Word Problem Problems? K-5 Schema-Based Instruction





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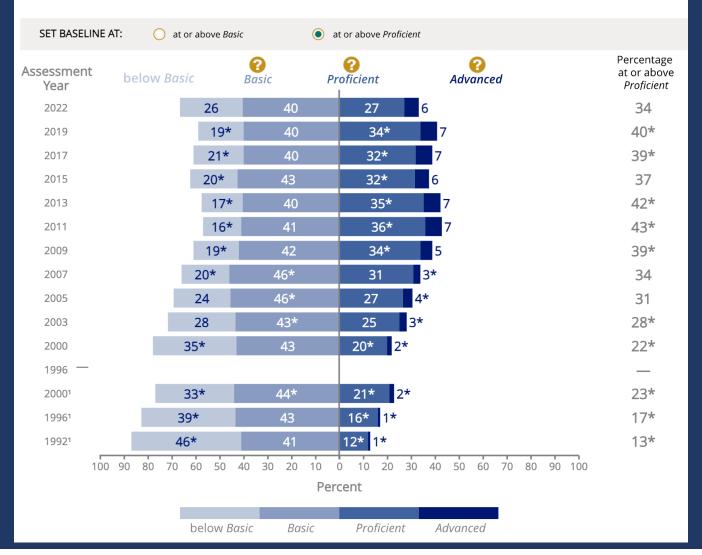
Say hello.

What makes word problems so difficult for students?



GRADE 4 | MATHEMATICS

Average scale scores, percentage , percentage , percentage , percentage and percentage for grade 4 mathematics, by All students jurisdiction: 1990, 1992, 1996, 2000, 2003, 2005, 2007, 2009, 2011, 2013, 2015, 2017, 2019, and 2022





Word Problems



Word Problem Problems? K-5 Schema-Based Instruction srpowell@utexas.edu @sarahpowellphd www.sarahpowellphd.com Research and Information





Key words tied to operations is an ineffective wordproblem strategy.

(Karp et al., 2019; Powell et al., 2022)

Using a meta-cognitive strategy improves word-problem performance.

(Freeman-Green et al., 2015; Krawec et al., 2012; Montague et al., 2011; Swanson et al., 2014)

A focus on schemas improves word-problem performance. (Alghamdi et al., 2020; Cook et al., 2020; Flores et al., 2016; Fuchs et al., 2021; Griffin et al., 2019; Jitendra et al., 2013; Lein et al., 2020; Peltier et al., 2020; Powell et al., 2022; Xin & Xhang, 2009; Zheng et al., 2013)



