Best Practices in Math: Math Language and Fluency (Grades 3-5)





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Say hello.

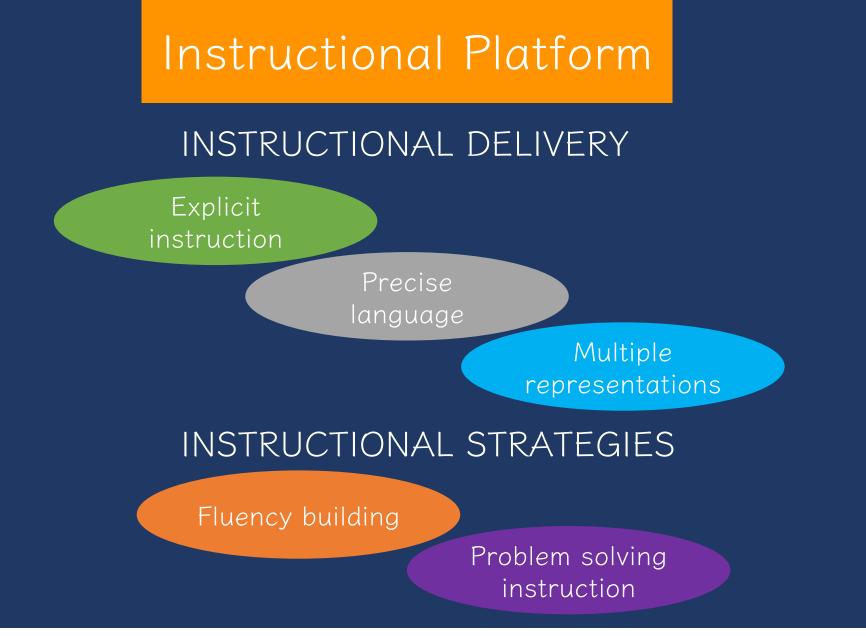
Describe your role as an educator and the mathematics you support.





December 2022	Best Practices in Math: Math Language and Fluency
January 24, 2023	Best Practices in Math: Modeling and Practice Word-Problem Solving
TBD	Best Practices in Math: Use of Multiple Representations

