

A comprehensive review on process optimization of composite moulding processes

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Abstract

A review on numerical optimization of parameters involved in mould filling, and curing that affects a class of composite moulding processes, namely Liquid Composite Moulding (LCM) processes are presented. The critical issues and prevention techniques of the entire process cycle are discussed to manufacture a void-free and cost-effective composite part. The key parameters discussed under mould filling stage are preform parameters such as permeability and porosity, gate and vent location, injection pressure, and mould geometry. Whereas, the key parameters discussed under curing stage are degree of cure, mould temperature and viscosity of resin. The number of single objective and multi-objective optimization techniques have been developed to optimize the objectives like the degree of cure, temperature overshoot, process time, gate and vent location and mould fill time. The Nelder mead simplex method, simulated annealing, GA, NSGA-II, and MOOGA are the most used traditional techniques for optimizing the process as well as mould parameters. The scope of meta-heuristic or hybrid optimization techniques for constrained single and multi-objective optimization problem in the LCM process has addressed.

Keywords: Composite processing; cure kinetics; mould filling; numerical optimization; stochastic techniques.

1. Introduction

The designing of composite process parameters has become crucial factor in different industries with increase in applications of composite materials in vital sectors. There have been various composite part manufacturing techniques from traditional methods like hand-layup which is cost and labour intensive to the use of automated techniques such as autoclave, injection moulding, extrusion and liquid composite moulding (LCM) process etc. [1–3]. Although, each technique has different manufacturing procedure, the major objectives and design parameters will be same to manufacture the cost effective void free composite part. In this article we will mainly focusing on the LCM process parameters, as this method is effective in manufacturing properly finished composite parts with complex geometries [4-8].

LCM is a closed moulding process, hence after closing the mould, it is difficult to know whether fibre preform has impregnated with resin or there are unsaturated regions where the air has entrapped [9]. Therefore it is important to identify and optimize the parameters during the process as depicted in figure 1.

This paper addresses following research questions for making the cost effective and void free composite part using LCM process.

Research questions

- Which factors need to consider to manufacture a void free cost effective composite part?
- Why there is need to develop meta-heuristic techniques over traditional numerical techniques?
- What advancements needed in meta-heuristic techniques for optimizing LCM process parameters for constrained single and multi-objective optimization problem?

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Following objectives formed to address these questions.

Objectives:

- To analyze the effect of mould, raw material, and process parameters on mould fill time and cure time
- To develop proper optimization technique for addressing the full-fledged complex and non-linear optimization problem
- Development of effective hybrid MOO algorithm to optimize the objectives related to mould fill time with minimum void content and cure time with given temperature range

