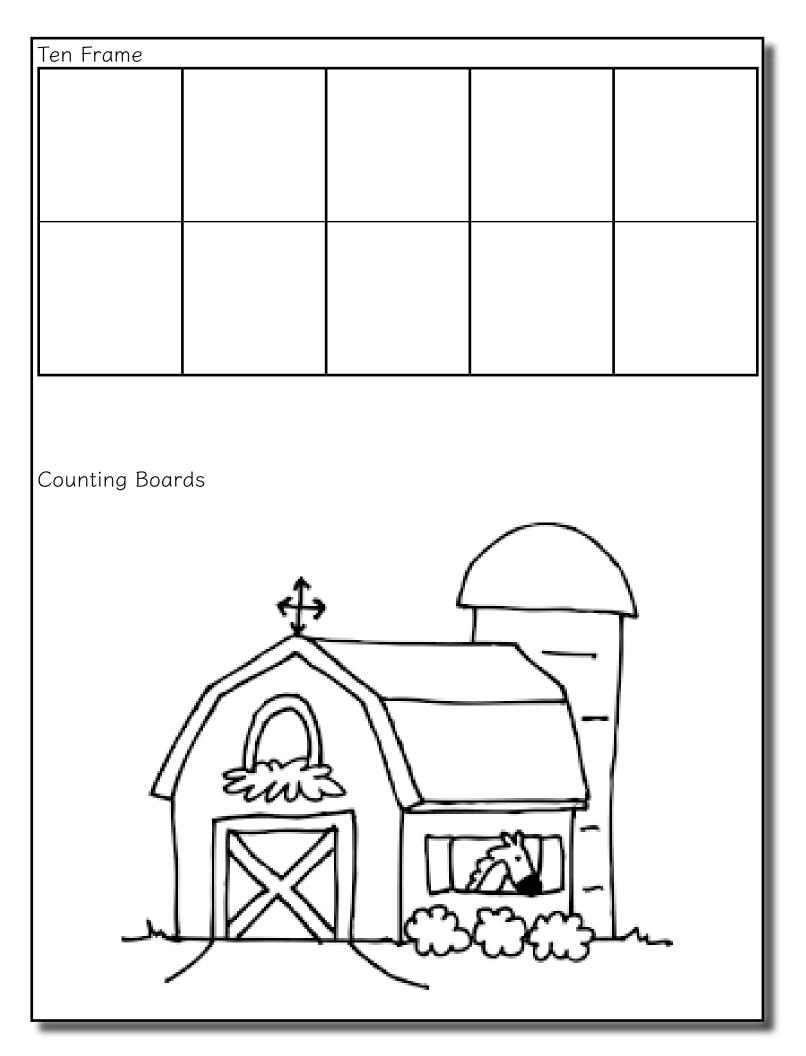
	Petersburg Math Cohort
	Summer 2022
	srpowell@utexas.edu @sarahpowellphd
	www.sarahpowellphd.com
Counting Prine	ciples
Stable Order	
One-to-One	
Correspondence	
Cardinality	
Abstraction	
Order Irrelevance	



Three Representations of N	umber			
Comparing Numbers		Build a Tower		6
	Less than	7	More than	6

Addition

Subtraction



Multiplication

Division

13 x 7 = 135 ÷ 5 =	 	

Fraction Concepts

Fraction	Length	Area	Set
<u>2</u> 3			
<u>1</u> 4			
$1\frac{1}{2}$			
<u>3</u> 7			

Improper Fractions and Mixed N	umbers	
Equivalent Fractions		
$\frac{1}{2}$	<u> </u>	
2	4	
Comparing Fractions		
<u>1</u> <u>3</u>	2 4	2 2
2 10	$\frac{2}{6}$ $\frac{4}{6}$	$\frac{2}{3} \frac{2}{5}$
	• •	
Ordering Fractions		
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		
8 5 3		