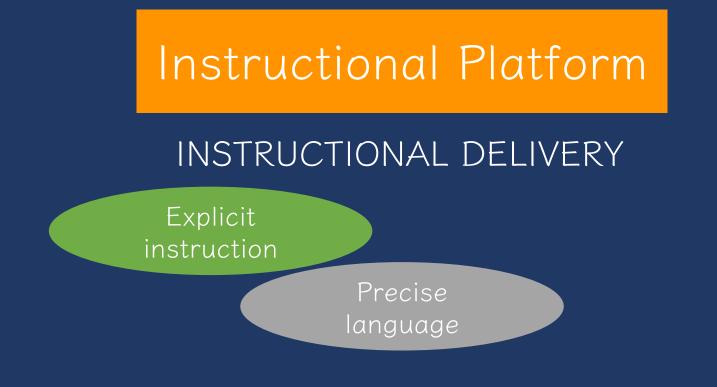






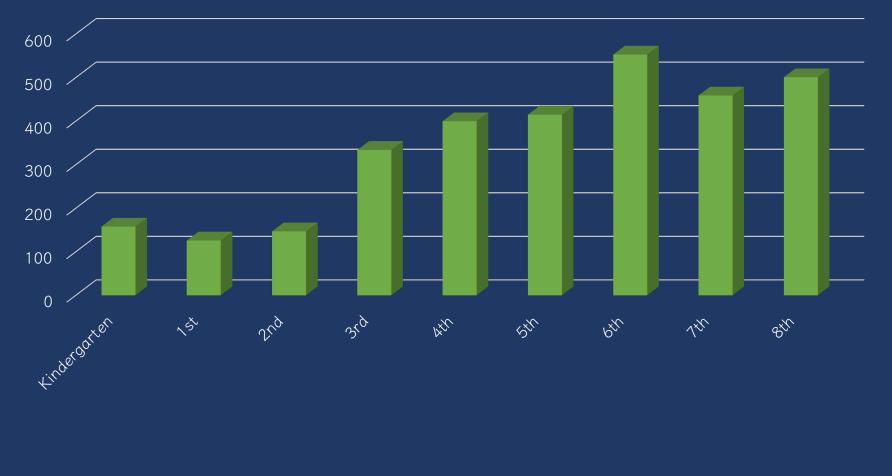
Mathematical Language

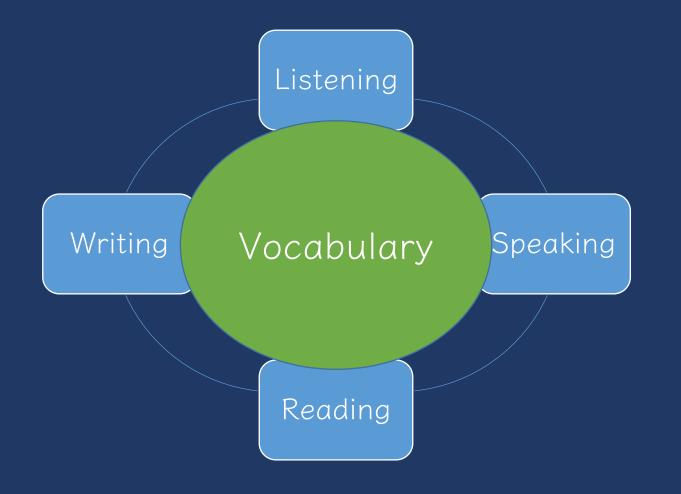




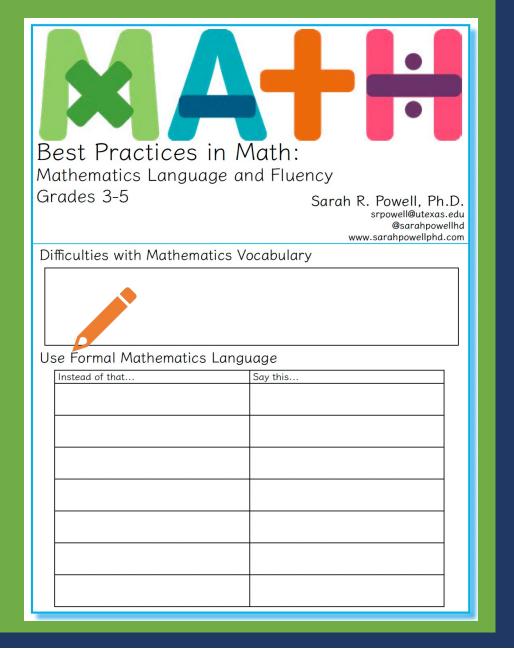
INSTRUCTIONAL STRATEGIES















Rubenstein & Thompson (2002)



- 1. Some math terms are shared with English but have different meanings
- 2. Some math words are shared with English with similar meanings (but a more precise math meaning)



Rubenstein & Thompson (2002)



- 2. Some math words are shared with English with similar meanings (but a more precise math meaning)
- 3. Some math terms are only used in math



Rubenstein & Thompson (2002)



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Rubenstein & Thompson (2002)



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5. Some math terms are similar to other content-area terms with different meanings







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6. Some math terms are homographs







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- 6. Some math terms are homographs
- 7. Some math terms are related but have distinct meanings

factor vs. multiple hundreds vs. hundredths

numerators vs. denominator

Rubenstein & Thompson (2002)



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- 7. Some math terms are related but have distinct meanings

8. An English math term may translate into another language with different meanings

mesa vs. tabla

Rubenstein & Thompson (2002)



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9. English spelling and usage may have irregularities

four vs. forty

Rubenstein & Thompson (2002)



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9. English spelling and usage may have irregularities

10. Some math concepts are verbalized in more than one way

skip count vs. multiples

XA++

one-fourth

vs. one

quarter

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10. Some math concepts are verbalized in more than one way

11. Informal terms may be used for formal math terms

rhombus vs. diamond

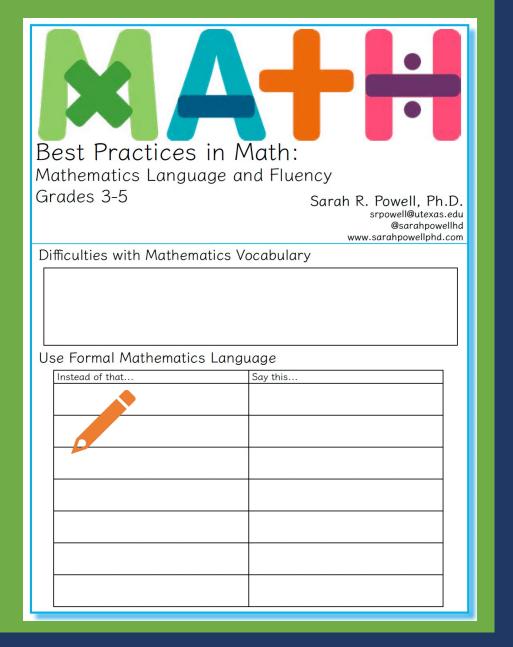
> vertex vs. corner





What are the ways you see your students experience difficulty with the vocabulary of math?







Use formal math language

Use terms precisely







What number is in the tens place?

What digit is in the tens place? What is the value of the digit in the tens place?

Why this is important...

- A number refers to the entire amount.
- The 3 in the tens place value is not a number, but rather a digit in the number 135.
- Reinforces conceptual understanding of place value.

135

• Emphasizes that 3 is part of the number 135 with a value of 30.



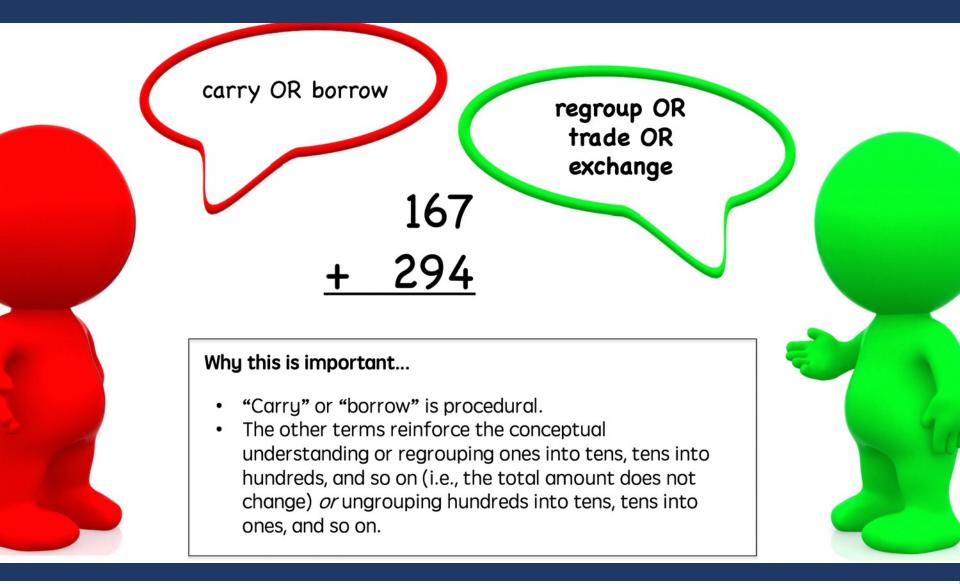
The alligator eats the bigger number

is less than OR is greater than

Why this is important...

- Students must learn how to read and write the inequality symbols.
- Students must learn to read equations correctly from left to right because < and > are two distinct symbols.







top number and bottom number

numerator and denominator

Why this is important...