Ineffective Strategies





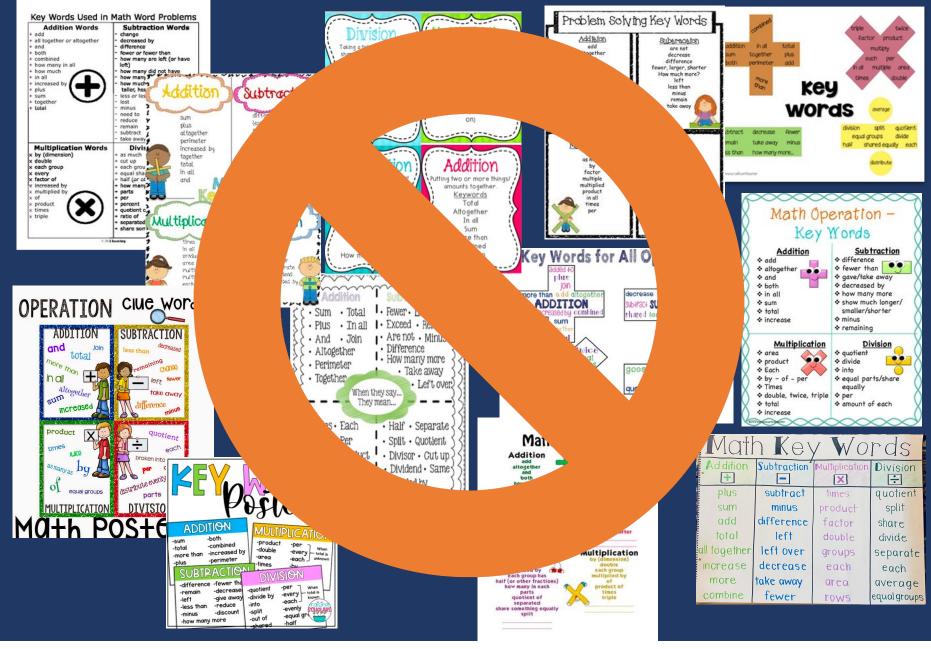




Carmelita had 8 pencils **fewer** than Jenny. If Jenny had 18 pencils, how many pencils did Carmelita have?

Carmelita had 8 pencils **fewer** than Jenny. If Carmelita had 18 pencils, how many pencils did Jenny have?













Description of Single-St	ep Word i	Problem	s (n = 132	?)						
					Schei	ma-			Keyword	(s) led
	Occurre	nce of	An	у	spec	ific	Multi	ple	to con	rect
	schema		keyword		keywords ^a		keywords ^a		solutiona	
Schema	n	%	n	%	n	%	n	%	n	%
Total	27	20.5	26	96.3	23	88.5	5	19.2	21	80.8
Difference	17	12.9	17	100.0	14	82.4	2	11.8	12	70.6
Change	11	8.3	7	63.6	5	71.4	5	71.4	2	28.6
Equal groups	29	22.0	26	89.7	22	84.6	18	69.2	8	30.8
Comparison	10	7.6	9	90.0	9	100.0	4	44.4	5	55.6
Ratios or proportions	29	22.0	23	79.3	9	39.1	9	39.1	6	26.1
Product of measures	9	6.8	9	100.0	8	88.9	1	11.1	5	55.6
^a When a problem featu	ired a key	word.								





_	Occurren schem	_	Any keywor	d	Keyword(s) l correct solu	
Schema	n	%	n	%	n	%
Total	40	47.6	39	97.5	3	7.7
Difference	11	13.1	11	100.0	1	9.1
Change	21	23.8	19	95.0	1	5.3
Equal groups	49	58.3	48	98.0	1	2.1

8.3

8.3

25.0

Comparison

Ratios or proportions

Product of measures

Description of Multi-Step Word Problems (n = 84)



0.0

6.3

28.6

100.0

76.2

100.0

16

^aSum across schemas does not equal 100 because each word problem featured more than one schema.

^bWhen a problem featured a keyword.

Keywords are important to identify and understand

Keywords are the mathematical vocabulary that help an students understand what the story is about and what they need to do

Talk about keywords ("What does *more than* tell you about?")

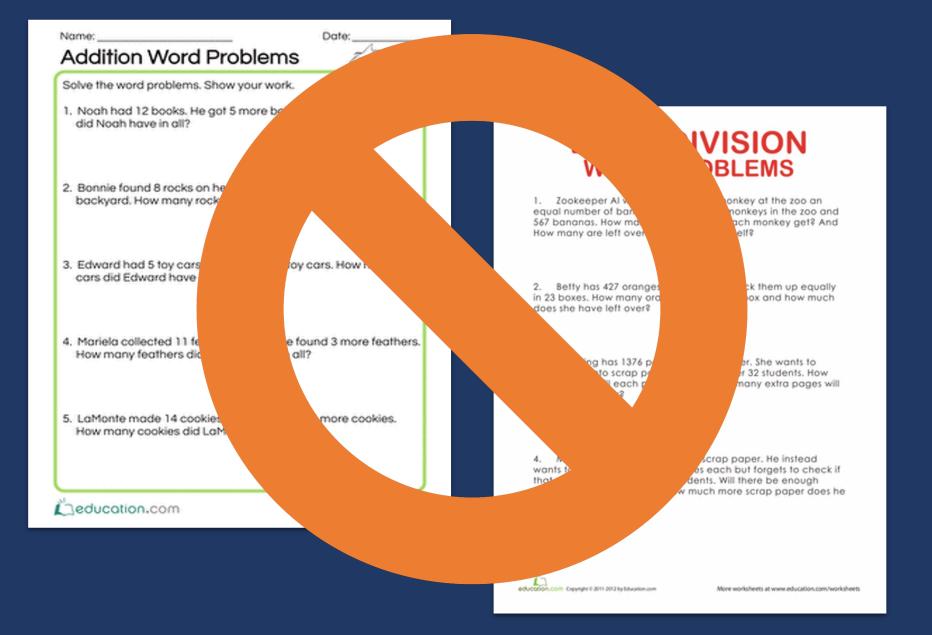


But, do not tie a keyword to a specific operation!