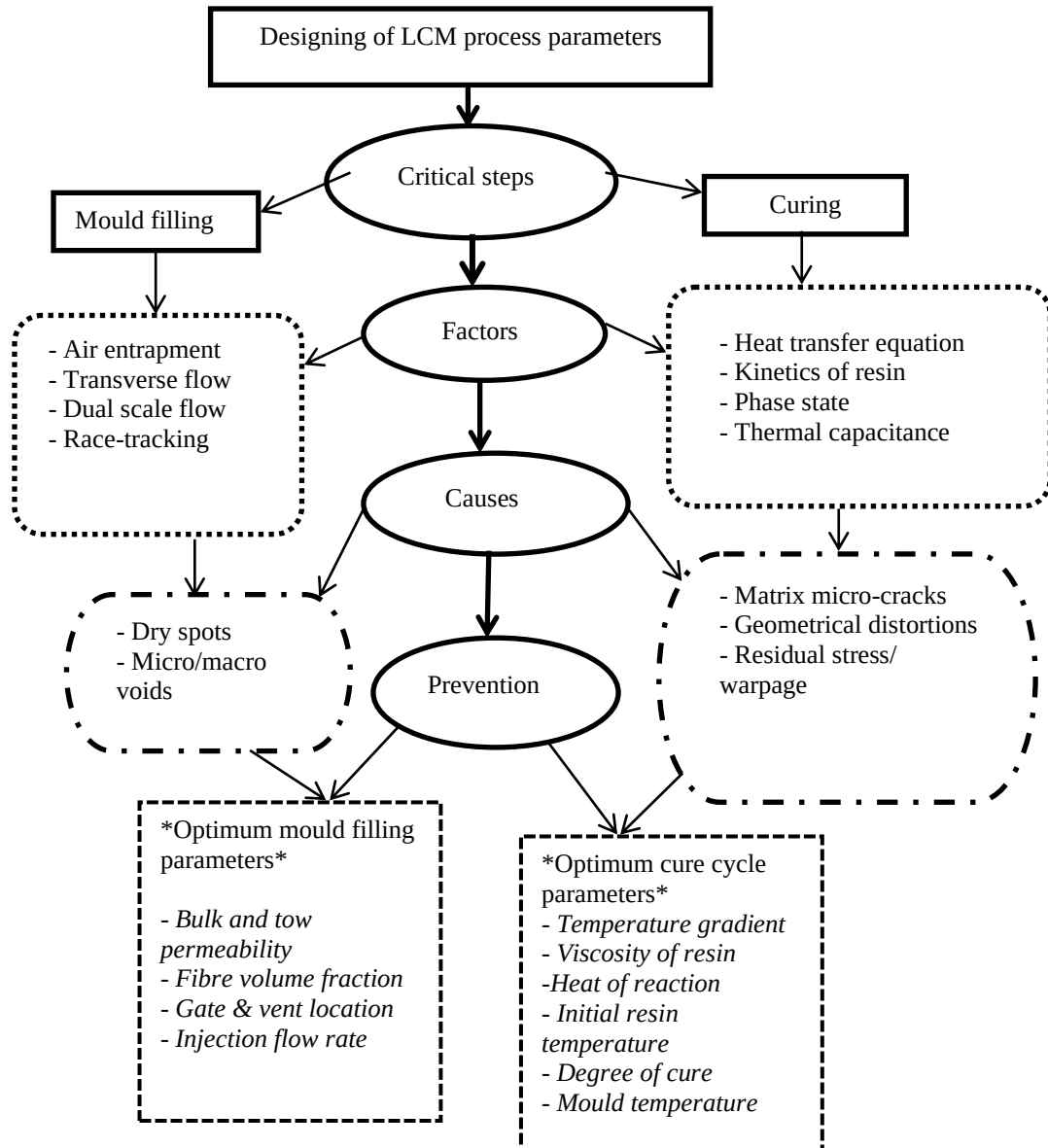


Fig. 1. Flow diagram depicting designing of LCM process parameters

In the LCM process, mould filling and curing are the critical steps [10-12]. The factors which affect during the mould filling stage are air entrapment, transverse flow, race tracking effect and dual scale flow [13]. Air entrapment arises due to non-uniform impregnation of fibre preform with resin. Usually, composite structures are very thin hence flow along the thickness direction has been considered negligible. However, when the in-plane permeability component of fibre preform along the thickness direction will change significantly then the transverse flow has to take into account [14]. When air channels will be present between the mould wall and fibre preform the race-tracking occurs. This effect arises mainly along mould wall edges, joints, inserts and around ribs for complex structures. When there is a difference between the fluid flow within the fibre tows and in between the tows the dual scale flow arise [15, 16]. Due to these defects voids and dry spots forms in the composite part as shown in figure 2 [17]. Therefore, proper selection of bulk and tow permeability, gate and vent location, porosity and injection pressure/flow rate need to take into account [18-23].

