

Solomon Press
Core Mathematics C4
Paper F
(Question Paper)

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GCE Examinations
Advanced Subsidiary

Core Mathematics C4

Paper F

Time: 1 hour 30 minutes

Instructions and Information

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration.

Full marks may be obtained for answers to ALL questions.

Mathematical formulae and statistical tables are available.

This paper has seven questions.

Advice to Candidates

You must show sufficient working to make your methods clear to an examiner.
Answers without working may gain no credit.



Written by Shaun Armstrong

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6. (a) Find $\int \tan^2 x \, dx$. (3)

(b) Show that

$$\int \tan x \, dx = \ln |\sec x| + c,$$

where c is an arbitrary constant. (4)

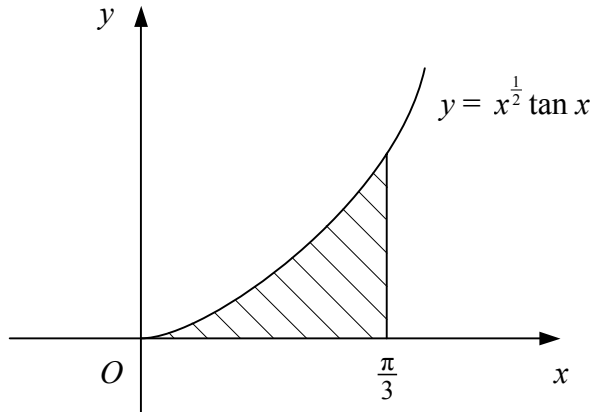


Figure 1

Figure 1 shows part of the curve with equation $y = x^{\frac{1}{2}} \tan x$.

The shaded region bounded by the curve, the x -axis and the line $x = \frac{\pi}{3}$ is rotated through 2π radians about the x -axis.

(c) Show that the volume of the solid formed is $\frac{1}{18} \pi^2 (6\sqrt{3} - \pi) - \pi \ln 2$. (6)

7.

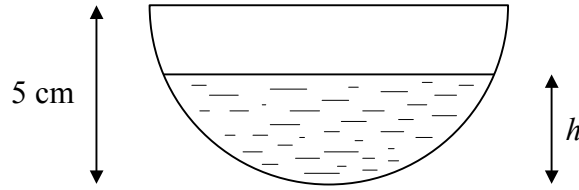


Figure 2

Figure 2 shows a hemispherical bowl of radius 5 cm.

The bowl is filled with water but the water leaks from a hole at the base of the bowl. At time t minutes, the depth of water is h cm and the volume of water in the bowl is V cm³, where

$$V = \frac{1}{3}\pi h^2(15 - h).$$

In a model it is assumed that the rate at which the volume of water in the bowl decreases is proportional to V .

(a) Show that

$$\frac{dh}{dt} = -\frac{kh(15 - h)}{3(10 - h)},$$

where k is a positive constant. (5)

(b) Express $\frac{3(10 - h)}{h(15 - h)}$ in partial fractions. (3)

Given that when $t = 0$, $h = 5$,

(c) show that

$$h^2(15 - h) = 250e^{-kt}. \quad (6)$$

Given also that when $t = 2$, $h = 4$,

(d) find the value of k to 3 significant figures. (3)
