



## Riemann Paper (1859) Is False

Jiang Chun-Xuan  
 P. O. Box 3924, Beijing 100854, P. R. China  
[jcxuan002@sina.com](mailto:jcxuan002@sina.com), & [jiangchunxuan234e@126.com](mailto:jiangchunxuan234e@126.com)

### ABSTRACT

In 1859 Riemann defined the zeta function  $\zeta(s)$ . From Gamma function he derived the zeta function with Gamma function  $\bar{\zeta}(s)$ .  $\bar{\zeta}(s)$  and  $\zeta(s)$  are the two different functions. It is false that  $\bar{\zeta}(s)$  replaces  $\zeta(s)$ . After him later mathematicians put forward Riemann hypothesis(RH) which is false. The Jiang function  $J_n(\omega)$  can replace RH.

AMS mathematics subject classification: Primary 11M26.

[Chun-Xuan, J. (2016). Riemann Paper (1859) Is False. *The Journal of Middle East and North Africa Sciences*, 2(7), 11-16]. (P-ISSN 2412- 9763) - (e-ISSN 2412-8937). [www.jomenas.org](http://www.jomenas.org), 3

**Keywords:** Riemann hypothesis, Gamma function.

In 1859 Riemann defined the Riemann zeta function (RZF) (Riemann, 1859)

$$\zeta(s) = \prod_p (1 - P^{-s})^{-1} = \sum_{n=1}^{\infty} \frac{1}{n^s}, \tag{1}$$

where  $s = \sigma + ti$ ,  $i = \sqrt{-1}$  ranges over all primes. RZF is the function of the complex  $P$  are real,  $t$  and  $\sigma$ , variable  $s$  in  $\sigma \geq 0, t \neq 0$ , which is absolutely convergent.

In 1896 J. Hadamard and de la Vallee Poussin proved independently (Borwin, 2007)

$$\zeta(1+ti) \neq 0. \tag{2}$$

In 1998 Jiang proved (Jiang, 2005)

$$\zeta(s) \neq 0, \tag{3}$$

where  $0 \leq \sigma \leq 1$ .

**Riemann paper (1859) is false (Riemann, 1859).** We define Gamma function (Riemann, 1859; Borwin, 2007)

$$\Gamma\left(\frac{s}{2}\right) = \int_0^{\infty} e^{-t} t^{\frac{s}{2}-1} dt. \tag{4}$$

For  $\sigma > 0$ . On setting  $t = n^2 \pi x$ , we observe that

$$\pi^{-\frac{s}{2}} \Gamma\left(\frac{s}{2}\right) n^{-s} = \int_0^{\infty} x^{\frac{s}{2}-1} e^{-n^2 \pi x} dx. \tag{5}$$

Hence, with some care on exchanging summation and integration, for  $\sigma > 1$ ,

$$\pi^{-\frac{s}{2}} \Gamma\left(\frac{s}{2}\right) \bar{\zeta}(s) = \int_0^{\infty} x^{\frac{s}{2}-1} \left( \sum_{n=1}^{\infty} e^{-n^2 \pi x} \right) dx$$

$$= \int_0^\infty x^{\frac{s}{2}-1} \left( \frac{\mathcal{G}(x)-1}{2} \right) dx, \tag{6}$$

where  $\bar{\zeta}(s)$  is called Riemann zeta function with gamma function rather than  $\zeta(s)$ ,

$$\mathcal{G}(x) := \sum_{n=-\infty}^\infty e^{-n^2\pi x}, \tag{7}$$

is the Jacobi theta function. The functional equation for  $\mathcal{G}(x)$  is

$$x^{\frac{1}{2}}\mathcal{G}(x) = \mathcal{G}(x^{-1}), \tag{8}$$

and is valid for  $x > 0$ .

Finally, using the functional equation of  $\mathcal{G}(x)$ , we obtain

$$\bar{\zeta}(s) = \frac{\pi^{\frac{s}{2}}}{\Gamma\left(\frac{s}{2}\right)} \left\{ \frac{1}{s(s-1)} + \int_1^\infty \left(x^{\frac{s}{2}-1} + x^{-\frac{s}{2}-\frac{1}{2}}\right) \cdot \left(\frac{\mathcal{G}(x)-1}{2}\right) dx \right\}. \tag{9}$$

From (9) we obtain the functional equation

$$\pi^{-\frac{s}{2}}\Gamma\left(\frac{s}{2}\right)\bar{\zeta}(s) = \pi^{-\frac{1-s}{2}}\Gamma\left(\frac{1-s}{2}\right)\bar{\zeta}(1-s). \tag{10}$$