Fraction Computation: Addition and Subtraction

Problem	Representation
$\frac{1}{5} + \frac{3}{5}$	
$\frac{2}{3} + \frac{2}{3}$	
$\frac{1}{2} + \frac{1}{4}$	
$\frac{1}{4} + \frac{4}{6}$	
$\frac{4}{5} - \frac{1}{5}$	
$\frac{6}{5} - \frac{2}{5}$	
$\frac{7}{8} - \frac{2}{4}$	
$\frac{1}{2} - \frac{2}{5}$	

Fraction Computation: Multiplication	
Problem	Representation
$2 \times \frac{1}{4}$	
$\frac{1}{2} \times \frac{4}{4}$	
$\frac{1}{2} \times \frac{2}{4}$	
$\boxed{\frac{1}{2} \times \frac{3}{4}}$	
$\frac{2}{3} \times \frac{3}{3}$	
$\frac{2}{5} \times \frac{5}{6}$	
$\frac{1}{4} \times \frac{2}{3}$	
$\frac{3}{4} \times \frac{1}{3}$	
L	

Fraction Co Division	omputation:
Problem	Representation
$\frac{3}{3}$ ÷ 3	
$\frac{3}{3} \div \frac{1}{3}$	
$\frac{2}{3} \div \frac{1}{3}$	
$\frac{5}{6} \div \frac{1}{2}$	
$\frac{7}{8} \div \frac{3}{4}$	
$\frac{1}{4} \div \frac{1}{2}$	
$\frac{3}{4} \div \frac{2}{3}$	
$\frac{4}{5} \div \frac{1}{2}$	

	Decimals	
		Thousandths
		Hundredths
1.034 0.829		Tenths
0.88 1.04		
1.2 2.8		Ones

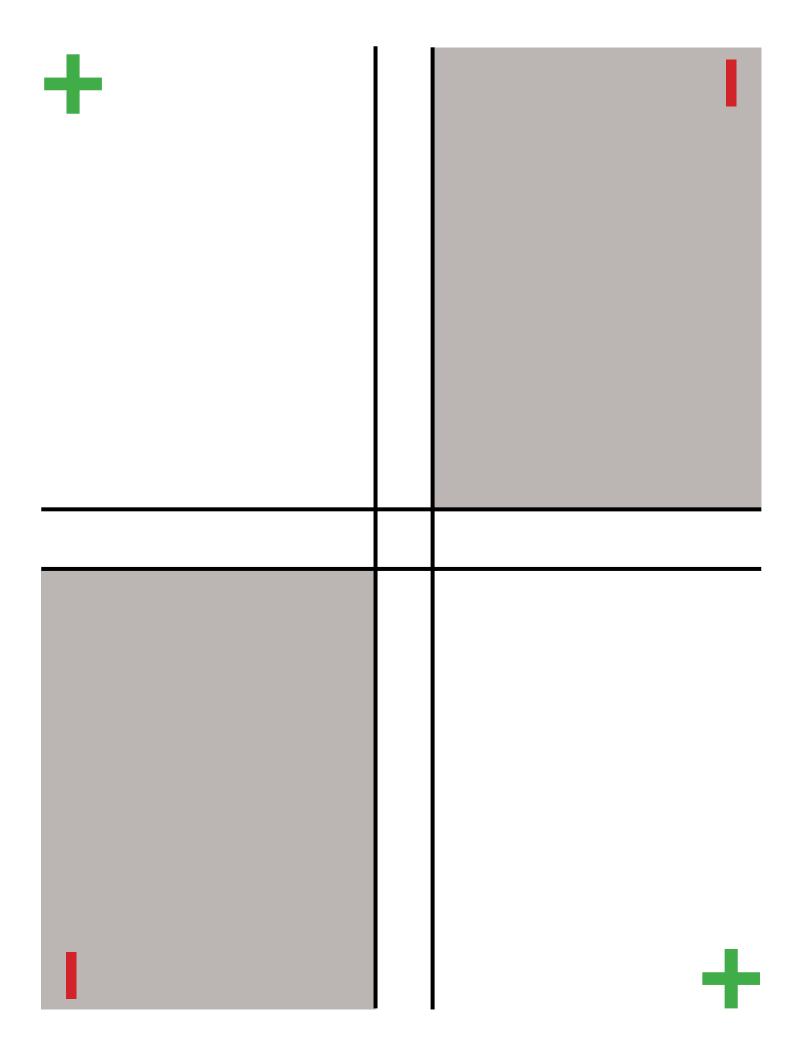
Decimal Computation	
Problem	Representation
2.34 <u>+ 1.61</u>	
1.98	
<u>+ 0.34</u>	
2.34 <u>– 1.61</u>	
3.09 <u>- 1.88</u>	

