

Abstract

The work studies **resilient distributed multi-task learning (MTL)** problem in a network of agents aiming to learn distinct but correlated models simultaneously. Some of the agents in the network are possibly **Byzantine** and their objective is to disrupt and prevent normal (non-adversarial) agents from achieving the MTL objective. We present and analyze a Byzantine-resilient distributed MTL approach whereby a normal agent **adaptively assigns weights** to its neighbors based on **similarities** with them, which are measured based on the accumulated loss of the **agent's data and its neighbors' models**. A small accumulated loss indicates a large similarity and vice-versa. We show that using the proposed weight assignment, normal agents with convex models **converge resiliently** towards their true target.

Highlights

- The proposed approach is resilient to an **arbitrary number of Byzantine agents** and require no knowledge of the number of Byzantine agents in the network.
- The learning performance is guaranteed to be at least **as good as the non-cooperative case**.
- A normal agent computes weights in time that is **linear** in the size of its neighborhood and the dimension of the data.

MTL

- A network of m agents $G = (V, E)$.
- Each agent k has data $\{(x_k^i, y_k^i)\}$ (sampled randomly from the distribution of ξ_k .)
- Prediction function: $f_k(x_k^i) = \theta_k^T x_k^i$
- Model parameter: θ_k
- Loss function: $\ell_k(\cdot)$
- Expected risk function: $r_k(\theta_k) = \mathbb{E}[\ell_k(\theta_k; \xi_k)]$

Objective:

$$\min_{\Theta} \left\{ \sum_{k=1}^m r_k(\theta_k) + \eta \mathcal{R}(\Theta, \Omega) \right\},$$

where, $\Theta = [\theta_1, \theta_2, \dots, \theta_m]$, $\mathcal{R}(\cdot)$ is a regularization function, and Ω is a relationship matrix among agents.

Distributed MTL

Adapt-then-Combine Strategy: At each iteration i , agent k minimizes the individual risk using stochastic gradient descent (SGD) given local data followed by a combination step that aggregates neighboring models according to the weights assigned.

$$\hat{\theta}_{k,i} = \theta_{k,i-1} - \mu_k \nabla \ell_k(\theta_{k,i-1}; \xi_k^{i-1}) \quad (\text{Adapt})$$

$$\theta_{k,i} = \sum_{l \in \mathcal{N}_k} a_{lk} \hat{\theta}_{l,i} \quad \text{subject to} \quad (\text{Combine})$$

$$\sum_{l \in \mathcal{N}_k} a_{lk} = 1, a_{lk} \geq 0, a_{lk} = 0 \text{ if } l \notin \mathcal{N}_k$$

Main challenge is to design suitable **weights, a_{lk}** .

Resilient Distributed MTL

Goal: Design resilient online weight assignment rule for MTL in the presence of Byzantine agents.

Weight Assignment:

$$a_{lk}(i) = \begin{cases} \frac{r_k(\hat{\theta}_{l,i}^{(\text{coop})})^{-1}}{\sum_{p \in \mathcal{N}_k^{\leq}} r_k(\hat{\theta}_{p,i}^{(\text{coop})})^{-1}}, & \text{if } r_k(\hat{\theta}_{l,i}^{(\text{coop})}) \leq r_k(\hat{\theta}_{k,i}^{(\text{coop})}), \\ 0, & \text{otherwise,} \end{cases}$$

Main Results

Resilient convergence: Using the computed weights, each normal agent resiliently converges to the true target.

$$\lim_{i \rightarrow \infty} \theta_{k,i}^{(\text{coop})} = \theta_k^*, \quad \forall k,$$

Improved expected regret compared to non-cooperation: The computed weights result in an improved expected regret as compared to using the SGD without cooperation, even with Byzantine agents.

$$\limsup_{i \rightarrow \infty} R_k^{(\text{coop})}(i) \leq \limsup_{i \rightarrow \infty} R_k^{(\text{ncop})}(i), \quad \forall k.$$

Computational efficiency: At each i , agent k computes weights in time linear in the size of neighborhood of k and the dimension of data.

Evaluation

We evaluated the resilience of the proposed online weight adjustment rule using three distributed MTL case studies, with and without Byzantine agents.

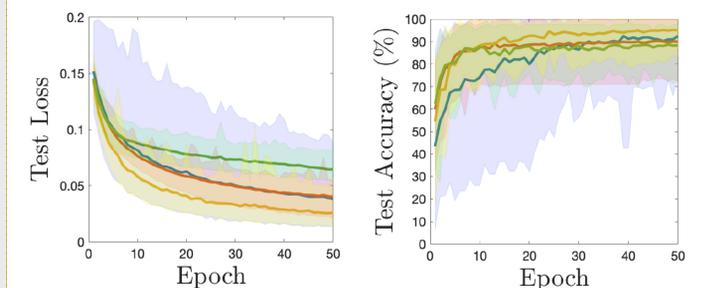
- Target localization** (regression problem)
- Human activity recognition** (classification)
- Digit classification** (non-convex model)

Evaluation – Human Activity Recognition

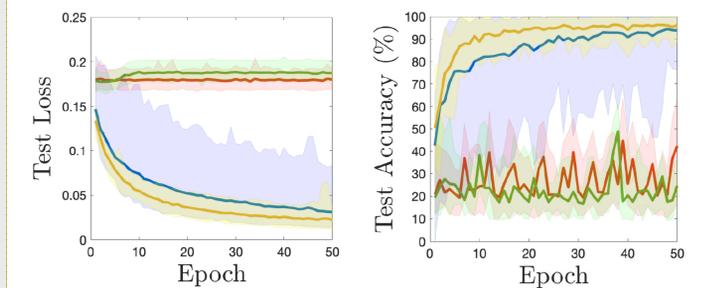
Goal: Predict activities (walking, walking upstairs, downstairs, sitting, standing, lying) using feature vectors generated by the sensor signals.

Set-up:

- Mobile phone sensor data of 30 individuals.
- Complete network topology.
- Byzantine agents continuously send random values.



(a) No attack



(c) 10 Byzantine agents



Concluding remark: The approach is easily extendable to general resilient distributed machine learning and federated learning systems.