1. Find the derivative of the following

(i)
$$y = x \sin^{-1} x$$

(ii)
$$y = \ln(x^2 + e^x)$$

(iii)
$$x^2 - xy + y^4 = x - y$$

2. Find the absolute minimium and maximum of the following on the given interval

(i)
$$f(x) = 2x^2 - 12x + 1$$
 on [0,6]
(ii) $f(x) = 2x^3 - 15x^2 + 24x$ on [0,3]

3. State the Mean Value Theorem. Verify the Mean Value Theorem for the following:

(i)
$$f(x) = x^3 - x$$
 on [0,2]
(ii) $f(x) = \frac{x}{x+2}$ on [1,10]

4. If $y = x(x-4)^3$ calculate the following

- (i) The critical numbers
- (ii) When y is increasing and decreasing.
- (iii) Determine whether any of the critical numbers are minimum or maximum.
- (iv) When y is concave up and down and determine the points of inflection.
- (v) Then sketch the curve.

5. A ladder 13 feet long is resting against the wall of a house. The base of the ladder is pulled away from the wall at a rate of 2 ft/sec. At rate is the tip of the ladder moving down the wall when the base of the ladder is 5 ft away from the wall?

6. A paper cup in the shape of an inverted cone with height 10 cm and a base of radius 3 cm, is being filled at a rate of $2 \text{ cm}^3/\text{min}$. Find the rate of change in the height of the water when the height of the water is 5 cm.