- Identifying that there are two separate (whole) numbers suggests that whole number properties can be applied to fractions.
- Emphasizing that a fraction is ONE number with ONE magnitude on a number line that is communicated with a numerator and denominator is important.





rename OR find equivalent OR simplify

Why this is important...

• Reducing suggests that the quantity or magnitude of the new number will be less than the original number.



Four point seven Four point oh seven

Four and seven tenths Four and seven hundredths

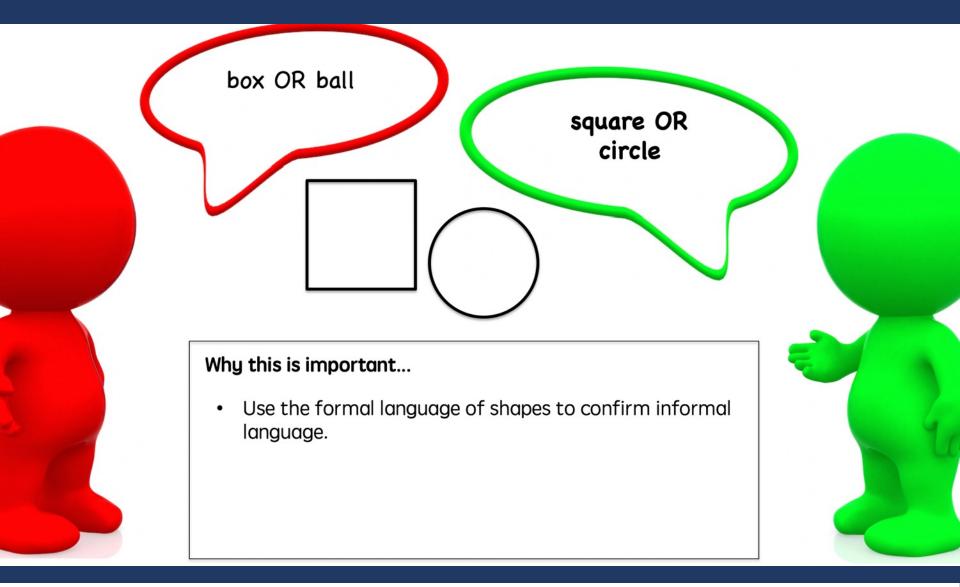
Why this is important...

• Accurately shares the magnitude of the decimal.

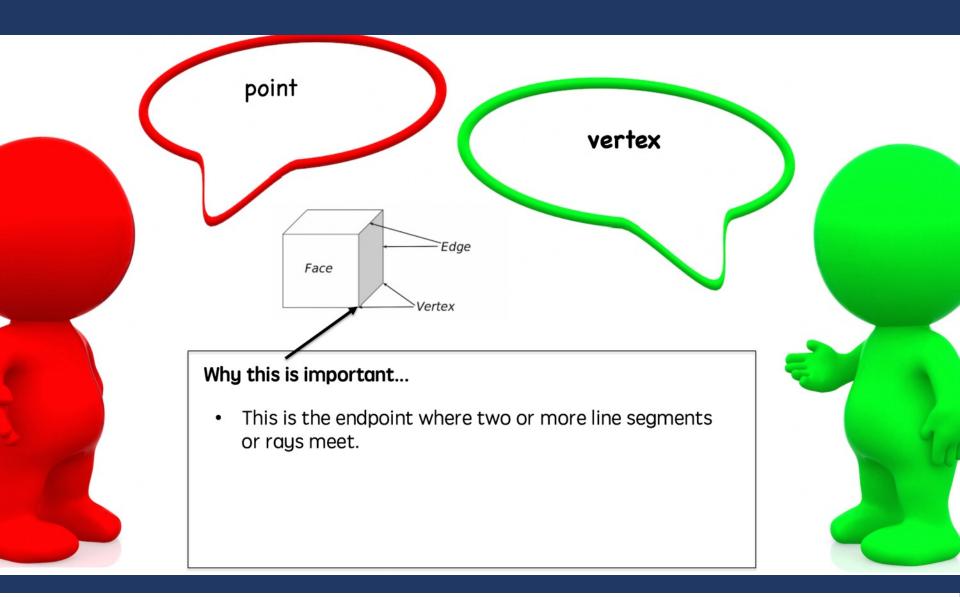
4.7 4.07

• Emphasizes place value.











Best Practices in Math: Mathematics Language and Fluency Grades 3-5

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Difficulties with Mathematics Vocabulary

Use Formal Mathematics Language

Instead of that	Say this	

Identify examples of "Instead of ____, say



Use formal math language

Use terms precisely



Use Mathematics Vocabulary With Precision	
L Strategies for Teaching Mathematics Language	



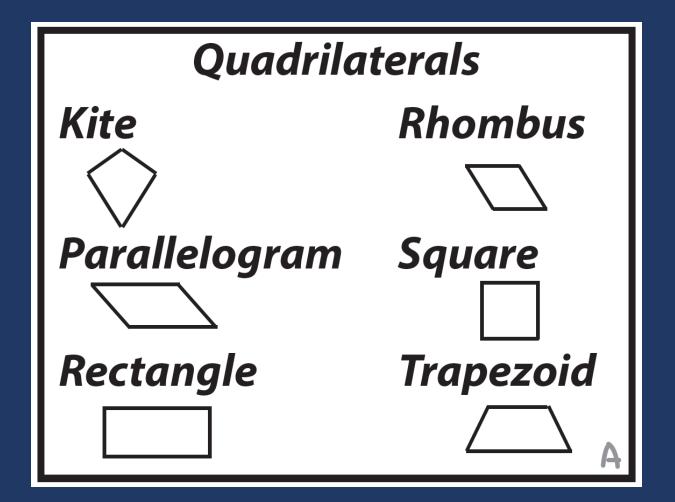
Factor
1 × 8 = 8
2 × 4 = 8

$$f_{a_{cto_{r}}}$$
 $f_{a_{cto_{r}}}$
Multiple
8 × 1 = 8
8 × 2 = 16
multiples of 8
Multiples of 8