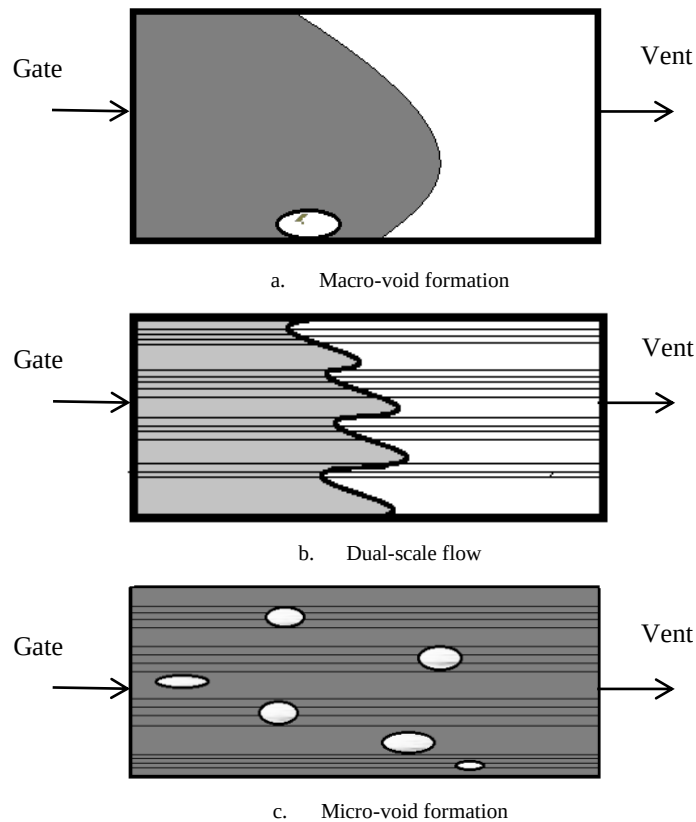


Fig. 2 (a, b, c). Flow issues in LCM Process

Curing is an exothermic process where heat transfer occurs between mould and saturated preform. With an increase in temperature of saturated preform liquid resin will convert to gel and then gel to solid this phase transition called as gelation and solidification respectively [24-27]. The factors which affect the curing process are temperature overshoot, glass transition temperature during phase change, and resin viscosity [28, 29]. This may develop the temperature and cure gradients along thick sectioned parts which results to matrix micro-cracks, residual stresses and geometrical distortions [30-35].

Numerous numerical techniques used by researchers to optimize the mould filling and curing parameters of LCM process [36, 37]. We found few review articles, book chapters and thesis chapters related to numerical optimization of composite process parameters [38]. They are particularly specified to some application based on use of traditional numerical techniques. To

the best of our knowledge we did not find review article in last ten years addressing use of meta-heuristic or hybrid optimization techniques for constrained single and multi-objective optimization problem in the LCM process.

This article describes the comprehensive review on identification of problem statement, formulation of optimization problem and use of suitable optimization technique based on the type of optimization problem in the composite processing. Depending on the accomplishment of target objectives, design parameters need to set. Then, we will present the different types of optimization techniques used for optimizing the different parameters of LCM processes. After that, to optimize the different conflicting objectives simultaneously the studies on multi-objective optimization (MOO) in composite processing has been reviewed. Here, the combination of different mould parameters, cure parameters and both mould and cure parameters optimized simultaneously.

2. Numerical optimization for composite processing

2.1. General formulation of optimization problem

Generally, the optimization problem formulated as,

$$\max/\min_x f_k(X) \quad k = 1, 2, \dots, N \quad (1)$$

Subject to,

$$\begin{aligned} h_l(X) &= 0 & l &= 1, 2, \dots, L \\ g_m(X) &\leq 0 & m &= 1, 2, \dots, M \\ lb &\leq X \leq ub & X &= (x_1, x_2, \dots, x_d)^T \end{aligned}$$

here, $f_k(X)$ is the scalar objective function which has to maximize or minimize, $h_l(X)$ represents the J number of equality constraints also called active constraints, $g_m(X)$ represents the M number of inequality constraints and X is the vector of d -dimensional design variables.

For the sake of understanding and correlation we have discussed the mathematical formulation of one example based on composite process parameter optimization. Jahromi et al. [39] used a dynamic artificial neural network (ANN) for achieving the uniform temperature and degree of cure for thick fibre reinforced composite parts, which is directly dependent on the temperature profile of mould wall. The objective function was formulated to minimize the temperature gradients between two selected points i.e. central and corner, to indicate the overall cure process subject to constraints on the degree of cure. Mathematically,

$$\min \sum_{i=1}^n (T_{i(\text{center})} - T_{i(\text{corner})})^2 \quad (2)$$

Subject to,

$$\begin{aligned} \alpha_{\text{corner}} &\geq \alpha_{\text{crit}} \\ \text{where } \alpha_{\text{crit}} &= 0.8 \\ 298 \text{ K} &\leq T_i \leq 430 \text{ K} \quad i = 1, 2, \dots, 5. \end{aligned}$$

2.2. Classification of optimization techniques

After the formulation of the optimization problem, the task is to solve it using an appropriate optimization technique. There are different types of optimization techniques based on the nature of optimization problem they can be classified as [40]:

- I. Deterministic techniques: These techniques are very effective for achieving good convergence. For highly non-linear and complex problems they may stick in the local optima.
- II. Stochastic algorithms: These techniques are very effective for achieving the global optimal solution [41-43].
- III. Hybrid algorithms: These types of algorithms used for achieving better convergence as well as the global optimal solution. Usually, Deterministic techniques and stochastic techniques are combined by taking into account the convergence property of the deterministic algorithm and exploration property of the stochastic algorithm as shown in figure 3. In composite processing, different optimization problems have been addressed in the literature using this method. For example, a hybrid GA-gradient based algorithm used to optimize the gate location, on the flow channels.

