CASE STUDY ANALYSIS OF TWO STAGE PLANETARY GEARBOX VIBRATION

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Abstract: A two stage planetary gearbox used in underground coal mining experienced an overload in service which caused bearing and bolting failures. The gearbox was repaired and underwent a no load spin test. A very audible noise was present in the vicinity of the 1st stage gear set. Vibration analysis was used to determine the source of the vibration. The equations for calculating the planetary gear shaft speeds, gear meshing frequencies, and bearing frequencies in the gearbox are provided.

Keywords: Gearbox, gearmesh, planetary, epicyclic, planet passing

Background: Gearboxes used in underground coal mining are of compact design. A typical two stage planetary gearbox, 800 HP, 40.173:1 Ratio with 1800 RPM input is shown in Figure 1. The unit was received by a repair facility for rebuild following failure from an overload incident. It was reported that the bearings were replaced and that one bearing had broken into many fragments. Following repairs a no load spin test of the gearbox was performed as a check for bearing faults, Figure 2. There was an audible impacting type noise from the input planetary section.

Analysis: During the spin test, vibration data was measured using an accelerometer with a rare earth magnetic mount. Initial inspection of the data indicated impacting and ringing of natural frequencies of the gearbox, Figure 3. The impacts measured a 221.87 mSec period or 4.507 Hz ~ 704.6 CPM. The FFT of the time domain data showed harmonics of 704.6 CPM, and indication of excitation of several natural frequencies of the gearbox.
Before a determination of the source of the vibration could be made, an understanding of the gearbox design was required as well as calculation of the excitation frequencies. Based on the information provided by the drawing shown in Figure 1, several calculations were made to obtain the shaft speeds, bearing fault frequencies, and gear meshing frequencies.

Epicyclic gear boxes derive their name from the epicycloidal curves that the planet gears produce during rotation. There are three general types of epicyclic arrangements: 1) planetary which consists of a stationary ring gear combined with a rotating sun gear and moving planet carrier, 2) star configuration which consists of a stationary planet carrier coupled with a rotating sun gear, and 3) solar gear that has a fixed sun gear combined with a moving ring gear and planet carrier. The planetary arrangement is most common and is shown by the schematic in Figure 4. The subject gearbox had the planetary arrangement for the 1st and 2nd stages. Input was from the sun with three planets supported by a carrier revolving about the sun pinion and the ring gear fixed.
### Table 1: Summary of The Gearbox Shaft Speeds and Gear Meshing frequencies.

<table>
<thead>
<tr>
<th></th>
<th>1st Stage</th>
<th>2nd Stage</th>
</tr>
</thead>
<tbody>
<tr>
<td>S&lt;sub&gt;S&lt;/sub&gt;</td>
<td>Sun Gear RPM (Input Speed)</td>
<td>1782</td>
</tr>
<tr>
<td>R&lt;sub&gt;T&lt;/sub&gt;</td>
<td>Ring Gear Teeth</td>
<td>112</td>
</tr>
<tr>
<td>P&lt;sub&gt;T&lt;/sub&gt;</td>
<td>Planet Gear Teeth</td>
<td>47</td>
</tr>
<tr>
<td>S&lt;sub&gt;T&lt;/sub&gt;</td>
<td>Sun Gear Teeth</td>
<td>17</td>
</tr>
<tr>
<td>T&lt;sub&gt;Value&lt;/sub&gt;</td>
<td>Train Value</td>
<td>0.151786</td>
</tr>
<tr>
<td>C&lt;sub&gt;S&lt;/sub&gt;</td>
<td>Carrier RPM</td>
<td>-234.837</td>
</tr>
<tr>
<td>P&lt;sub&gt;S&lt;/sub&gt;</td>
<td>Planet RPM</td>
<td>559.612</td>
</tr>
<tr>
<td>P&lt;sub&gt;Subabsolute&lt;/sub&gt;</td>
<td>Planet RPM Absolute</td>
<td>-324.775</td>
</tr>
<tr>
<td>R&lt;sub&gt;S&lt;/sub&gt;</td>
<td>Ring Gear RPM</td>
<td>0</td>
</tr>
<tr>
<td>P&lt;sub&gt;GMF&lt;/sub&gt;</td>
<td>Planet Gear Meshing Freq CPM</td>
<td>26,301.76</td>
</tr>
<tr>
<td>F&lt;sub&gt;GMF-Sun&lt;/sub&gt;</td>
<td>Sun Gear Meshing Freq CPM</td>
<td>30,294.00</td>
</tr>
<tr>
<td>Ratio</td>
<td>Stage Ratio</td>
<td>7.5882</td>
</tr>
</tbody>
</table>