The function  $\bar{\zeta}(s)$  satisfies the following

1.  $\bar{\zeta}(s)$  has no zero for  $\sigma > 1$ ;
  2. The only pole of  $\bar{\zeta}(s)$  is at  $s = 1$ ; it has residue 1 and is simple;
  3.  $\bar{\zeta}(s)$  has trivial zeros at  $s = -2, -4, \dots$  but  $\zeta(s)$  has no zeros;
  4. The nontrivial zeros lie inside the region  $0 \leq \sigma \leq 1$  and are symmetric about both the vertical line  $\sigma = 1/2$ .
- The strip  $0 \leq \sigma \leq 1$  is called the critical strip and the vertical line  $\sigma = 1/2$  is called the critical line.

**Conjecture** (The Riemann Hypothesis). All nontrivial zeros of  $\bar{\zeta}(s)$  lie on the critical line  $\sigma = 1/2$ , which is false (Jiang, 2005)

$\bar{\zeta}(s)$  and  $\zeta(s)$  are the two different functions. It is false that  $\bar{\zeta}(s)$  replaces  $\zeta(s)$ , Pati proved that is not all complex zeros of  $\bar{\zeta}(s)$  lie on the critical line:  $\sigma = 1/2$  (Pati, (2007).

Schadeck pointed out that the falsity of RH implies the falsity of RH for finite fields (Schadeck, 2008). RH is not directly related to prime theory. Using RH mathematicians prove many prime theorems which are false. In 1994

Jiang discovered Jiang function  $J_n(\omega)$  which can replace RH, Riemann zeta function, and L-function in view of its proved feature: if  $J_n(\omega) \neq 0$  then the prime equation has infinitely many prime solutions; and if  $J_n(\omega) = 0$ ,

then the prime equation has finitely many prime solutions. By using  $J_n(\omega)$  Jiang proves about 600 prime theorems including the Goldbach's theorem, twin prime theorem and theorem on arithmetic progressions in primes (Jiang 2002, 2006).

In the same way, we have a general formula involving  $\bar{\zeta}(s)$

$$\int_0^\infty x^{s-1} \sum_{n=1}^\infty F(nx) dx = \sum_{n=1}^\infty \int_0^\infty x^{s-1} F(nx) dx$$

$$= \sum_{n=1}^{\infty} \frac{1}{n^s} \int_0^{\infty} y^{s-1} F(y) dy = \overline{\zeta}(s) \int_0^{\infty} y^{s-1} F(y) dy \tag{11}$$

where  $F(y)$  is arbitrary.

From (11) we obtain many zeta functions  $\overline{\zeta}(s)$  which are not directly related to the number theory. The prime distributions are order rather than random. The arithmetic progressions in primes are not directly related to ergodic theory, harmonic analysis, discrete geometry, and combinatorics. Using the ergodic theory Green and Tao prove that there exist infinitely many arithmetic progressions of length  $k$  consisting only of primes which are false (Kra, 2006; Green & Tao 2008; Tao, 2005). Fermat's last theorem (FLT) is not directly related to elliptic curves. In 1994 using elliptic curves Wiles proved FLT which is false (Wiles, 1995; Zhivotov, 2006a; Zhivotov, 2006b). There are Pythagorean theorem and FLT in the complex hyperbolic functions and complex trigonometric functions. In 1991 without using any number theory Jiang proved FLT which is Fermat's marvelous proof (Jiang, 2002).

**Primes Represented by  $P_1^n + mP_2^n$  (Jiang, 2003)**

1 (Let  $n = 3$  and  $m = 2$ . We have

$$P_3 = P_1^3 + 2P_2^3$$

We have Jiang function

$$J_3(\omega) = \prod_{3 \leq P} (P^2 - 3P + 3 - \chi(P)) \neq 0$$

Where  $\chi(P) = 2P - 1$  if  $2^{\frac{P-1}{3}} \equiv 1 \pmod{P}$ ;  $\chi(P) = -P + 2$  if  $2^{\frac{P-1}{3}} \not\equiv 1 \pmod{P}$ ;  $\chi(P) = 1$  otherwise.

Since  $J_n(\omega) \neq 0$ , there exist infinitely many primes  $P_1$  and  $P_2$  such that  $P_3$  is a prime.