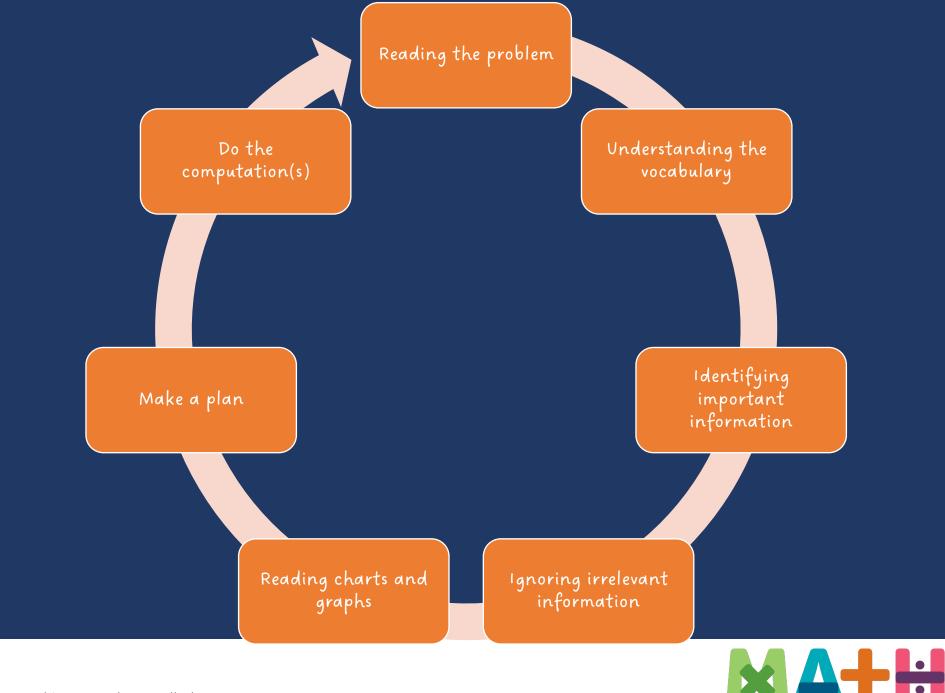


Effective Strategies



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Research and Information





Teach an attack strategy

Teach about schemas



WORD PROBLEMS

Attack Strategies

SOLVE

Study the problem
Organize the information
Line up a plan
Verify the plan
Examine the answer

UPS Check Understand Plan Solve

Check

R-CUBES

Read the problem
Circle key numbers
Underline the question
Box action words
Evaluate steps
Solve and check





RIDE

Read the problem.

Identify the relevant information.

Determine the operation and unit for the answer.

Enter the correct numbers and calculate, then check the answer.

RICE

Read and record the problem.
Illustrate your thinking.
Compute.

Explain your thinking.

RIDGES

Read the problem.

I know statement.

Draw a picture.

Goal statement.

Equation development.

Solve the equation.



SUPER

Slowly read the story problem twice.

Underline the question and circle the numbers you need.

Picture it. Draw the scenario to show what is happening.

Explain the problem with a number sentence.

Rewrite the answer in a sentence.

STAR

SHINES

Slowly and carefully read the problem.

Highlight or underline key information.

Identify the question by drawing a circle around it.

Now solve the problem. Show your work. Examine your work for precision, accuracy, and clarity.

Share your answer by writing a sentence.

Stop and read the problem carefully.

Think about your plan and the strategy you will use.

Act. Follow your plan and solve the problem.

Review your answer.



SOLVE

Study the problem.

Organize the facts.

Line up the plan.

Verify the plan with computation.

Examine the answer.

R-CUBES

Read the problem.
Circle key numbers.
Underline the question.
Box action words.
Evaluate steps.
Solve and check.