### Step 1: Carrier Speed

The 1<sup>st</sup> stage carrier speed can be calculated using equation (1) and (2).

**Train value:**

\[
T_{\text{Value}} = \frac{S_T \times P_T}{P_T \times R_T} = \frac{S_T}{R_T} = \frac{17}{112} = 0.15179
\]  

(1)

The 1<sup>st</sup> stage Carrier Speed was then calculated using equation (2).

\[
C_s = \frac{R_S - T_{\text{Value}} \times S_S}{1 + T_{\text{Value}}} = \frac{-0.15179 \times 1782}{1 + 0.15179} = \frac{-270.48978}{1.15179} = -234.8372 \text{ RPM}
\]  

(2)

The negative “-“ simply indicates the carrier is rotating in the opposite direction of the sun gear.
The 2nd stage carrier speed which is also the output of the gearbox was calculated in the same manner using equations (1) and (2).

\[ T_{value} = \frac{S_T \times P_T}{P_T \times R_T} = \frac{17}{73} = 0.23288 \quad (1) \]

\[ C_S = \frac{R_S - T_{value} \times S_S}{1 + T_{value}} = \frac{-0.23288 \times 234.8376}{1 + 0.2328767} = \frac{-54.6882}{1.2328767} = -44.3582 \text{ RPM} \quad (2) \]

The gearbox ratio was calculated using equation (3).

\[ Ratio = \frac{Input_{RPM}}{Output_{RPM}} = \frac{1782}{44.35814} = 40.1730 \quad (3) \]

The calculated ratio agreed with the ratio provided by the gearbox manufacture of 40.173.

The carrier speed and ratio can also be calculated as follows:

The 1st stage ratio was calculated using equations (4), (5) and (6).

\[ R_O = \frac{R_S + S_s}{S_s} = \frac{112 + 17}{17} = 7.5882 \quad (4) \]

\[ R_O = \frac{1}{T_{value}} + 1 = \frac{1}{0.15179} + 1 = 7.5882 \quad (5) \]

The carrier speeds can also be calculated using equations (7), (8) and (9)

\[ C_S = \frac{-R_O}{S_O} = \frac{-234.838}{7.5882} = -234.838 \text{ RPM} \quad (7) \]

\[ C_S = \frac{S_S}{R_O} = \frac{1782}{(R_T \div S_T) + 1} = \frac{1782}{(112 \div 17) + 1} = 234.838 \text{ RPM} \quad (8) \]

\[ C_S = \frac{-S_S}{1 + \frac{1}{T_{value}}} = \frac{-1782}{1 + \frac{1}{0.15179}} = 234.838 \text{ RPM} \quad (9) \]

The 2nd stage ratio and carrier speed were calculated using equations (4) and (6).

\[ R_O = \frac{R_S + S_s}{S_s} = \frac{73 + 17}{17} = 5.2941 \quad (4) \]

\[ C_S = \frac{S_S}{R_O} = \frac{234.838}{5.2941} = 44.3581 \text{ RPM} \quad (6) \]
Step 2: Planet Speed

The 1st stage planet rotational frequency or planet spin speed was calculated using equation (10).

