

**Solomon Press**  
**Core Mathematics C2**  
**Paper I**  
**(Mark Scheme)**

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GCE Examinations  
Advanced Subsidiary

# Core Mathematics C2

Paper 1

## MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks could be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.

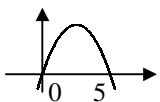
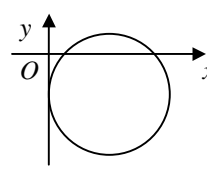


*Written by Shaun Armstrong*

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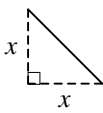
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## C2 Paper I – Marking Guide

1. (a)  $\frac{1}{2} \times 9.2^2 \times \angle AOB = 37.4$  M1  
 $\angle AOB = 0.884$  radians (3sf) A1  
 (b)  $= (2 \times 9.2) + (9.2 \times 0.8837) = 26.5$  cm (3sf) M1 A1 **(4)**
- 
2.  $\frac{2}{p-1} = \frac{2p+5}{2}$  M1  
 $(2p+5)(p-1) = 4$  M1  
 $2p^2 + 3p - 9 = 0$  A1  
 $(2p-3)(p+3) = 0, \quad p = -3, \frac{3}{2}$  M1 A1 **(5)**
- 
3.  $5x - x^2 = 0$   
 $x(5-x) = 0$   
 crosses  $x$ -axis at  $(0, 0)$  and  $(5, 0)$   B1  
 area  $= \int_0^5 (5x - x^2) dx$   
 $= [\frac{5}{2}x^2 - \frac{1}{3}x^3]_0^5$  M1 A2  
 $= (\frac{125}{2} - \frac{125}{3}) - (0) = 20\frac{5}{6}$  M1 A1 **(6)**
- 
4.  $1 - \cos^2 \theta = 4 \cos \theta$  M1  
 $\cos^2 \theta + 4 \cos \theta - 1 = 0$  A1  
 $\cos \theta = \frac{-4 \pm \sqrt{16+4}}{2} = -2 - \sqrt{5}$  (no solutions) or  $-2 + \sqrt{5}$  M1 A1  
 $\theta = 76.3, 360 - 76.3$  B1 M1  
 $\theta = 76.3^\circ, 283.7^\circ$  (1dp) A1 **(7)**
- 
5. (a)  $-27 + 63 - 3p - 6 = 0, \quad p = 10$  M1 A1  
 (b) remainder  $= f(2) = 8 + 28 + 20 - 6 = 50$  M1 A1  
 (c)  $x = -3$  is a solution  $\therefore (x+3)$  is a factor B1
- $$\begin{array}{r} x^2 + 4x - 2 \\ x+3 \overline{) x^3 + 7x^2 + 10x - 6} \\ \underline{x^3 + 3x^2} \phantom{- 6} \\ 4x^2 + 10x \phantom{- 6} \\ \underline{4x^2 + 12x} \phantom{- 6} \\ -2x - 6 \\ \underline{-2x - 6} \\ 0 \end{array}$$
- $\therefore (x+3)(x^2+4x-2) = 0$   
 $x = -3$  or  $x^2 + 4x - 2 = 0$   
 other solutions:  $x = \frac{-4 \pm \sqrt{16+8}}{2} = -4.45, 0.45$  M1 A1 **(9)**
- 
6. (a)  $(x-6)^2 - 36 + (y+4)^2 - 16 + 16 = 0$  M1  
 $\therefore$  centre  $(6, -4)$  A1  
 (b)  $(x-6)^2 + (y+4)^2 = 36$  M1  
 $\therefore$  radius  $= 6$  A1  
 (c)  B2  
 (d)  $y = 0 \therefore (x-6)^2 + 16 = 36$  M1  
 $x = 6 \pm \sqrt{20} = 6 \pm 2\sqrt{5}$  A1  
 $AB = 6 + 2\sqrt{5} - (6 - 2\sqrt{5}) = 4\sqrt{5}$  M1 A1 **(10)**

7.	(a)	$(1 + ax)^n = 1 + n(ax) + \frac{n(n-1)}{2}(ax)^2 + \dots$	B2
		$\therefore an = -24$ (1)      and $\frac{1}{2}a^2n(n-1) = 270$ (2)	M1
		(1) $\Rightarrow a = \frac{-24}{n}$ sub. (2) $\frac{288}{n}(n-1) = 270$	M1
		$288n - 288 = 270n$	M1
		$18n = 288$	
		$n = \frac{288}{18} = 16, a = -\frac{3}{2}$	A2
	(b)	$1 - \frac{3}{2}x = 0.9985 \therefore x = 0.001$	B1
		$\therefore (0.9985)^{16} \approx 1 - 0.024 + 0.000270$	M1
		$= 0.97627$ (5dp)	A1 (10)

8.	(a)	$\log_2(y-1) - \log_2 x = 1, \quad \log_2 \frac{y-1}{x} = 1$	M1
		$\frac{y-1}{x} = 2^1 = 2$	M1
		$y-1 = 2x, \quad y = 2x+1$	A1
	(b)	$2 \log_3 y = 2 + \log_3 x \Rightarrow \log_3 y^2 - \log_3 x = 2$	M1
		$\frac{y^2}{x} = 3^2 = 9$	M1
		$y^2 = 9x$	A1
		sub. $y = 2x+1$ $(2x+1)^2 = 9x$	M1
		$4x^2 + 4x + 1 = 9x$	
		$4x^2 - 5x + 1 = 0$	
		$(4x-1)(x-1) = 0$	M1
		$x = \frac{1}{4}, 1$	A1
		$\therefore x = \frac{1}{4}, y = \frac{3}{2}$ or $x = 1, y = 3$	A1 (10)

9.	(a)	area of XS = $\frac{1}{2} \times (8x + 10x) \times x = 9x^2$	M1
		volume = $9x^2y = 900$	M1
		$\therefore y = \frac{100}{x^2}$	A1
	(b)	 width of sloping sides = $\sqrt{2}x$	B1
		$A = 8xy + 2(9x^2) + 2(\sqrt{2}xy)$	M1
		$A = 18x^2 + 2xy(4 + \sqrt{2})$	
		$A = 18x^2 + 2x(4 + \sqrt{2}) \times \frac{100}{x^2}$	M1
		$A = 18x^2 + \frac{200(4 + \sqrt{2})}{x}$	A1
	(c)	$\frac{dA}{dx} = 36x - 200(4 + \sqrt{2})x^{-2}$	M1 A1
		for SP, $36x - 200(4 + \sqrt{2})x^{-2} = 0$	M1
		$x^3 = \frac{200(4 + \sqrt{2})}{36}$	
		$x = \sqrt[3]{\frac{50(4 + \sqrt{2})}{9}} = 3.11$	A1
	(d)	$A = 522$ (3sf)	B1
		$\frac{d^2A}{dx^2} = 36 + 400(4 + \sqrt{2})x^{-3}$	M1
		when $x = 3.11, \frac{d^2A}{dx^2} = 108, \frac{d^2A}{dx^2} > 0 \therefore$ minimum	A1 (14)

Total (75)