We have the best asymptotic formula

$$\pi_2(N, 3) = \left| \{P_1, P_2 : P_1, P_2 \leq N, P_1^3 + 2P_2^3 = P_3 \text{ prime}\} \right|$$

$$\sim \frac{J_3(\omega)\omega}{6\Phi^3(\omega)} \frac{N^2}{\log^3 N} = \frac{1}{3} \prod_{3 \leq P} \frac{P(P^2 - 3P + 3 - \chi(P))}{(P-1)^3} \frac{N^2}{\log^3 N}$$

$$\omega = \prod_{2 \leq P} P \quad \Phi(\omega) = \prod_{2 \leq P} (P-1)$$

where  $\prod_{2 \leq P} P$  is called primorial,

It is the simplest theorem which is called the Heath-Brown problem (Heath-Brown, 2001).

2 (Let  $n = P_0$  be an odd prime,  $2|m$  and  $m \neq \pm b^{P_0}$ .

we have

$$P_3 = P_1^{P_0} + mP_2^{P_0}$$

We have

$$J_3(\omega) = \prod_{3 \leq P} (P^2 - 3P + 3 - \chi(P)) \neq 0$$

where  $\chi(P) = -P + 2$  if  $P|m$ ;  $\chi(P) = (P_0 - 1)P - P_0 + 2$  if  $m^{\frac{P-1}{P_0}} \equiv 1 \pmod{P}$ ;

$\chi(P) = -P + 2$  if  $m^{\frac{P-1}{P_0}} \not\equiv 1 \pmod{P}$ ;  $\chi(P) = 1$  otherwise.

Since  $J_n(\omega) \neq 0$ , there exist infinitely many primes  $P_1$  and  $P_2$  such that  $P_3$  is a prime.

We have

$$\pi_2(N, 3) \sim \frac{J_3(\omega)\omega}{2P_0\Phi^3(\omega)} \frac{N^2}{\log^3 N}$$

**The Polynomial  $P_1^n + (P_2 + 1)^2$  Captures Its Primes** (Jiang, 2003)

) 1 (Let  $n = 4$ , We have

$$P_3 = P_1^4 + (P_2 + 1)^2,$$

We have Jiang function

$$J_3(\omega) = \prod_{3 \leq P} (P^2 - 3P + 3 - \chi(P)) \neq 0,$$

Where  $\chi(P) = P$  if  $P \equiv 1 \pmod{4}$ ;  $\chi(P) = P - 4$  if  $P \equiv 1 \pmod{8}$ ;  $\chi(P) = -P + 2$  otherwise.

Since  $J_n(\omega) \neq 0$ , there exist infinitely many primes  $P_1$  and  $P_2$  such that  $P_3$  is a prime.

We have the best asymptotic formula

$$\pi_2(N, 3) = |\{P_1, P_2 : P_1, P_2 \leq N, P_1^4 + (P_2 + 1)^2 = P_3 \text{ prime}\}|$$

$$\sim \frac{J_3(\omega)\omega}{8\Phi^3(\omega)} \frac{N^2}{\log^3 N}.$$

It is the simplest theorem which is called Friedlander-Iwaniec problem (Friedlander, & Iwaniec 1998).

) 2 (Let  $n = 4m$ , We have

$$P_3 = P_1^{4m} + (P_2 + 1)^2,$$

where  $m = 1, 2, 3, \dots$ .

We have Jiang function

$$J_3(\omega) = \prod_{3 \leq P \leq P_i} (P^2 - 3P + 3 - \chi(P)) \neq 0,$$

where  $\chi(P) = P - 4m$  if  $8m | (P - 1)$ ;  $\chi(P) = P - 4$  if  $8 | (P - 1)$ ;  $\chi(P) = P$  if  $4 | (P - 1)$ ;  $\chi(P) = -P + 2$  otherwise.

Since  $J_3(\omega) \neq 0$ , there exist infinitely many primes  $P_1$  and  $P_2$  such that  $P_3$  is a prime. It is a generalization of Euler proof for the existence of infinitely many primes.

We have the best asymptotic formula

$$\pi_2(N, 3) \sim \frac{J_3(\omega)\omega}{8m\Phi^3(\omega)} \frac{N^2}{\log^3 N}.$$

) 3 (Let  $n = 2b$ . We have

$$P_3 = P_1^{2b} + (P_2 + 1)^2,$$

where  $b$  is an odd.