\[ P_s = C_s \cdot \frac{R_t}{P_t} = -234.838 \cdot \frac{112}{47} = -559.6121 \text{ RPM} \] (10)

The 1st stage absolute planet rotational frequency can be determined by summing the carrier and planet rotational frequencies algebraically, as shown by equation (11). Note that this frequency seldom appears in vibration data.

\[ P_{s, \text{absolute}} = C_s + P_s = -234.838 + (-559.612) = 324.7749 \text{ RPM} \] (11)

The 2nd stage planet spin speed was calculated using equation (10).

\[ P_s = C_s \cdot \frac{R_t}{P_t} = 44.3594 \cdot \frac{73}{27} = 119.935 \text{ RPM} \] (10)

The 2nd stage absolute planet rotational frequency was then determined using equation (11).

\[ P_{s, \text{absolute}} = C_s + P_s = -44.358 + 119.935 = 75.577 \text{ RPM} \] (11)

The planet speed in each stage can also be calculated using equation (12).

1st stage planet RPM:

\[ P_R = \frac{R_s}{P_t} \cdot (R_s - C_s) = \frac{112}{47} \cdot (-234.838) = -559.6121 \text{ RPM} \] (12)

The 2nd stage planet RPM was calculated in the same manner.

\[ P_R = \frac{R_s}{P_t} \cdot (R_s - C_s) = \frac{73}{27} \cdot (-44.3594) = -119.9313 \text{ RPM} \] (12)
Step 3: Gear Meshing Frequencies

The planet gear meshing frequencies were then determined for stage 1 using equation (13).

\[ P_{GMF} = P_s \times P_r = 559.612 \times 47 = 26,301.76 \text{ CPM} \] (13)

The higher frequency sun gear meshing frequency is the product of the sun gear teeth and rotational frequency of the sun gear and was calculated using equation (14).

\[ S_{GMF} = S_s \times S_r = 1782 \times 17 = 30,294.00 \text{ CPM} \] (14)

The 2\textsuperscript{nd} stage planet gear meshing frequencies were then calculated using equation (13).

\[ P_{GMF} = P_s \times P_r = 119.931 \times 27 = 3,238.144 \text{ CPM} \] (13)

And finally, the 2\textsuperscript{nd} stage sun gear meshing frequency was calculated using equation (14).

\[ S_{GMF} = S_s \times S_r = 234.8376 \times 17 = 3,992.23 \text{ CPM} \] (14)

Step 4: Bearing Fault Frequencies

After the gearbox shaft speeds were determined, the bearing fault frequencies were calculated and are listed in Table 2. For purposes of calculating the bearing fault frequencies of the planet bearings, the spin frequency of the planets must be summed to the carrier rotational frequency. Since the outer race was turning faster than the inner race, the calculations were made as if the bearing inner race was not rotating.

Stage 1 Planet Spin Freq 559.612 + 234.838 = 794.45 RPM
Stage 2 Planet Spin Freq 119.931 + 44.359 = 164.29 RPM

Note that time did not permit determination of the dimensions for the cylindrical roller bearing NUP 3972.

<table>
<thead>
<tr>
<th>Component</th>
<th>1X Brg Fault Frequencies CPM</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Brg Inner Race RPM (Relative to Outer Race)</td>
</tr>
<tr>
<td>Sun NU228E</td>
<td>1782.00</td>
</tr>
<tr>
<td>Sun 6226</td>
<td>1782.00</td>
</tr>
<tr>
<td>1st Stage Planet NJ314</td>
<td>794.45</td>
</tr>
<tr>
<td>Output Carrier NCF 1864B</td>
<td>44.36</td>
</tr>
<tr>
<td>Output Carrier NUP 3972</td>
<td>44.36</td>
</tr>
<tr>
<td>2nd Stage Planet JN2318</td>
<td>164.29</td>
</tr>
</tbody>
</table>

Table 2: Listing of Gearbox Bearings and Fault Frequencies CPM.
The bearing fault frequencies were calculated using Machinery Health Manager Ref 3 software (CSI RBMware Ref 3). Equations from Reference 2 are provided below.