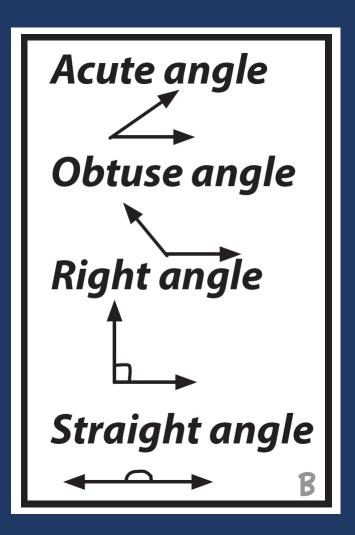


Improper fraction 8 5	Proportion $\frac{2}{5} = \frac{8}{20}$
Mixed number $1\frac{3}{5}$	Ratio 4:3
Proper fraction 2 9	Unit fraction $\frac{1}{6}$ D

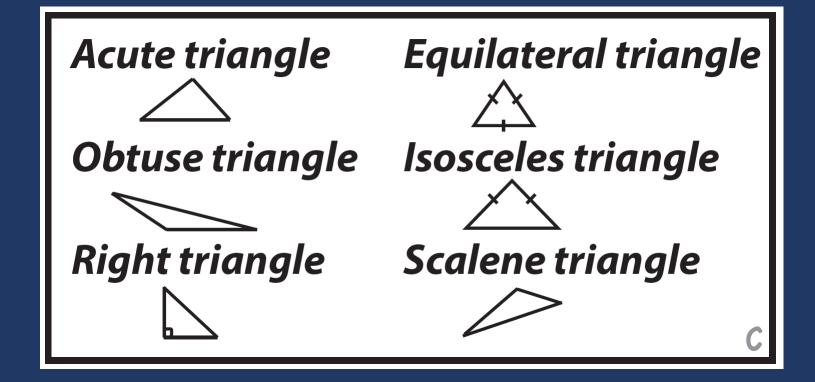




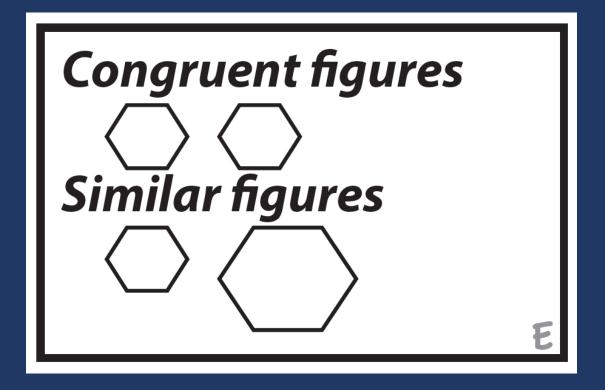




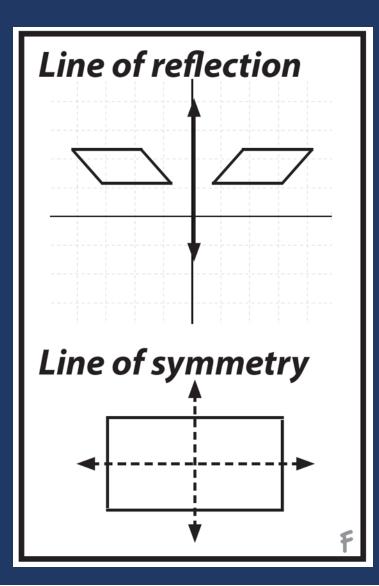




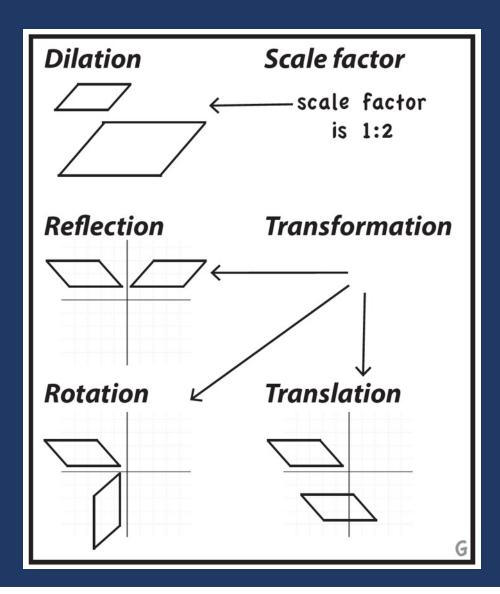




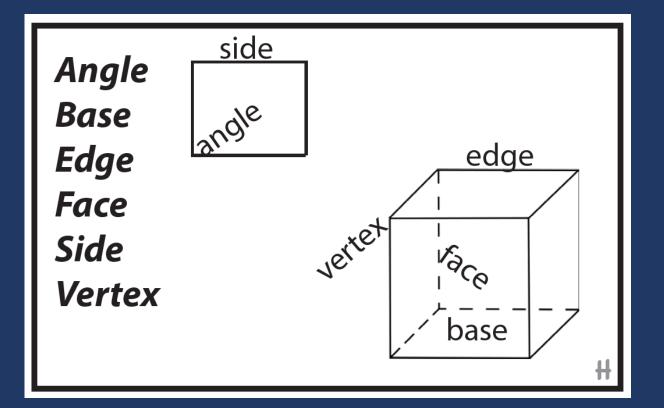




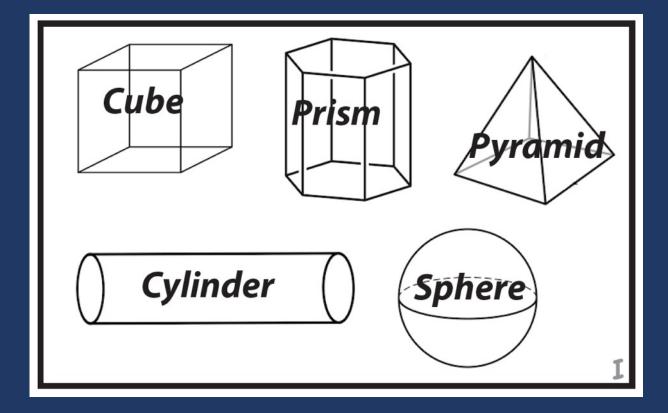














Use Mathematics Vocabulary With Precision

Strategies for Teaching Mathematics Language

Discuss terms you want your students to use with precision.