UPS UNDERSTAND

PLAN
How will you solve the problem?

SOLVE
Set up and do the math!



Created by: Sarah Powell (srpowell@austin.utexas.edu





Share your favorite attack strategy.



Teach an attack strategy

Teach about schemas



Difference

Change

Equal Groups

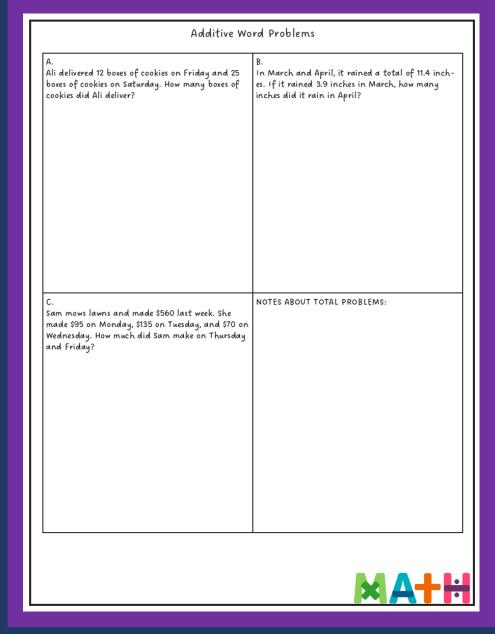
Comparison

Ratios/Proportions



Schema and Definition	Equations and Graphic Organizers	Examples			Variations
Total (Combine; Part-part- whole) Parts combined for a sum	P1 + P2 = T (part + part = total) (total) (part) (part)	Sum unknown: Lyle has 11 red apples and 18 green apples. How many apples does Lyle have altogether?	Part unknown: Lyle has 29 red and green apples. If 11 of the apples are red, how many green apples does Lyle have?		More than two parts: Lyle has 34 apples. Of the apples, 11 are red, 18 are green, and the rest are yellow. How many yellow apples does Lyle have?
Difference (Compare) Sets compared for a difference	B - s = D (bigger - smaller = difference) (greater - less = difference) (greater) (greater) (greater) (difference)	Difference unknown: Sasha wrote 85 words in her essay, and Tabitha wrote 110 words. How many fewer words did Sasha write than Tabitha?	Bigger/greater un- known: Tabitha wrote 25 more words than Sasha. If Sasha wrote 85 words, how many words did Tabitha write?	Smaller/lesser unknown: Tabitha wrote 110 words in her essay. Sasha wrote 25 words fewer than Tabitha. How many words did Sasha write?	(None)
Change (Join; Separate) An amount that increases or decreases	ST +/- C = E (start +/- change = end) (start) (change) (end)	End (increase) unknown: Jorge had \$52. Then, he earned \$16 babysitting. How much money does Jorge have now?	Change (increase) unknown: Jorge had \$52. Then, he earned some money babysitting. Now, Jorge has \$68. How much did Jorge earn babysitting?	Start (increase) un- known: Jorge has some money, and then he earned \$16 for babysitting. Now, Jorge has \$68. How much money did he have to start with?	Multiple changes: Jorge had \$78. He stopped and bought a pair of shoes for \$42 and then he spent \$12 at the grocery. How much money does Jorge have now?
	(change) (end)	End (decrease) unknown: Jorge had \$52. Then, he spent \$29 at the ballpark. How much money does Jorge have now?	Change (decrease) unknown: Jorge had \$52 but spent some money when he went to the ballpark. Now, Jorge has \$23. How much did Jorge spend at the ballpark?	Start (decrease) unknown: Jorge had some money. Then, he spent \$29 at the ballpark and has \$23 left. How much money did Jorge have before going to the ballpark?	







Part-part-whole Combine

Parts put together into a total

Mandy saw 3 canoes and 8 kayaks. How many boats did Mandy see?

Mandy saw 11 boats. If 3 of the boats were canoes, how many were kayaks?

Mandy saw 11 boats. 8 of the boats were kayaks, how many were canoes?