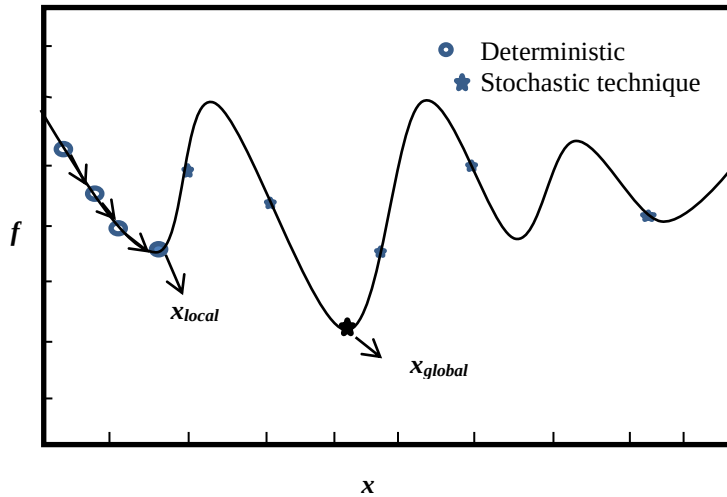


Fig. 3. Convergence flow of optimal solution for stochastic and deterministic techniques

3. Numerical studies on optimization

3.1. Numerical studies on single objective optimization

The number of research articles found on the single objective optimization of gate and vent location using numerous deterministic and stochastic techniques. Particle swarm optimization (PSO) and genetic algorithm (GA) found to be the most used stochastic algorithms with the aim of reducing computational time and increasing accuracy [44]. The mostly formulated objective was minimizing mould fill time with reduced void content [45-54]. To optimize the curing stage the majorly formulated objective was cure process time with respect to variables on temperature and cure gradients, a constraint on degree of cure. Table 1 reviews the categorization of single-

objective optimization studies of composite processing in terms of objectives, parameters and numerical techniques.

Table 1. Objective function categorization for Single Objective Optimization of Composite Processing

Objective	Parameters	Numerical Techniques	Reference	Year
Least square error between experimental & predicted data from simulation	In-plane 3D permeability components	FEM, golden section search method	[55]	2011
Flow front progression time	Characterization of 3D permeability	FEM, golden-section search method	[56]	2017
Buckling load, Fundamental frequency, Structural weight	Geometry, Temperature	Meta-heuristic technique	[57]	2018
Stress distribution, Critical buckling load, Fundamental frequency	Material distribution, pattern,	GA, PSO, ANN, ANFIS	[58]	2019
Gate location	Permeability, Fill time, Mould fill fraction	GA, Gradient-based algorithm	[59]	2007
Injection gates and vents	Permeability	Graph-based two-phase heuristic algorithm (GTPH)	[60]	2008
Fill time	Gate and vent location,	Depth-first search and	[61]	2015

	Distribution media, Race-tracking effect	Tree search algorithm		
Total cure cycle time	Central temperature, Duration of two steps	ANSYS, Simulated Annealing (SA), NM-simplex method	[62]	2014
Process cycle time	Mould temperature profile	GA	[63]	2005
Mould fill time	Gate locations	GA, exhaustive search, Centroidal Voronoi Diagram (CVD) method	[64]	2016
Mean square error between corner and centre part of temperature	Temperature	ANN, SQP	[39]	2012

3.2. Numerical studies on multi-objective optimization

Multi-objective optimization (MOO) problem contains more than one objective which is conflicting to each other. Hence, there will be more optimal solutions which are represented in terms of Pareto fronts. The best optimal solutions are called non-dominated solutions. Different MOO techniques have been developed to find out the Pareto front between the quality and productivity of the composite part. Evolutionary algorithms like MOGA, NSGA-II has been mainly used for optimizing the process and design parameters for composite parts. Different objectives addressed using numerous MOO techniques such as mould fill and cure process time, gate and vent location [66], temperature overshoot and degree of cure, etc. Few algorithms have been developed for thick and ultra-thick components for simple geometries to optimize the trade-off between temperature overshoot and cure process time [67]. Table 2 reviews the categorization of multi-objective optimization studies of composite processing in terms of objectives, parameters and numerical techniques.

Table 2. Objective function categorization for Multi-objective Optimization of Composite Processing

Objectives	Parameters	Numerical Techniques	Reference	Year
Crowding distance, Filling time	Gate and vent location	NSGA-II	[66]	2009
Warpage, Shrinkage rate, Short shot possibility	Process parameters: part cooling time, melt temperature, pressure holding time, & mould fill time; Geometric parameters: modified edge & Round gate	FAHP, TOPSIS	[68]	2018
Cure degree difference, Set up cost, Fill time, Variance of cure degree, Cure time	First temperature rise, Dwell time, Dwell temperature, Second temperature rise, Hold temperature	NSGA-II	[65]	2019
Setup cost, Fill time	Resin temperature, Temperature of mould	Hybrid FE/FD method	[69]	2019
Weld line, Fill time, Wasted resin, Dry spot	Gate and vent location	FEA, MOOGA	[70]	2016
Cure time, Temperature	First and second dwell	Surrogate model,	[67]	2018

overshoot	temperature, duration of 1 st dwell, heating rate	Monte-Carlo simulator, MOOGA		
Standard deviation and Average of degree of cure	Mould temperature, Heat flux, Cure part temperature	Ant swarm strategy	[71]	2015
Tensile load, flexural strength	Duration and temperature of the 1 st curing step, heating rate	MOOGA toolbox	[72]	2018
Residual stresses, Cure process time, Degree of cure	Temperature profile	MOOGA	[73]	2006
Cure process time, Temperature gradient, Degree of cure at the end of mould filling, Filling time	Cure profile, Thermal profile of mould filling, Initial resin temperature, Gate & vent location	MOOGA	[74]	2014
Cure process time, Temperature overshoot	Thermal profile, Thickness of composite part, Mould geometry	MOOGA	[75]	2016
Warpage, Volumetric shrinkage and Residual	Fibre content, fibre aspect ratio, Melt temperature,	NSGA-II	[76]	2018

stress		Cooling time, Injection pressure			
Peak tensile residual stress, Roller speed	Degree of bonding, Peak residual stress, & Thermal degradation	NM-Simplex method	[77]	2007	
Maximum difference in degree of cure, Total cure time and Maximum difference in temperature	Temperature, Degree of cure	MOOGA	[78]	2018	
Weld line, Void content, fill time, wasted resin	Void fraction, Distance between gate	MOGA	[16]	2019	

4. The mathematical formulation of optimization problems studied in the literature

4.1. The mathematical formulation of single objective optimization problems

1. An optimal heating control problem was formulated as [79],

$$J = \max_{\Omega} (|\nabla \alpha|_{t_0}) \quad (2)$$

$$\text{Subject to, } \alpha_1 \leq \langle \alpha \rangle_{t_0} \leq \alpha_2$$

$$\langle \alpha \rangle = \int_{\Omega} \alpha(r, T, t) d\omega;$$

$$\langle \nabla \alpha \rangle = \int_{\Omega} |\nabla \alpha(r, T, t)| d\omega$$

The boundaries α_1 and α_2 were used differently at each stage of the process, that is $\alpha_1=0.15$, and $\alpha_2= 0.25$ at liquefaction stage and $\alpha_1=0.97$ and $\alpha_2=1$ at the solidification stage or final stage of

curing.