Use formal math language

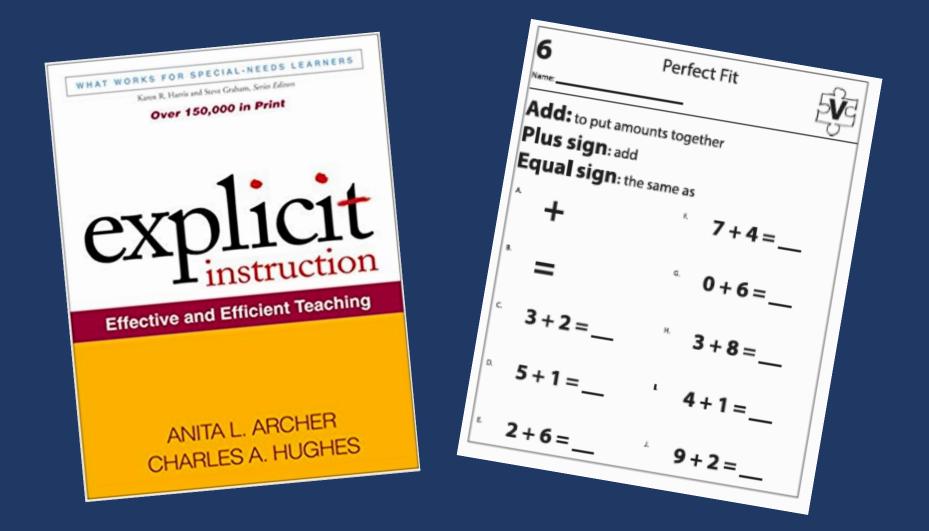
Use terms precisely



Use Mathematics Vocabulary With Precision	
L Strategies for Teaching Mathematics Language	

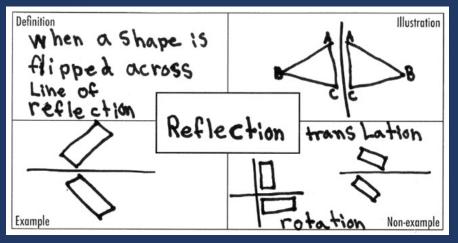


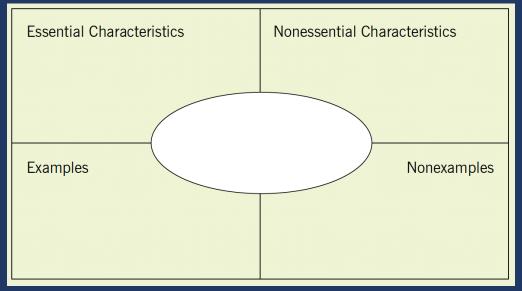
1. Use explicit instruction





2. Use graphic organizers





Dunston & Tyminski (2013)



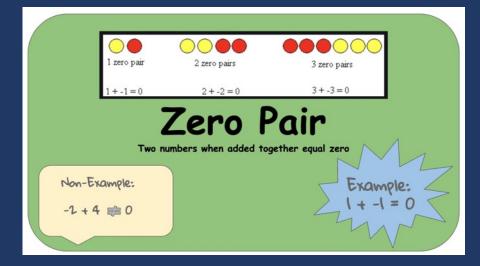
2. Use graphic organizers

Word	Lightbulb Word
Definition	Picture

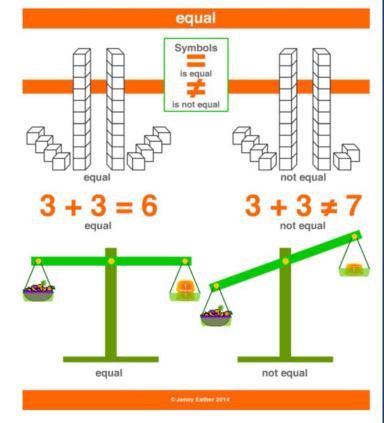
Dunston & Tyminski (2013)



3. Have students create vocabulary cards

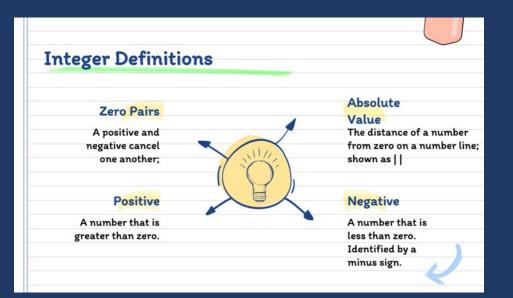


6. Equal: having the same amount or value.





4. Have students create glossaries



Numerator: how many parts of the whole



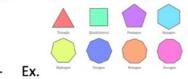
Odd number: a number not divided evenly by 2

- Ex. 1, 3, 5, 7, 9....

