Calculus II Sample Final Questions

1. Integrate the following

$$\begin{array}{rcl} (i) & \int \sin^2 x \, \cos^3 x \, dx & (ii) & \int x \ln x \, dx & (iv) & \int x \sin 2x \, dx \\ (iv) & \int \frac{dx}{x^2 + 3x + 2} \, dx & (v) & \int \frac{x}{\sqrt{1 - x^2}} \, dx & (vi) & \int_0^\infty x e^{-x^2} \, dx \\ (viii) & \int \frac{dx}{(x^2 + 1)^{3/2}} & (viii) & \int \frac{x \, dx}{(x - 1)(x - 2)^2} & (ix) & \int \frac{dx}{x \, (x^2 + 1)} \\ (x) & \int x \, e^{-3x} \, dx & (xi) & \int_0^1 \frac{dx}{\sqrt{1 - x^2}} & (xii) & \int \frac{dx}{x^2 \sqrt{x^2 - 4}} \end{array}$$

2. Do the following

3. Calculate the 4^{th} degree Taylor polynomial for the following. Expand about the point given.

(i)
$$f(x) = \sin x$$
 about $x = \pi/4$
(ii) $f(x) = \frac{1}{x+2}$ about $x = 1$

4. Determine the radius and interval of convergence of the following.

(i)
$$\sum_{n=1}^{\infty} \frac{(3x)^n}{(n+1)!}$$
 (ii) $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}x^n}{n4^n}$

5. Polar Areas

(i) Find the area inside both $r = \sin \theta$ an $r = \cos \theta$.

(ii) Find the area inside $r = 2\cos\theta$ and outside $r = 1/2 + \cos\theta$.

6. Planes and Lines

(i) Find the equation of the plane contains the lines

$$x = -1 + t, \quad x = 2 - s$$

 $y = 1 + t, \quad y = s$
 $z = 2t, \quad z = 2$

(ii) Find the equation of the plane that contains the points P(1, 1, 3), Q(-2, 4, -3) and R(3, -4, 4)

(iii) Find the equation of the line perpendicular to the plane in part (i) through the point *P*.

(iv) Find the equation of the line through *P* and *Q* in part (ii).

7. Vector Projections

Find the projection of \vec{u} onto \vec{v} and its orthogonal complement for the following:

(i)
$$\vec{u} = \langle -1, 3 \rangle$$
, $\vec{v} = \langle 2, 2 \rangle$,
(ii) $\vec{u} = \langle 5, 5 \rangle$, $\vec{v} = \langle 1, 2 \rangle$.