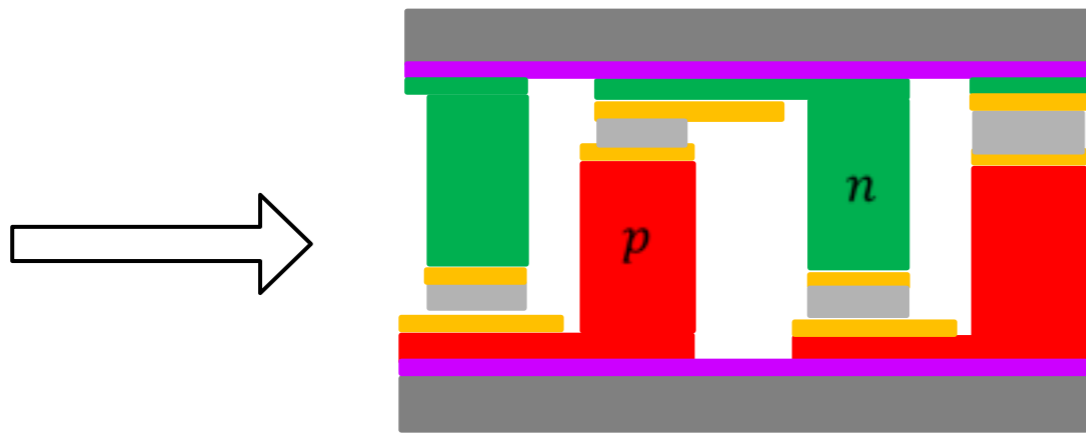
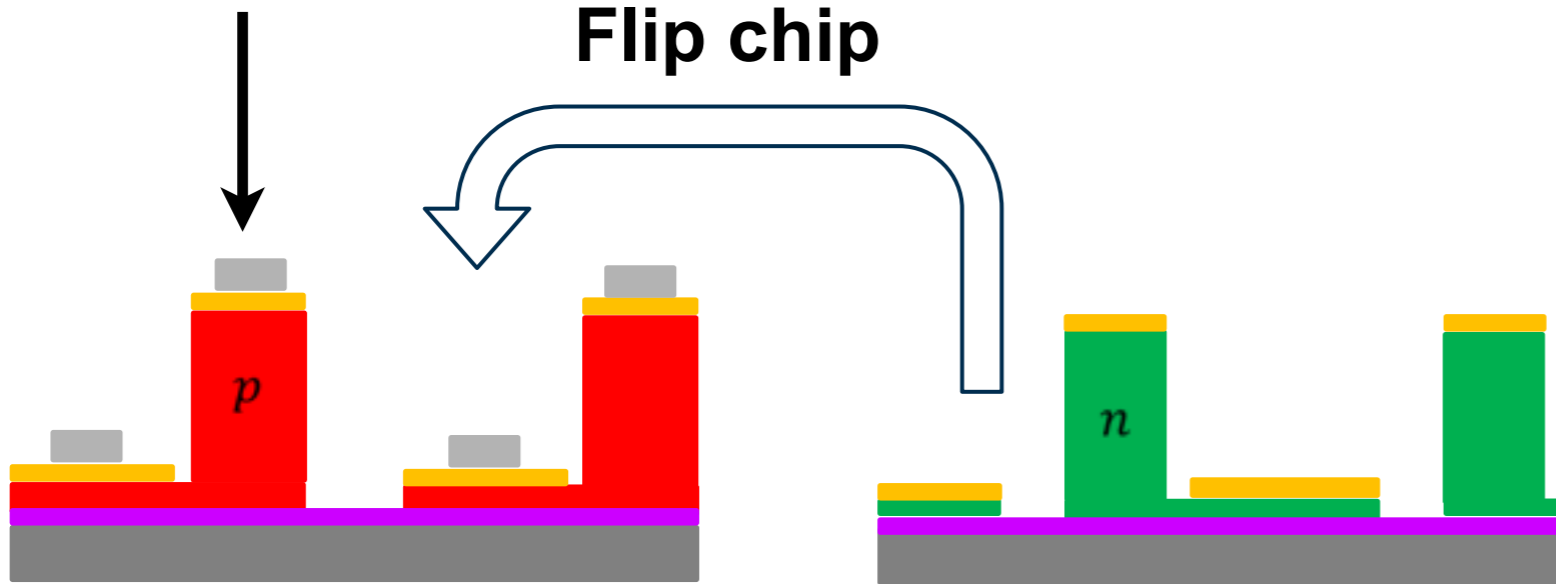


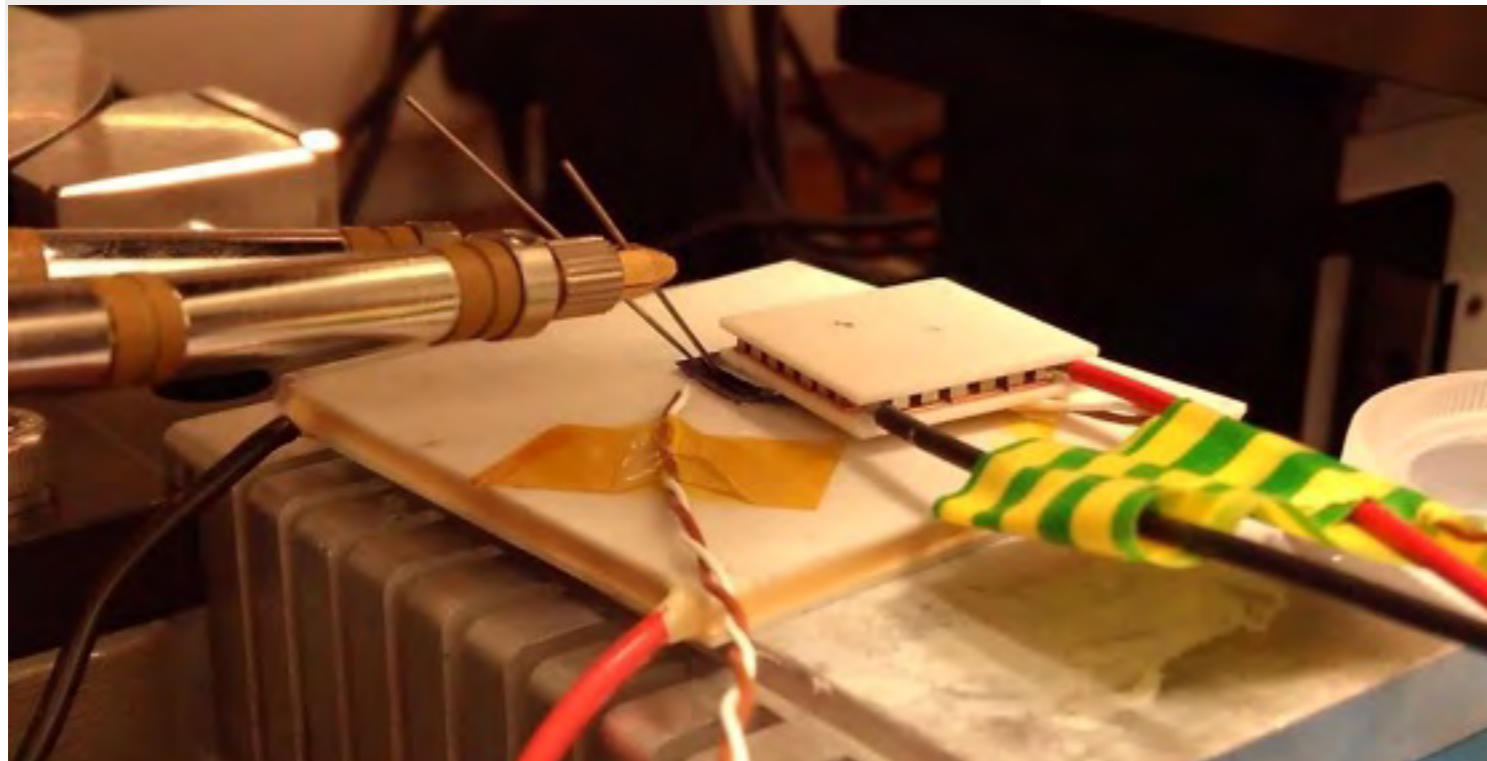
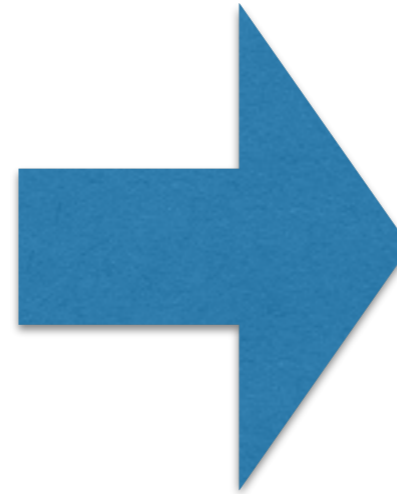
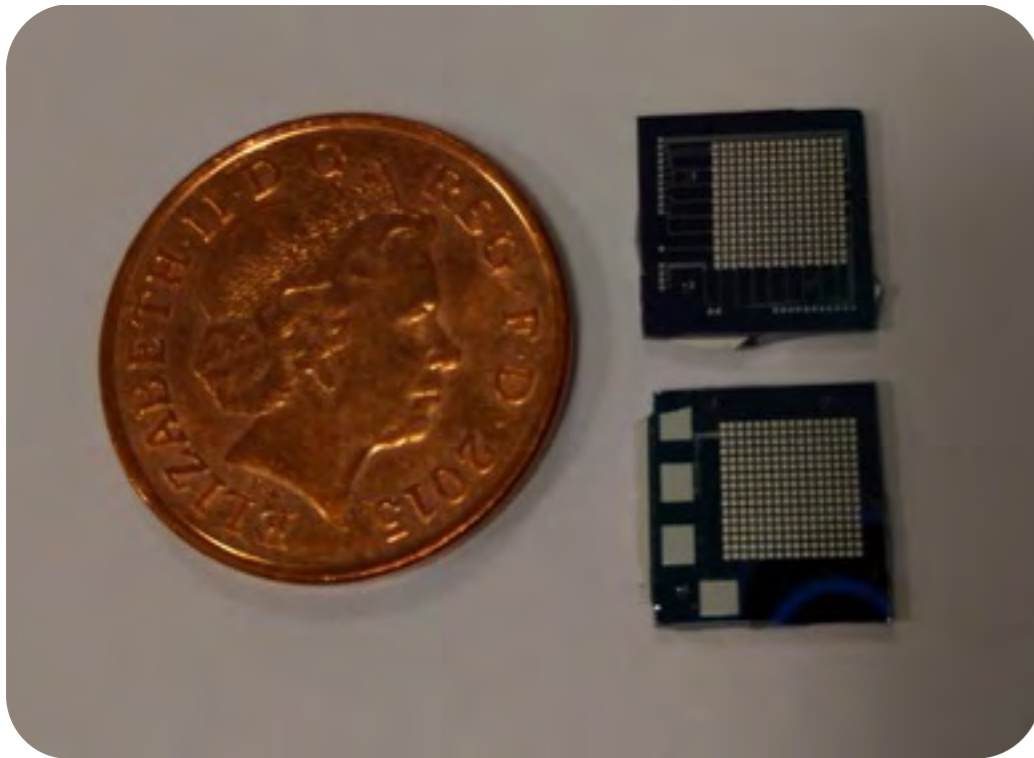
- Shorter legs better for high P but need to consider κ to maintain ΔT

68 pairs TE legs



In bumps





**Heater & 2 Peltiers
used to drive heat through
module**

**Microfabricated
thermometers measure ΔT**

- **Material cracks limit yield & ∴ legs: requires better epitaxy (limited area epitaxy?)**
- **In bumps limit T_H & dominate leg R**
- **High temperature bumps & flip-chip bonding in development**
- **Present silicides limited to ≤ 400 °C: new high T silicides e.g. $TiSi_2$ or WSi_2 stable to > 700 °C**
- **Ohmic to bumps requires better diffusion barrier => TiN**

- **Si/SiGe heterostructures for engineered electron & phonon transport towards enhanced thermoelectrics**
- **New test structures for α and κ developed**
- **ZT and power factor enhanced over bulk Si, Ge and SiGe values**
- **Prototype modules delivered: optimisation required**
- **<http://www.greensilicon.eu/GREENSilicon/index.html>**

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<http://userweb.eng.gla.ac.uk/douglas.paul/index.html>

<http://www.jwnc.gla.ac.uk/>

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Engineering and Physical Sciences
Research Council



European Thermodynamics Limited
Intelligent Thermal Management