Percent: a specific number in comparison to 100

- 74%

Polygon: any enclosed shape that is made up of 3 or more straight lines



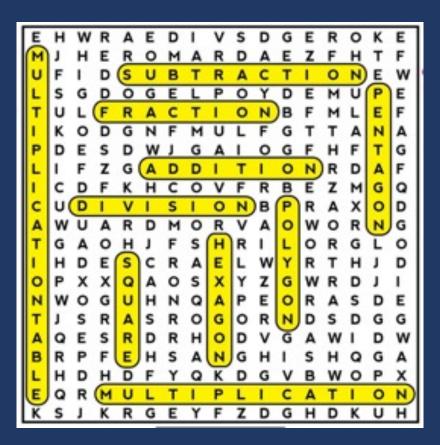


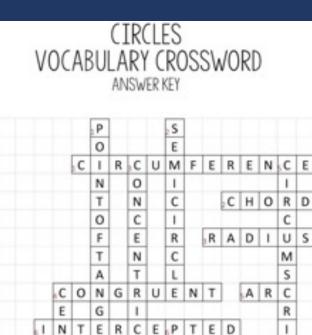
5. Create a word wall





6. Do word games





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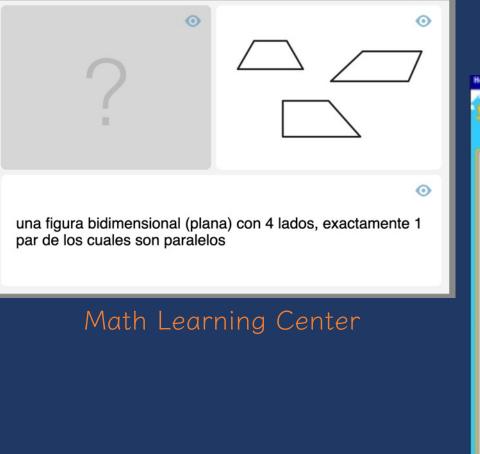
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7. Use technology





Math Lingo



Use Mathematics Vocabulary With Precision

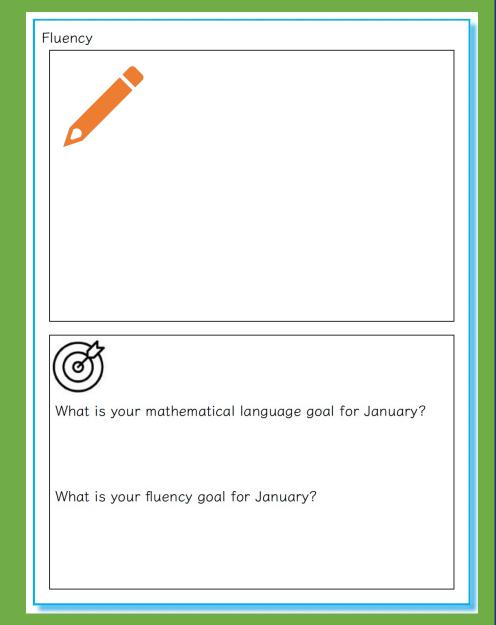
Strategies for Teaching Mathematics Language

Discuss your strategy for focusing on mathematical language in your teaching.

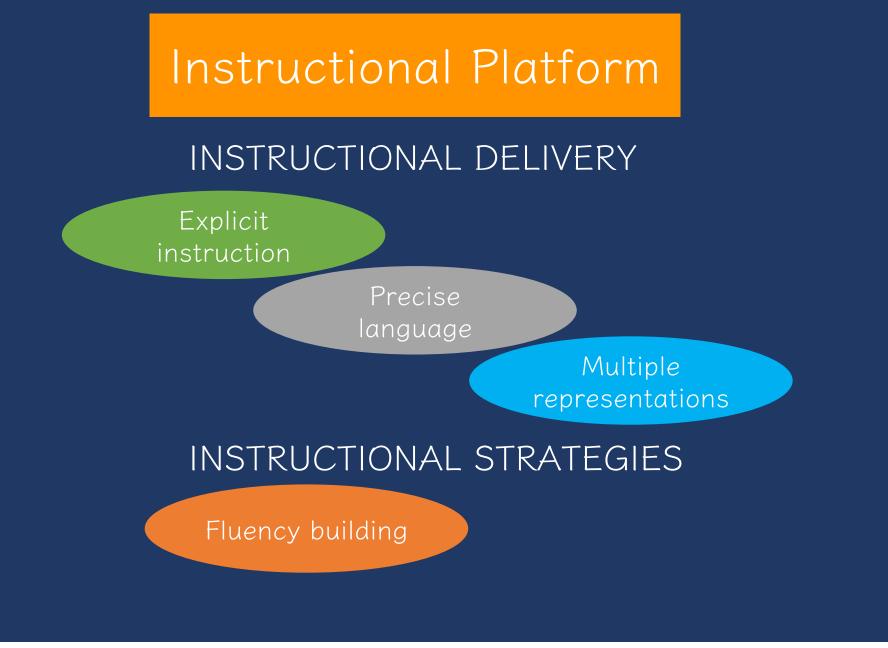












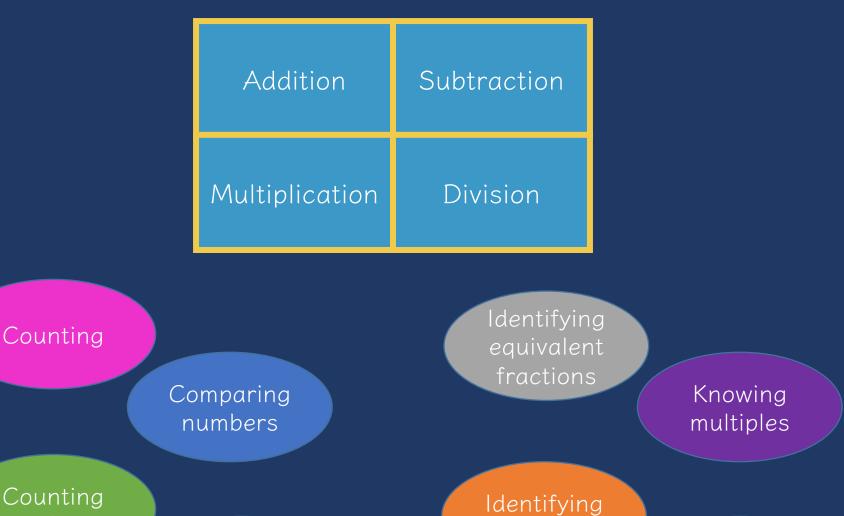


Building Fluency

Fluency is doing mathematics easily and accurately. Fluency in mathematics makes mathematics easier. Fluency provides less stress on working memory. Fluency helps students build confidence with mathematics.

