

Math 4315/5315 - PDEs Home Work 6

Due: Mon. Nov. 15, 2021

1. Calculate the Fourier series for the following

(i) $f(x) = 1 - x^2$ on $[-1, 1]$

(ii) $f(x) = \begin{cases} x + 2 & \text{if } -2 \leq x \leq 0 \\ 0 & \text{if } 0 < x \leq 2 \end{cases}$

For each sketch the curve on $[-L, L]$ and $[-3L, 3L]$.

2. Calculate the Fourier Sine and Cosine series for the following

(i) $f(x) = 2x - x^2$ on $[0, 2]$

(ii) $f(x) = \begin{cases} x & \text{if } 0 \leq x \leq 2 \\ 4 - x & \text{if } 2 < x \leq 4 \end{cases}$

For each sketch the curve on $[-L, L]$ and $[-3L, 3L]$.