Where:

\[
\text{Cage}_{Hz} = \frac{n}{2} \left[ 1 - \left( \frac{d}{P.D.} \right) \cos \alpha \right]
\]

(13)

\[
\text{Ball Spin}_{Hz} = \frac{P.D.}{d} \cdot \frac{n}{2} \left[ 1 - \left( \frac{d}{P.D.} \right)^2 \cos^2 \alpha \right]
\]

(14)

\[
\text{Ball Pass}_{\text{Outer Race}}_{Hz} = Z \cdot \frac{n}{2} \left[ 1 - \left( \frac{d}{P.D.} \right) \cos \alpha \right]
\]

(15)

\[
\text{Ball Pass}_{\text{Inner Race}}_{Hz} = Z \cdot \frac{n}{2} \left[ 1 + \left( \frac{d}{P.D.} \right) \cos \alpha \right]
\]

(16)

\[d = \text{Rolling Element Diameter}\]
\[n = \text{Shaft Frequency} \frac{\text{Cycles}}{\text{sec}} \text{ or } \left( \frac{\text{RPM}}{60} \right) , \text{Hz}\]
\[P.D. = \text{Pitch Diameter} \text{ (For ball bearings } P.D. = \frac{O.D. + \text{bore}}{2})\]
\[Z = \text{Number of balls or rollers (per row)}\]
\[\alpha = \text{Bearing contact angle} 0 \text{ deg} \text{ for pure radial load}\]
\[\alpha = 15 \text{ to } 20 \text{ deg (thinner – section bearings)}\]
\[\alpha = 37 \text{ to } 40 \text{ deg (73, 74 Series)}\]
\[\alpha = 10 \text{ to } 15 \text{ deg spherical roller typical range}\]

**Step 5: Determination of Vibration Source**

Referring to the data plots in Figure 3, it was readily determined using the vibration software cursors that the impulse frequency was 4.407 Hz ~ 704.6 CPM. A check of the frequencies in Table 2 showed that this frequency does not match any of the bearing fault frequencies.

A check of the gearbox shaft speeds and gear meshing frequencies in Table 1 also did not immediately identify a forcing frequency. The pulses in the time domain measured 85.42 mSec ~ 11.7 Hz ~ 702.4 CPM. Since the gearbox has three planets in each stage an impulse could occur at three times the 1st stage carrier frequency of 234.838 CPM if there was damage to the ring gear teeth. This frequency was calculated as follows:

\[3 \times 234.8372 = 704.5 \text{ CPM} \sim 11.74 \text{ Hz}, \quad \frac{1}{11.74 \text{Hz}} = 0.08517 \text{Sec} \sim 85.17 \text{mSec}\]

The source of the pulses was related to rotation of the carrier and the three planets in the 1st stage also called the planet passing frequency.
Updating Table 1 to include the planet passing frequency $P_{\text{Pass}}$, Table 1A:

