

Solomon Press
Core Mathematics C3
Paper F
(Mark Scheme)

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FOR EDEXCEL

GCE Examinations
Advanced Subsidiary

Core Mathematics C3

Paper F

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks could be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.

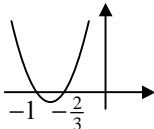
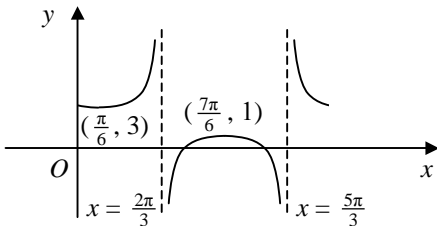


Written by Shaun Armstrong

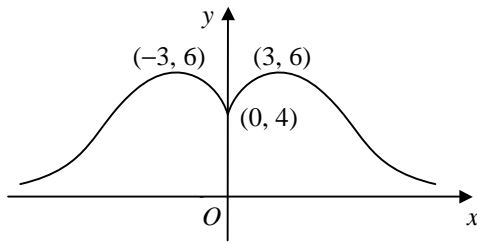
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C3 Paper F – Marking Guide

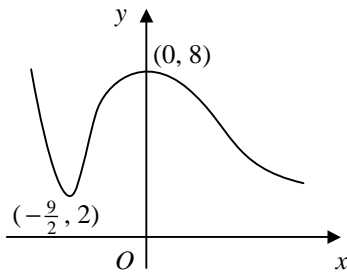
<p>1. $\frac{3}{\sin \theta} = -8 \cos \theta$ $3 = -8 \sin \theta \cos \theta = -4 \sin 2\theta$ $\sin 2\theta = -\frac{3}{4}$ $2\theta = 180 + 48.590, 360 - 48.590 = 228.590, 311.410$ $\theta = 114.3, 155.7$ (1dp)</p>	<p>M1 M1 A1 M1 A2</p>	<p>(6)</p>
<p>2. (a) $g(x) = (x+a)^2 - a^2 + 2$ $\therefore g(x) \geq 2 - a^2$</p> <p>(b) $gf(3) = g(1-3a) = (1-3a)^2 + 2a(1-3a) + 2$ $\therefore 1 - 6a + 9a^2 + 2a - 6a^2 + 2 = 7, \quad 3a^2 - 4a - 4 = 0$ $(3a+2)(a-2) = 0$ $a = -\frac{2}{3}, 2$</p>	<p>M1 A1 A1 M1 A1 M1 A1</p>	<p>(7)</p>
<p>3. (a) $3x + 1 = e^2$ $x = \frac{1}{3}(e^2 - 1)$</p> <p>(b) consider $\ln(3x^2 + 5x + 3) \geq 0$ $\Rightarrow 3x^2 + 5x + 3 \geq 1$ $3x^2 + 5x + 2 \geq 0$ $(3x+2)(x+1) \geq 0$ $x \leq -1$ or $x \geq -\frac{2}{3}$</p> <p>\therefore if (e.g.) $x = -\frac{3}{4}, \ln(3x^2 + 5x + 3) = \ln \frac{15}{16} = -0.0645\dots$ \therefore if $x = -\frac{3}{4}, \ln(3x^2 + 5x + 3) < 0 \quad \therefore$ statement is false</p>	<p>M1 M1 A1 M1 M1 A1 M1 A1</p> 	<p>(8)</p>
<p>4. (a) $\frac{dx}{dy} = 1 \times \sqrt{1-2y} + y \times \frac{1}{2}(1-2y)^{-\frac{1}{2}} \times (-2)$ $= \sqrt{1-2y} - \frac{y}{\sqrt{1-2y}} = \frac{(1-2y)-y}{\sqrt{1-2y}} = \frac{1-3y}{\sqrt{1-2y}}$ $\frac{dy}{dx} = 1 \div \frac{dx}{dy} = \frac{\sqrt{1-2y}}{1-3y}$</p> <p>(b) $y = -1, x = -\sqrt{3}, \text{grad} = \frac{1}{4}\sqrt{3}$ $\therefore y + 1 = \frac{1}{4}\sqrt{3}(x + \sqrt{3})$ $4y + 4 = \sqrt{3}x + 3$ $\sqrt{3}x - 4y - 1 = 0 \quad [p = -4, q = -1]$</p>	<p>M1 A1 M1 M1 A1 B1 M1 A1</p>	<p>(8)</p>
<p>5. (a) </p> <p>(b) $2 + \sec(x - \frac{\pi}{6}) = 0, \quad \sec(x - \frac{\pi}{6}) = -2, \quad \cos(x - \frac{\pi}{6}) = -\frac{1}{2}$ $x - \frac{\pi}{6} = \pi - \frac{\pi}{3}, \pi + \frac{\pi}{3} = \frac{2\pi}{3}, \frac{4\pi}{3}$ $x = \frac{5\pi}{6}, \frac{3\pi}{2}$</p>	<p>M2 A3 M1 B1 M1 A2</p>	<p>(10)</p>