With fluency, it is important to emphasize both conceptual learning and procedural learning.



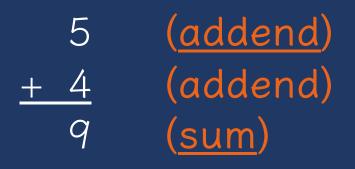






100 addition facts

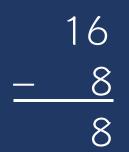
Single-digit addends sum to a single- or double-digit number





100 subtraction facts

Subtrahend and difference are single-digit numbers and minuend is single- or double-digit number



(minuend) (subtrahend) (<u>difference</u>)



100 multiplication facts

Multiplication of single-digit factors results in a single- or double-digit product







90 division facts

Divisor and quotient are single-digit numbers and dividend is single- or double-digit number

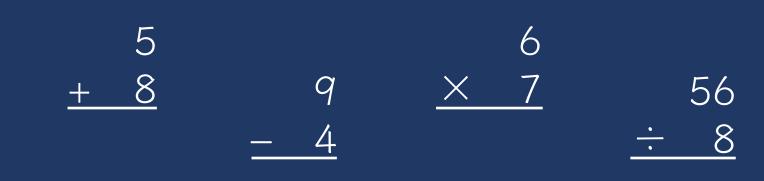
 $8 \div 4 = 2$ (dividend) (divisor) (quotient)



Addition	Subtraction
Multiplication	Division

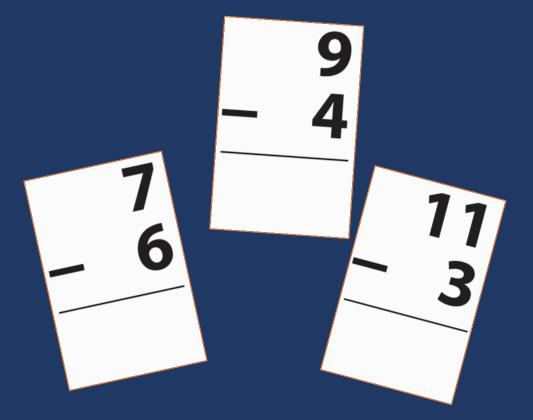
Build fluency with math facts.

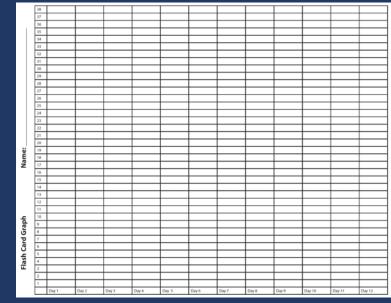
- Addition: single-digit addends
- Subtraction: single-digit subtrahend
- Multiplication: single-digit factors
- Division: single-digit divisor



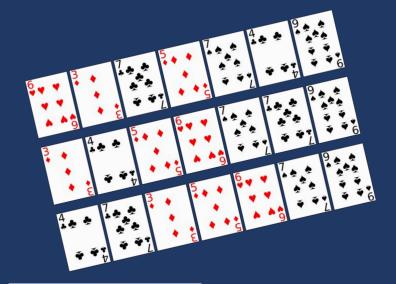


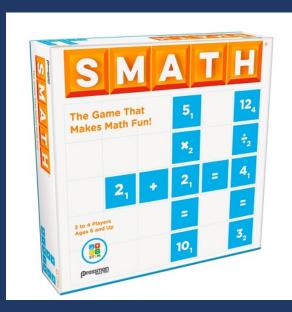
	Cover, Copy, Com	pare				Taped Prob	lems		
	9	8 × 6			6 × 5	8 × 6	7 × 9	6 × 8	
	× 6 54 7	48 6 × 5			9 × 8	8 × 5	7 × 8	6 × 6	
	× 8 56 9	$3_{6+3=1+7=}$	File Folder		7 × 7	6 × 9	5 × 9	8 × 4	
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	6 × 7 42	5+6= 4+7= 7+8=		9 11 11	6 × 7	8 × 8	4 × 8	5 × 7	
	8 × 8	6 + 7 = 7 + 9 = 7 + 6 =		15 13 16					
	64	8+7= 7+0=		13 15 7					
		9+6= 6+0= 6+8=		15					
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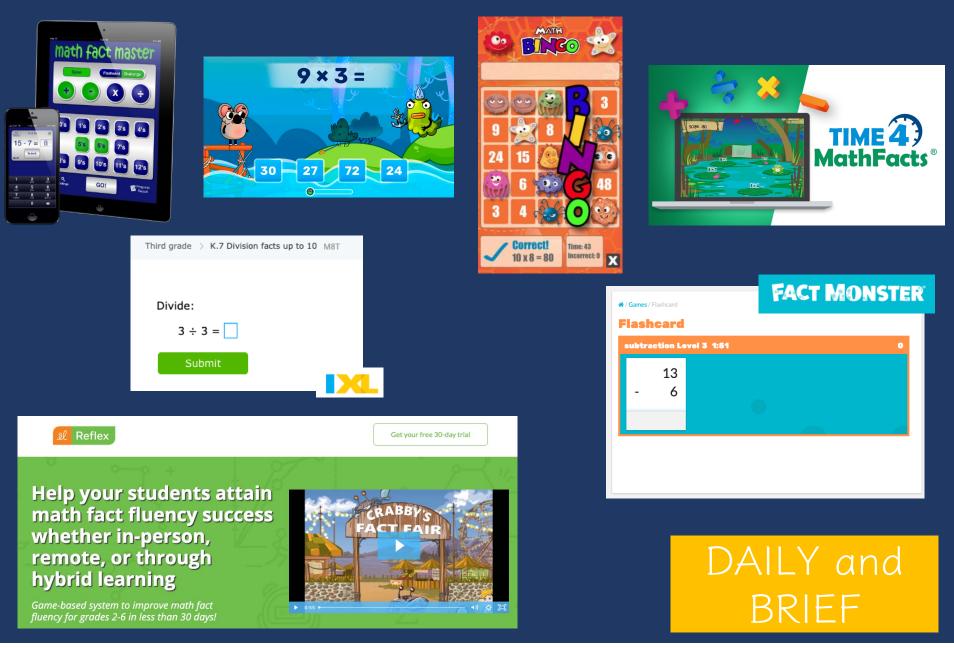