2. Two different optimization problems were addressed, to minimize the peak tensile residual stress and to maximize the roller velocity of tape placement of thermoplastic composites [77].

$$\begin{aligned}
 & \min \sigma_r \quad (3) \\
 \text{Subject to,} \quad & D_b = 1 \\
 & \alpha_d \leq \alpha_d^{all} \\
 & 0.5\text{cm} \leq h_l \leq 9 \text{ cm} \\
 & 20 \text{ }^\circ\text{C} \leq T_0 \leq 135 \text{ }^\circ\text{C} \\
 & 1 \text{ mm/s} \leq v_r \leq 25 \text{ mm/s} \\
 & 400 \text{ }^\circ\text{C} \leq T_{hg} \leq 750 \text{ }^\circ\text{C} \\
 & \max v_r \\
 \text{Subject to,} \quad & D_b \geq D_{b,min} \\
 & \alpha_d \leq \alpha_d^{max} \\
 & 0.5\text{cm} \leq h_l \leq 9 \text{ cm} \\
 & 20 \text{ }^\circ\text{C} \leq T_0 \leq 135 \text{ }^\circ\text{C} \\
 & 400 \text{ }^\circ\text{C} \leq T_{hg} \leq 1000 \text{ }^\circ\text{C}
 \end{aligned}$$

3. Ruiz & Trochu (2005) proposed the methodology based on GA implemented in C++ to minimize the thermal & cure gradients & the reduction of processing stresses. To increase the convergence rate of the search algorithm seven sub-objectives were constructed with sigmoid functions.

$$F_f(V_d) = \frac{A_f}{B_f + e^{-F_w C_f}} + D_f \quad (4)$$

$$F_w = w_{fc} J_{fc} + w_{T_{max}} J_{T_{max}} + w_{AGP} J_{AGP} + w_{cure} J_{cure} + w_{stress} J_{stress} + w_{cooling} J_{cooling} + w_{time} J_{time}$$

$$\text{Subject to,} \quad V_d \in Cs$$

The vector of design parameters V_d defined as $V_d = [Q_1, dt_1, Q_2, dt_2, Q_3, dt_3, \dots, Q_7, dt_7]$

where the discrete set of Q_i defines the heating ramps and dt_i defines the dwell time. The pair sum of (Q_i, dt_i) describes the mould temperature profile.

The constraint vector $Cs = [T_{init}, T_{room}, Q_{max}^+, Q_{max}^-]$

Where Q_{max}^+ defines the maximum permitted heating ramps, Q_{max}^- defines the maximum cooling ramps allowed by the mould, T_{init} is the initial room temperature and T_{room} the room temperature.

$F_f(V_d)$ is the fitness function to be optimized and parameters w are the weighting coefficient for each subjective function. A_f , B_f , C_f , & D_f are the coefficients of the sigmoid function. The definitions of each sub-objective function described in the article [63].

4.2. The mathematical formulation of multi-objective optimization problems

1. The MOO problem was defined to minimize the die temperature (T_1 , T_2 , T_3), and maximize the pull speed (u) subject to constraints on the degree of cure [80].

$$\min f_1(T) = \frac{c \times m \times [(T_1 - T_0) + (T_2 - T_0) + (T_3 - T_0)]}{\gamma \times t} \quad (5)$$

$$\max f_2(u) = u$$

$$\begin{aligned} \text{Subject to,} \quad & \alpha_c \geq 0.9 \\ & \alpha_c - \alpha_w \leq 0.0035 \\ & 373 \leq T_1 \leq 413 \\ & 413 \leq T_2 \leq 458 \\ & 413 \leq T_3 \leq 458 \\ & 100 \leq u \leq 300 \end{aligned}$$

where c is the special heat of die, m is the mass of die, t is the heating time, T_0 is the environmental temperature, and γ is the thermal efficiency. T_1 , T_2 , T_3 & u are the design variables. This MOO problem was converted into SOO problem by using the weighted average method and constrained problem converted into unconstrained one using the penalty method.

$$\min F(X) = a \times F_1(T) + (1 - a) \times F_2(u) + P(\alpha)$$

where $F_1(T)$ and $F_2(u)$ are unitized forms of $f_1(T)$ and $f_2(u)$ respectively. a is weighting factor a [0,1], $P(\alpha)$ is the penalty function which was expressed as,

$$P(\alpha) = r_1 |\min\{0, \alpha_c - 0.9\}| + r_2 |\min\{0, 0.0035 - \alpha_c + \alpha_w\}|$$

where r_1 and r_2 are penalty parameters.