6. (a)

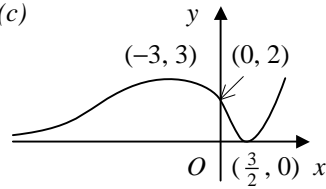


B3

(b)



(c)



M2 A2

M2 A2 (11)

7. (a)

$$\begin{aligned} f(x) &= 1 + \frac{4x}{2x-5} - \frac{15}{(2x-5)(x-1)} \\ &= \frac{2x^2 - 7x + 5 + 4x(x-1) - 15}{(2x-5)(x-1)} \\ &= \frac{6x^2 - 11x - 10}{(2x-5)(x-1)} = \frac{(3x+2)(2x-5)}{(2x-5)(x-1)} = \frac{3x+2}{x-1} \end{aligned}$$

B1

M1 A1

M1 A1

(b) $y = \frac{3x+2}{x-1}, \quad y(x-1) = 3x+2$

M1

$$x(y-3) = y+2$$

M1

$$x = \frac{y+2}{y-3}$$

$$\therefore f^{-1}(x) = \frac{x+2}{x-3}$$

A1

$$f(x) = \frac{3(x-1)+5}{x-1} = 3 + \frac{5}{x-1}$$

M1

$$x < 1 \quad \therefore f(x) < 3 \quad \therefore \text{domain of } f^{-1}(x) \text{ is } x \in \mathbb{R}, x < 3$$

A1

(c) $f(x) = 2 \Rightarrow x = f^{-1}(2) = -4$

M1 A1 (12)

8. (a)

$$\frac{dy}{dx} = 2x - \frac{1}{2}(4 + \ln x)^{-\frac{1}{2}} \times \frac{1}{x} = 2x - \frac{1}{2x\sqrt{4 + \ln x}}$$

M1 A1

$$x = 1, \quad y = -1, \quad \text{grad} = \frac{7}{4}$$

A1

$$\therefore y + 1 = \frac{7}{4}(x - 1)$$

M1

$$4y + 4 = 7x - 7$$

$$7x - 4y = 11$$

A1

(b) SP: $2x - \frac{1}{2x\sqrt{4 + \ln x}} = 0$

M1

$$\text{let } f(x) = 2x - \frac{1}{2x\sqrt{4 + \ln x}}, \quad f(0.3) = -0.40, \quad f(0.4) = 0.088$$

M1

sign change, $f(x)$ continuous \therefore root

A1

(c) $2x - \frac{1}{2x\sqrt{4 + \ln x}} = 0 \Rightarrow 2x = \frac{1}{2x\sqrt{4 + \ln x}}$

$$x^2 = \frac{1}{4\sqrt{4 + \ln x}} = \frac{1}{4}(4 + \ln x)^{-\frac{1}{2}}$$

M1

$$x = \sqrt{\frac{1}{4}(4 + \ln x)^{-\frac{1}{2}}} = \frac{1}{2}(4 + \ln x)^{-\frac{1}{4}}$$

A1

(d) $x_1 = 0.38151, x_2 = 0.37877, x_3 = 0.37900, x_4 = 0.37898$ (5dp)

M1 A2 (13)

Total (75)