Decimal Computation		
Problem	Representation	
0.52 <u>× 3</u>		
0.52 <u>× 34</u>		
1.24 ÷ 2		
1.27 ÷ 5		

Integers		
Addition		
Problem	Representation	
3 + 5		
3 + (-5)		
3 + (-5)		
3 + (-5)		
-2 + 6		
-6 + (-3)		
3 + (-1)		

Integers			
Subtractio	Subtraction		
Problem	Representation		
5 – 3			
-3 – 4			
-3 – 4			
-3 – 4			
2 – 5			
-2 – (-6)			
-3 – 2			

Integers		
Multiplication and Division		
Problem	Representation	
2(3)		
(2)(-3)		
(-2)(-3)		
9 ÷ 3		
9 ÷ (-3)		
-9 ÷ (-3)		



Showing Expressions		
Problem	With Cups/Plates and Counters Problem Representations	
x + 4		
y – 6		
2(x)		

With Algebra Tiles

Problem	Representations	
x + 4		
у – б		
2(x)		

With Algeblocks

Problem	Representations	
x + 4		
у – б		
2(x)		

	Solving Equations
With Cups/Plates and Counters	
Problem	Representations
x + 2 = 5	
x + 2 = 5	
4 + x = 6	
5 = x - 3	
-2 = x + 3	
With Algebra Ti	les
Problem	Representations
x + 2 = 5	
4 + x = 6	
x + 3 = 7	
y – 4 = 2	
5 = x - 3 y - 2 = 5	

With Algeblocks Problem Representations $x + 2 = 5$		Solving Equations
x + 2 = 5 $4 + x = 6$ $-2 = x + 3$ $-1 = y - 4$ $2x + 2 = 6$ $x + 4 = 3x$ $2(x + 3) = x + 4$ $2x - 4 = 1 + 3x$ $3y - 5 = -y - 1$	With Algeblocks	
4 + x = 6 $-2 = x + 3$ $-1 = y - 4$ $2x + 2 = 6$ $x + 4 = 3x$ $2(x + 3) = x + 4$ $2x - 4 = 1 + 3x$ $3y - 5 = -y - 1$	Problem	Representations
-2 = x + 3 $-1 = y - 4$ $2x + 2 = 6$ $x + 4 = 3x$ $2(x + 3) = x + 4$ $2x - 4 = 1 + 3x$ $3y - 5 = -y - 1$	x + 2 = 5	
-1 = y - 4 $2x + 2 = 6$ $x + 4 = 3x$ $2(x + 3) = x + 4$ $2x - 4 = 1 + 3x$ $3y - 5 = -y - 1$	4 + x = 6	
2x + 2 = 6 $x + 4 = 3x$ $2(x + 3) = x + 4$ $2x - 4 = 1 + 3x$ $3y - 5 = -y - 1$	-2 = x + 3	
x + 4 = 3x $2(x + 3) = x + 4$ $2x - 4 = 1 + 3x$ $3y - 5 = -y - 1$	-1 = y - 4	
2(x + 3) = x + 4 $2x - 4 = 1 + 3x$ $3y - 5 = -y - 1$	2x + 2 = 6	
2x - 4 = 1 + 3x $3y - 5 = -y - 1$	x + 4 = 3x	
3y - 5 = -y - 1	2(x+3) = x+4	
	2x - 4 = 1 + 3x	
1 - x = x + 1	3y – 5 = -y – 1	
	1 - x = x + 1	

Solving Equations	
With Algeblocks	
Problem	Representation
x(3)	
-2(y)	
x(1 + x)	
-y(y + 2)	
(x – 2)(-2x)	
(y – 1)(y + 2)	
3y ÷ 3	
-2xy÷y	
-3x ÷ 3x	
4x ² ÷ − x	