Total

Part

Part



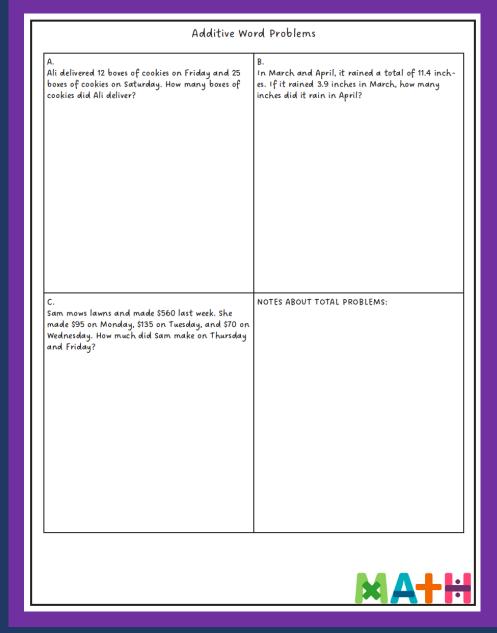
"Are parts put together for a total?"



P1 + P2 = T

(total) (part) (part)









Share a Total problem.



Difference

Additive Word Problems Audrey has 162 wooden beads and 95 glass beads. Damian's dog eats 9 1/2 cups of dog food each What is the difference between Audrey's wooden week. Monte's dog eats 4 1/4 cups less each week beads and glass beads? than Damian's dog. How much does Monte's dog eat in a week? NOTES ABOUT DIFFERENCE PROBLEMS: The temperature in Norfolk was 12 degrees warmer than in Roanoke where the temperature was 79 degrees. It was 86 degrees in Marion. What was the temperature in Norfolk?



Difference

Compare

Greater and lesser amounts compared for a difference

L'Tanya has 10 pencils. Vickie has 4 pencils. How many more pencils does L'Tanya have?

L'Tanya has 6 more pencils than Vickie. If Vickie has 4 pencils, how many does L'Tanya have?

Vickie has 6 fewer pencils than L'Tanya. L'Tanya has 10 pencils. How many pencils does Vickie have?

Difference

Greater amount

Lesser amount



Total

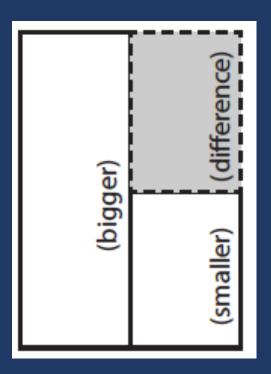
"Are parts put together for a total?"

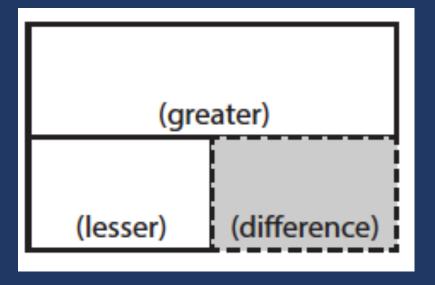
Difference

"Are amounts compared for a difference?"



D







Difference

Additive Word Problems Audrey has 162 wooden beads and 95 glass beads. Damian's dog eats 9 1/2 cups of dog food each What is the difference between Audrey's wooden week. Monte's dog eats 4 1/4 cups less each week beads and glass beads? than Damian's dog. How much does Monte's dog eat in a week? NOTES ABOUT DIFFERENCE PROBLEMS: The temperature in Norfolk was 12 degrees warmer than in Roanoke where the temperature was 79 degrees. It was 86 degrees in Marion. What was the temperature in Norfolk?



Difference



Share a Difference problem.



Additive Word Problems A plant was 3 3/4 inches tall at the beginning of Martina has some money in her bank account. June. By the end of July, the plant was 9 1/8 inch-Then, she spent \$135.69 and has a balance of es tall. How many inches did the plant grow in 2 -\$24.80. How much money did Martina have to begin with? NOTES ABOUT CHANGE PROBLEMS: Hui saved \$70 in January. In February, she spent \$64 of the money she saved. She saved \$92 more in March. How much has Hui saved by the end of





Join

An amount that increases or decreases

Annette had 6 notebooks. Then, she bought 3 notebooks. How many notebooks does Annette have now?