<table>
<thead>
<tr>
<th></th>
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<th>2nd Stage</th>
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<tbody>
<tr>
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<td>Sun Gear RPM (Input Speed)</td>
<td>1782</td>
</tr>
<tr>
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<td>Ring Gear Teeth</td>
<td>112</td>
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<tr>
<td>$P_T$</td>
<td>Planet Gear Teeth</td>
<td>47</td>
</tr>
<tr>
<td>$S_T$</td>
<td>Sun Gear Teeth</td>
<td>17</td>
</tr>
<tr>
<td>$T_{\text{value}}$</td>
<td>Train Value</td>
<td>-0.151786</td>
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<tr>
<td>$C_S$</td>
<td>Carrier RPM</td>
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</tr>
<tr>
<td>$P_S$</td>
<td>Planet RPM</td>
<td>559.6121</td>
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<tr>
<td>$P_{\text{absolute}}$</td>
<td>Planet RPM Absolute</td>
<td>-324.775</td>
</tr>
<tr>
<td>$R_S$</td>
<td>Ring Gear RPM</td>
<td>0</td>
</tr>
<tr>
<td>$P_{\text{GMF}}$</td>
<td>Planet Gear Meshing Freq CPM</td>
<td>26,301.77</td>
</tr>
<tr>
<td>$F_{\text{GMF-Sun}}$</td>
<td>Sun Gear Meshing Freq CPM</td>
<td>30,294.00</td>
</tr>
<tr>
<td>$P_{\text{Pass}}$</td>
<td>Planet Passing Freq</td>
<td>704.514</td>
</tr>
<tr>
<td>Ratio</td>
<td>Stage Ratio</td>
<td>7.5882</td>
</tr>
<tr>
<td>Ratio</td>
<td>Gearbox Ratio</td>
<td>40.17301:1</td>
</tr>
</tbody>
</table>

Table 1A: Summary of the Gearbox Shaft Speeds, Gear Meshing and Planet Passing Frequencies.

Expanding the time domain plot to show only two pulses, Figure 5, the pulses ring down which is typical response of structural resonance. The spectrum data also provided clear indication of resonance excitation.

Figure 5. Time Data Expanded To Show Impacting and Ring Down.
Plotting a single pulse in Figure 6 showed more clearly the time between oscillations was about 1.042 mSec or 57,600 CPM. Note that spectrum analyzers do not make good oscilloscopes due to the rather coarse sampling at 2.56 times the maximum frequency to be displayed in the frequency spectrum.

Plotting the time data in a circular plot, Figure 7, clearly shows three periodic impacts per revolution of the carrier. The impacts occurred as each planet rolled over a damaged ring gear tooth.

Figure 6. Expanded Plot of One of The Impact Events in The Time Domain Shows The Ring Down Frequency Is About 57,600 CPM.

Figure 7. Time Domain Data Plotted in Circular Format.
Peakvue spectrum and time domain data are plotted in Figure 8 and shows impacting to be about 5g’s with the same frequency content as the normal vibration data. The auto correlation plot of Peakvue time data is plotted in Figure 9 in a circular plot format.

Figure 8. PeakVue Data Also Contained Impacting Data At the 3X the Carrier RPM.

Figure 9. Auto Correlation of Peakvue Time Data.
After reviewing the data and calculations, the conclusions were as follows:

1) The 1st stage carrier was impacting a stationary object three times each revolution, or

2) Each planet gear in the 1st stage was rolling over damaged teeth on the ring gear.

No gear meshing frequencies were evident in the data. Opening of the gearbox for inspection of the 1st stage was recommended.

**Gearbox Inspection:**

With the likely problem area in the gearbox identified, the gearbox was disassembled for inspection. A small fragment of the disintegrated bearing race was found imbedded in the unloaded side of one tooth of the ring gear. The bearing fragment was removed, the damaged tooth dressed, the gearbox reassembled and spin tested again.

Before and after vibration data are plotted in Figures 9 & 10. The periodic impacting caused by the planet teeth rolling over the damaged ring gear tooth was reduced.

![Figure 9. Initial Spectrum And Time Domain Data With Brg Fragment Imbedded In The Ring Gear.](image-url)
A photo of the damaged ring gear tooth is shown in Figure 11 after dressing. Indentations can be seen where the tooth material was compressed by the bearing fragments.

Conclusions:

This article describes the process that was used to analyze impacting type vibration of a two stage epicyclic planetary gearbox during a post-repair unloaded spin test. The forcing frequencies were calculated and identified the probable source of the vibration. Inspection of the ring gear identified fragments of a bearing race embedded in the unloaded side of a ring gear tooth.

Special thanks to Jim Maddrey for reviewing this article, providing some of the equations and his helpful comments.

References: