## Math 2371 Calc III Sample Test 3

1. Is the following vector field conservative?

$$\vec{F} = \langle yz + 3, xz + 4y, xy + 3z^2 \rangle$$
.

If so, find the potential  $\phi$ . Use this to evaluate

$$\int_{c} (yz+3)dx + (xz+4y)dy + (xy+3z^{2})dz$$

where c is any path from (0,0,0) to (1,2,3).

- 2. Evaluate the following line integral  $\int xy ds$  where c is counterclockwise direction around a circle of radius 1 from (1,0) to (0,1).
- 3. Green's Theorem is

$$\int\limits_C P\,dx + Q\,dy = \iint\limits_R \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y}\right)\,dA.$$

Verify Green's Theorem where  $\vec{F} = \langle y^2, x^2 + 2xy \rangle$  and R is the region bound by the curves  $y = x^2$ , y = 1 and x = 0 in Q1.

- 4. Evaluate  $\iint_S z \, dS$  where S is the surface of the paraboloid  $z = 1 x^2 y^2, z \ge 0$ . 5. Find the flux  $\iint_S \vec{F} \cdot \hat{n} dS$  of the vector field  $\vec{F} = \langle 2x, 2y, 2z + 2 \rangle$  through the surface of the plane x + y + z = 1 in the first quadrant.