End amount

Annette had 6 notebooks. Then, she bought a few more notebooks. Now, Annette has 9 notebooks. How many notebooks did she buy?

Change amount

Annette had some notebooks. Then, she bought 3 notebooks. Now, Annette has 9 notebooks. How many notebooks did she have to start with?

Start amount



Separate

An amount that increases or decreases

Jenny baked 20 cookies. Then, she ate 3 of the cookies. How many cookies does Jenny have now?

End amount

Jenny baked 20 cookies. Then, she ate some of the cookies. Now, she has 17 cookies. How many cookies did Jenny eat?

Change amount

Jenny baked some cookies. She ate 3 of the cookies and has 17 cookies left. How many cookies did Jenny bake?

Start amount



Total

"Are parts put together for a total?"

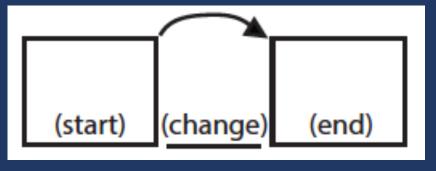
Difference

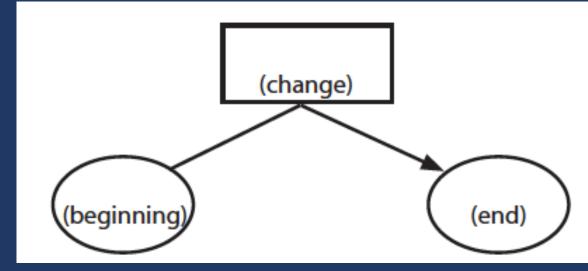
"Are amounts compared for a difference?"

Change

"Does an amount increase or decrease?"









Fuchs et al. (2008); Griffin & Jitendra (2009)

Additive Word Problems A plant was 3 3/4 inches tall at the beginning of Martina has some money in her bank account. June. By the end of July, the plant was 9 1/8 inch-Then, she spent \$135.69 and has a balance of es tall. How many inches did the plant grow in 2 -\$24.80. How much money did Martina have to begin with? NOTES ABOUT CHANGE PROBLEMS: Hui saved \$70 in January. In February, she spent \$64 of the money she saved. She saved \$92 more in March. How much has Hui saved by the end of







Share a Change problem.