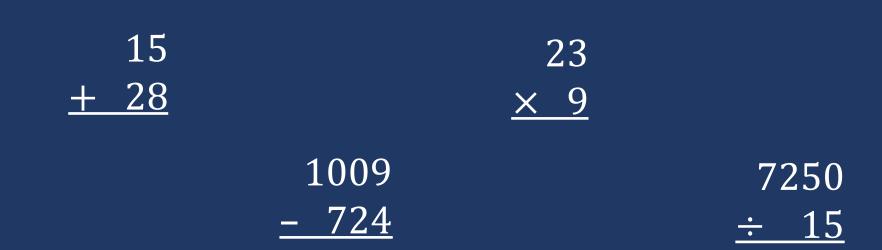






Addition	Subtraction
Multiplication	Division

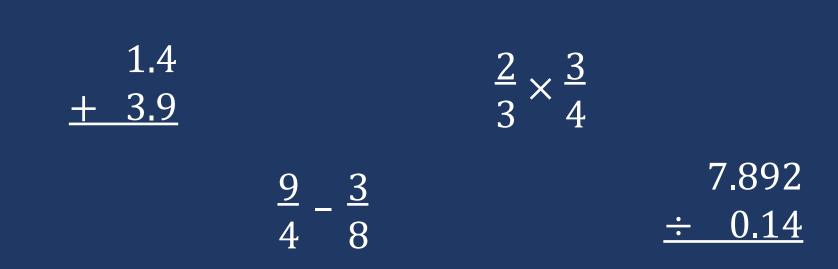
Build fluency with whole-number computation





Addition	Subtraction
Multiplication	Division

Build fluency with rational-number computation





Addition	Subtraction
Multiplication	Division

1.4

-3.9

Build fluency with integer computation



<u>× -12</u>

6

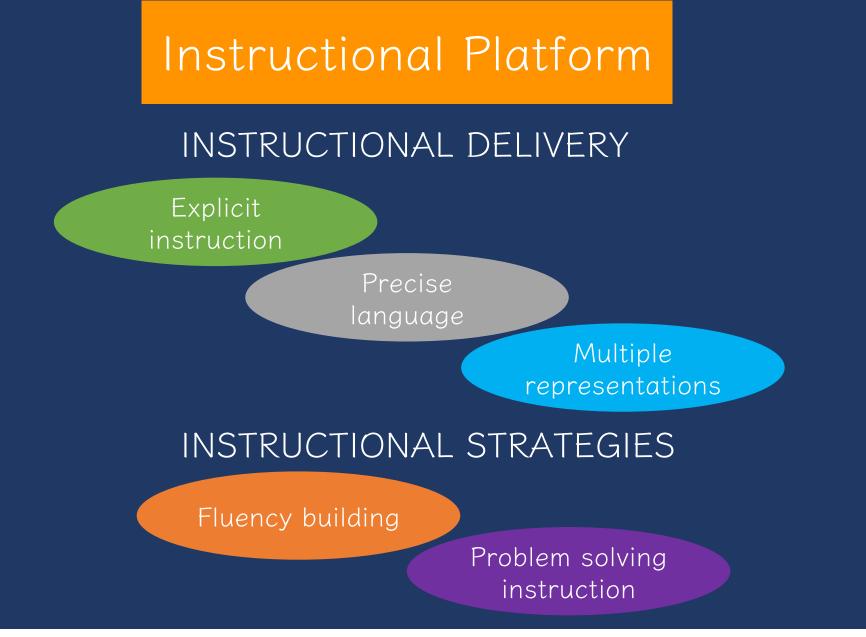


Addition	Subtraction
Multiplication	Division

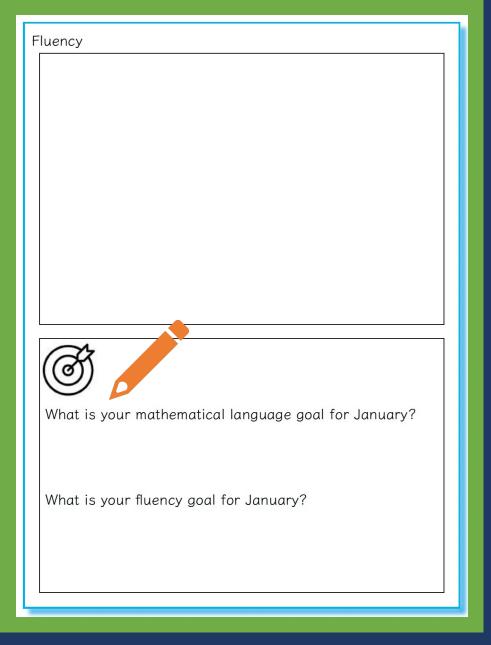


What fluency practice do your students need?













What is your mathematical language goal for January?



What is your fluency goal for January?





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