

# Math 6345 Advanced ODEs

## Homework 5

1. Given the systems

$$\begin{aligned} (i) \quad \dot{x} &= -y - x^3, & \dot{y} &= x - y^3, \\ (ii) \quad \dot{x} &= -x - 2y^2, & \dot{y} &= xy - y^3, \\ (iii) \quad \dot{x} &= 2x + x^3 + 2x^2y + y^3, & \dot{y} &= x + x^2y + y^3, \end{aligned}$$

determine all critical points and classify them.

Hint: On (iii) try  $V = x^2 + axy + by^2$

Due. Tues. Nov 3, 2020