Total

Difference

Change

Equal Groups

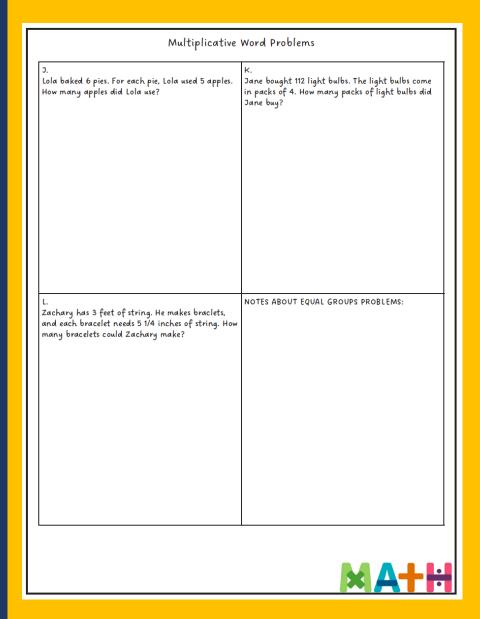
Comparison

Ratios/Proportions



Schema and Definition	Graphic Organizers	Examples			Variations
Equal Groups (Vary) A number of equal sets or units	$GR \times N = P$ $Groups' \times Order = Order$	Product unknown: Maria bought 5 cartons of eggs with 12 eggs in each carton. How many eggs did Maria buy?	Groups unknown: Maria bought 60 eggs. The eggs were sold in cartons with 12 eggs each. How many cartons of eggs did Maria buy?	Number unknown: Maria bought 5 cartons of eggs for a total of 60 eggs. How many eggs were in each carton?	With rate: Maria bought 5 cartons of eggs. Each carton cost \$2.95. How much did Maria spend on eggs?
Comparison One set as a multiple or part of another set	$S \times T = P$ $(set) \times (multiplier/ (product))$	Product unknown: Malik picked 7 flowers. Danica picked 3 times as many flowers. How many flowers did Danica pick?	set unknown: Danica picked 3 times as many flowers as Malik. If Danica picked 21 flowers, how many flowers did Malik pick?	Times unknown: Malik picked 7 flowers. Danica picked 21 flowers. How many times more flowers did Danica pick?	with fraction: Malik picked 25 red and yellow flowers. If 1/5 of the flowers were yellow, how many were red?
Ratios/ Proportions (Percentages; Unit Rate) Relationships among quantities	IF THEN	subject unknown: Sally typed 56 words in 2 minutes. How many words could Sally type in 7 minutes?	Object unknown: Sally typed 56 words in 2 minutes. How many minutes would it take Sally to type 192 words?		With percentage: Watson received an 80% on his science quiz. If the test had 40 questions, how many questions did Watson answer correctly?
Ratio	COMPARED RATIO BASE	Base unknown: Justin baked cookies and brownies. The ratio of cookies to brownies was 3:5. If he baked 15 cookies, how many brownies did he bake?	Compared unknown: Justin baked cookies and brownies. The ratio of cookies to brownies was 3:5. If he baked 25 brownies, how many cookies did he bake?	Ratio unknown: Justin baked 15 cookies and 25 brownies. What's the ratio of cookies to brownies?	With unit rate: Paula bought 5 boxes of markers. She spent \$9.75. What is the price of one box of markers?







Array Vary

Groups multiplied by number in each group for a product

Mandy has 2 boxes. There are 6 muffins in each box. How many muffins does Mandy have?

Product

Mandy has 12 muffins. They want to place them equally into 2 boxes. How many muffins will Mandy place in each box?

Number in each group

Mandy has 12 muffins. They put them into boxes with 6 muffins each. How many boxes did Mandy use?

Groups



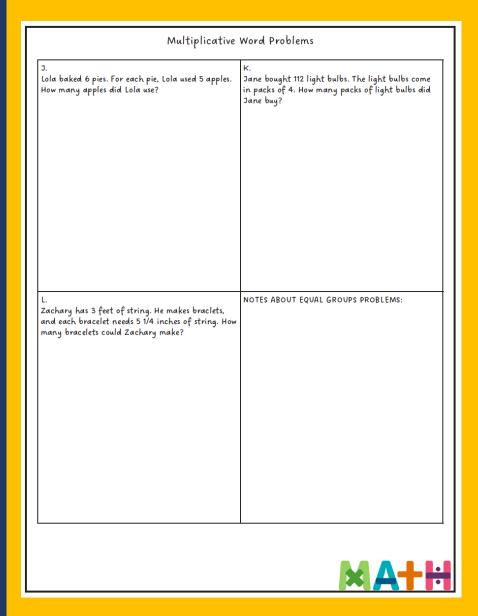
"Are there groups with an equal number in each group?"



$$GR \times N = P$$
 $GR \times E = P$

(groups/ (number/ (product) units) rate)









Share an Equal Groups problem.



Multiplicative Word Problems					
M. Enrique has 2 times as many pencils as Ava. Ava has 6 pencils. How many pencils does Enrique have?	N. Susan has 7 times as many books as Mo. Mo has 18 books. How many books Susan has?				
NOTES ABOUT COMPARISON PROBLEMS:					
	MA+H				



set multiplied by a number of times for a product

Joan ran 6 minutes. L'Tanya ran 4 times longer than Joan. How many minutes did L'Tanya run?

Set

Number of times

Product



"Are there groups with an equal number in each group?"

Comparison

"Is a set compared a number of times?"





Multiplicative Word Problems					
M. Enrique has 2 times as many pencils as Ava. Ava has 6 pencils. How many pencils does Enrique have?	N. Susan has 7 times as many books as Mo. Mo has 18 books. How many books Susan has?				
NOTES ABOUT COMPARISON PROBLEMS:					
	MATH				





Share a Comparison problem.



Total

Difference

Change

Equal Groups

Comparison

Ratios/Proportions



Mr. Abdul has a Ferrari, but Mr. Stark has 75 times more Ferraris than him. Who is cooler than Mr. Abdul?