We have Jiang function

$$J_3(\omega) = \prod_{3 \leq P} (P^2 - 3P + 3 - \chi(P)) \neq 0,$$

Where  $\chi(P) = P - 2b$  if  $4b | (P - 1)$ ;  $\chi(P) = P - 2$  if  $4 | (P - 1)$ ;  $\chi(P) = -P + 2$  otherwise.

We have the best asymptotic formula

$$\pi_2(N, 3) \sim \frac{J_3(\omega)\omega}{4b\Phi^3(\omega)} \frac{N^2}{\log^3 N}.$$

) 4 (Let  $n = P_0$ , We have

$$P_3 = P_1^{P_0} + (P_2 + 1)^2$$

where  $P_0$  is an odd. Prime.

we have Jiang function

$$J_3(\omega) = \prod_{3 \leq P} (P^2 - 3P + 3 - \chi(P)) \neq 0$$

where  $\chi(P) = P_0 + 1$  if  $P_0 | (P-1)$ ;  $\chi(P) = 0$  otherwise.

Since  $J_3(\omega) \neq 0$ , there exist infinitely many primes  $P_1$  and  $P_2$  such that  $P_3$  is also a prime.

We have the best asymptotic formula

$$\pi_2(N, 3) \sim \frac{J_3(\omega)\omega}{2P_0\Phi^3(\omega)} \frac{N^2}{\log^3 N}$$

The Jiang function  $J_n(\omega)$  is closely related to the prime distribution. Using  $J_n(\omega)$  we are able to tackle almost all prime problems in the prime distributions.

### Acknowledgements

The Author would like to express his deepest appreciation to R. M. Santilli, L. Schadeck and Chen I-wan for their help and supports.

### Corresponding Author:

Jiang Chun-Xuan,

P. O. Box 3924, Beijing 100854, P. R. China

Email: [jcxuan002@sina.com](mailto:jcxuan002@sina.com), & [jiangchunxuan234e@126.com](mailto:jiangchunxuan234e@126.com)

### References

1. Borwin, P., Choi, S., & Rooney, B. (2007). The Riemann Hypothesis.
2. Chun-Xuan, J. (2005). Disproofs of Riemann's hypothesis. *Algebras Groups and Geometries*, 22, 123-136.
3. Friedlander, J., & Iwaniec, H. (1998). The polynomial  $x^2 + y^4$  captures its primes. *Annals of Mathematics*, 148, 945-1040.
4. Green, B., & Tao, T. (2008). The primes contain arbitrarily long arithmetic progressions. *Annals of Mathematics*, 481-547.
5. Heath-Brown, D. R. (2001). Primes represented by  $x^3 + 2y^3$ . *Acta Math.*, 186(1), 1-84.
6. Jiang, C. X. (2003). Prime theorem in Santilli's isonumber theory (II). *Algebras Groups and Geometries*, 20, 149-170.
7. Jiang, C. X. (2006). The simplest proofs of both arbitrarily long arithmetic progressions of primes. preprint.
8. Jiang, C. X., (2002). *Foundations of Santilli's Isonumber Theory: With Applications to New Cryptograms, Fermat's Theorem and Goldbach's Conjecture*. International academic press.
9. Kra, B. (2006). The Green-Tao theorem on arithmetic progressions in the primes: an ergodic point of view. *Bulletin of the American Mathematical Society*, 43(1), 3-23.
10. Pati, T. (2007). the Riemann hypothesis. arXiv preprint math/0703367.



11. Riemann, B. (1859). Ueber die Anzahl der Primzahlen unter einer gegebenen Grosse. Ges. Math. Werke und Wissenschaftlicher Nachlaß, 2, 145-155.
12. Schadeck, L. (2008). Jiang Number Theory (JNT).
13. Tao, T. (2005). The dichotomy between structure and randomness, arithmetic progressions, and the primes. arXiv preprint math/0512114.
14. Wiles, A. (1995). Modular elliptic curves and Fermat's last theorem. Annals of mathematics, 141(3), 443-551.
15. Zhivotov, Y. (2006). Fermat last theorem and mistakes of Andrew Wiles.  
[www.baoway.com/bbs/viewthread.php?tid=18162&fpage=3](http://www.baoway.com/bbs/viewthread.php?tid=18162&fpage=3).
16. Zhivotov, Y. (2006). Fermat last theorem and Kenneth Ribet mistakes.  
[www.baoway.com/bbs/viewthread.php?tid=18164&fpage=3](http://www.baoway.com/bbs/viewthread.php?tid=18164&fpage=3).

Received May 15, 2016; revised June 10, 2016; accepted June 10, 2016; published online July 01, 2016.