2. The MOO problem was formulated using the Poisson regression analysis with backward elimination for tensile load and flexural strength. The design variables considered are heating rate (a °C/min), the temperature of the 1st curing step (T_1 °C), and duration of the

1st curing step (h_1 hours). In the flexural strength regression model, only T_1 and h_1 are considered as independent variables because a was removed by backward elimination [72].

$$\max f(a, T_1, h_1) = \begin{cases} \max Tensile\ load = \min(1/tensile\ load) = \min(1/e^{Y'_1}) \\ \max Flexural\ strength = \min(1/flexural\ strength) = \min(1/e^{Y'_2}) \end{cases} \quad (6)$$

where,

$$Y'_1 = -0.3 - 0.8 \times a + 0.524 \times T_1 - 0.83 \times h_1 + 0.784 \times a^2 - 0.002901 \times T_1^2 + 1.547 \times h_1^2 + 5.31 \times a \times h_1 - 0.1979 \times T_1 \times h_1 + 0.000003 \times T_1^3 - 0.285 \times h_1^3 - 0.3327 \times a \times h_1^2 + 0.00099 \times T_1^2 \times h_1 + 0.01975 \times T_1 \times h_1^2 + 0.0153 \times T_1^3 \times h_1 - 0.000064 \times T_1^2 \times h_1^2 - 0.000481 \times T_1 \times h_1^3 - 0.00573 \times a \times h_1^4$$

$$Y'_2 = 4.6336 + 0.009461 \times T_1 + 0.1188 \times h_1 - 0.000792 \times T_1 \times h_1$$

3. The MOO problem has been formulated to find out the fibre content (C_f), fibre aspect ratio (A_f), melting temperature (T_{me}), injecting pressure (P_{in}), and cooling time (t_c) [76].

$$\min f(x) = \{\text{warping, volumetric shrinkage, residual stress}\} \quad (7)$$

subjected to, warpage < 0.15 mm

volumetric shrinkage < 6%

residual stress < 30 MPa

$10\% \leq C_f \leq 30\%$

$10 \leq A_f \leq 50$

$220\text{ }^\circ\text{C} \leq T_{me} \leq 260$

$60\text{ MPa} \leq P_{in} \leq 80\text{ MPa}$

$20\text{ s} \leq t_c \leq 30\text{ s}$

4. To optimize the design variables of cure profile such as 1st temperature rise (Rt_1), dwell temperature, dwell time (T_{dwell}), 2nd temperature rise (Rt_2), & hold temperature (T_{hold}), a MOO problem has been formulated to minimize the conflicting objectives such as difference of cure degree, variance of cure degree and cure time [65].

$$\begin{aligned} \min f_1 &= t|_{\alpha_{\min}=0.9} \\ \min f_2 &= \alpha_{\max} - \alpha_{\min} \\ \min f_3 &= \frac{1}{N} \sum_{i=1}^N (\alpha_i - \alpha_{ave})^2 \end{aligned} \quad (8)$$

Subject to,

$$373 \leq T_{\text{dwell}} \leq 433$$

$$1 \leq Rt_1 \leq 5$$

$$1 \leq Rt_2 \leq 5$$

$$443 \leq T_{\text{hold}} \leq 463$$

$$0 \leq \text{Time}_{\text{dwell}} \leq 90$$

5. Summary and Conclusion

This review article has targeted the process optimization of mould filling and curing steps in the composite moulding process. Bulk and tow permeability, gate and vent location, injection pressure, and component geometry were found to be the crucial parameters for addressing the multi-phase and multi-scale problems for mould filling stage. Whereas, mould temperature, initial temperature of resin, degree of cure, heat flux, temperature gradient and temperature overshoot found to be crucial parameters for optimizing thermal profile in curing stage. To manufacture a void-free composite part with the optimized parameters different optimization techniques have been developed. The number of single objective and multi-objective optimization techniques has been developed to optimize the objectives like the degree of cure, temperature overshoot, process time, gate and vent location and mould fill time. The Nelder mead simplex method, simulated annealing, GA, NSGA-II, and MOOGA are the most used traditional techniques for optimizing the process as well as mould parameters.

Although there are number of articles found on the development of numerical models for addressing multi-scale and multi-phase problems for the complex geometries. The development of an effective optimization technique for addressing such problems is a crucial task. Nowadays, the development of a hybrid multi-objective optimization technique for optimizing the LCM process parameters is an active area of research. Till now, very few articles found on MOO for both mould filling and curing parameters using appropriate optimization techniques. Hence for optimizing the parameters of complex geometry, thick and ultra-thick component development of an effective optimization technique is needed. This may advance the use of LCM technology in the industry for manufacturing large and complex structures instead of traditional techniques.

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