For a three day walk a thon, Mekhi walked 1.5 miles on Monday, 4 miles on Tuesday, and 2.5 on Wed. What was the total that Mekhi walked during the 3 days?



There are 72 students in fifth grade. Each student has three notebooks. How many notebooks do all fifth grade students have all together?

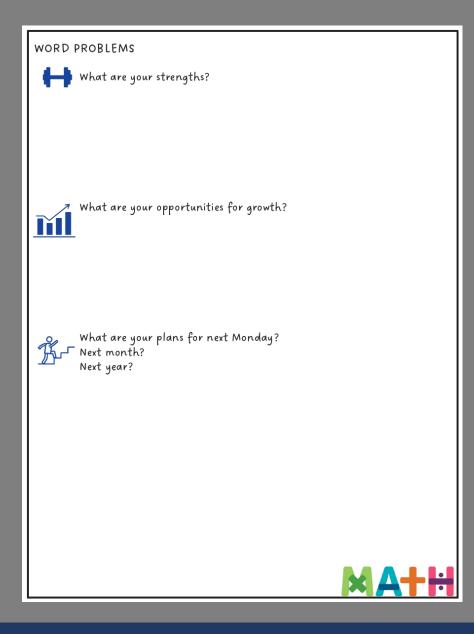


Mrs. Smith's class had 4 more students than Mr. Bell's class. Mr. Bell's class has 19 students. How many students are in Mrs. Smith's class?



Martha had \$62 in her checking account. She then made a withdrawal of \$15. How much money is in her account now?









Pirate Math Equation Quest



About

Research

Individual

Small Group

STAAR

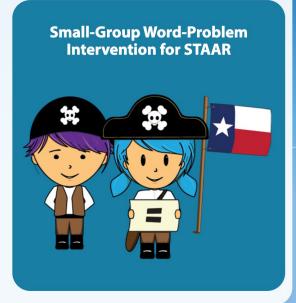
Videos



Welcome to Pirate Math Equation Quest!











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MODULE 5: INTENSIVE MATHEMATICS INTERVENTION: INSTRUCTIONAL STRATEGIES

Intensive Intervention in Mathematics Course Content

NCII, through a collaboration with the University of Connecticut, developed a set of course content focused on developing educators' skills in designing and delivering intensive mathematics instruction. This content is designed to support faculty and professional development providers with instructing paservice and in-service educators who are developing and/or refining their implementation of intensive mathematics intervention.

Intensive instruction was recently identified as a high-leverage practice in special education , and DBI is a research based approach to delivering intensive instruction across content areas (NCII, 2013). This course provides learners with an opportunity to extend their understanding of intensive instruction through in-depth exposure to DBI in mathematics, complete with exemplars from actual classroom teachers.

NCII, through a collaboration with the University of Connecticut and the National Center on Leadership in Intensive Intervention and with support from the CEEDAR Center , developed course content focused on enhancing educators' skills in intensive mathematics intervention. The course includes eight modules that can support faculty and professional development providers with instructing pre-service and in-service educators who are learning to implement intensive mathematics intervention through data-based individualization (DBI). The content in this course complements concepts covered in the Features of Explicit Instruction Course and so we suggest that users complete both courses.







Instructional Routines for Mathematics Intervention

The purpose of these mathematics instructional routines is to provide educators with materials to use when providing intervention to students who experience difficulty with mathematics. The routines address content included in the grades 2-8 Texas Essential Knowledge and Skills (TEKS). There are 23 modules that include routines and examples – each focused on different mathematical content. Each of the 23 modules include vocabulary cards and problem sets to use during instruction. These materials are intended to be implemented explicitly with the aim of improving mathematics outcomes for students.





https://spedsupportstage.tea.texas.gov/resource-library/instructional-routines-mathematics-intervention



https://ies.ed.gov/ncee/wwc/PracticeGuide/26



Assisting Students Struggling with Mathematics: Intervention in the Elementary Grades

Educator's Practice Guide

What Works Clearinghouse™

WWC 2021006 U.S. DEPARTMENT OF EDUCATION

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